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Separation of benzene from mixtures with water, methanol, ethanol, and acetone: highlighting hydrogen bonding and molecular clustering influences in CuBTC[†]

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Configurational-bias Monte Carlo (CBMC) simulations are used to establish the potential of CuBTC for separation of water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures. For operations under pore saturation conditions, the separations are in favor of molecules that partner benzene; this is due to molecular packing effects that disfavor benzene. CBMC simulations for adsorption of quaternary water/methanol/ethanol/benzene mixtures show that water can be selectively adsorbed at pore saturation, making CuBTC effective in drying applications. Ideal Adsorbed Solution Theory (IAST) calculations anticipate the right hierarchy of component loadings but the quantitative agreement with CBMC mixture simulations is poor for all investigated mixtures. The failure of the IAST to provide reasonable quantitative predictions of mixture adsorption is attributable to molecular clustering effects that are induced by hydrogen bonding between water–water, methanol–methanol, and ethanol–ethanol molecule pairs. There is, however, no detectable hydrogen bonding between benzene and partner molecules in the investigated mixtures. As a consequence of molecular clustering, the activity coefficients of benzene in the mixtures is lowered below unity by one to three orders of magnitude at pore saturation; such drastic reductions cannot be adequately captured by the Wilson model, that does not explicitly account for molecular clustering. Molecular clustering effects are also shown to influence the loading dependence of the diffusivities of guest molecules.

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1. Introduction

Several recent publications have highlighted the potential of metal–organic frameworks (MOFs) and zeolitic imidazolate frameworks (ZIFs) for separation of hexane isomers,^{1,2} xylene isomers,^{3–6} styrene/ethylbenzene,^{7–10} and water/alcohols.^{11–13} A common distinguishing feature of these separations is that

under industrially relevant operating conditions, the pores of the microporous adsorbents are invariably saturated.¹⁴ Under pore saturation conditions, the separation hierarchy and selectivity is dictated by molecular packing effects; molecular packing effects favor the selective adsorption of molecules with the higher packing efficiencies.^{9,13–15} For example, 1,3,5 trichlorobenzene can be selectively separated from its isomers due to optimum face-to-face stacking within the triangular channels of Fe₂(BDP)₃.⁶ Generally speaking, smaller molecules pack more efficiently and have higher saturation capacities; this implies that under pore saturation conditions smaller molecules can be selectively adsorbed from mixtures, in preference to larger-sized molecules.^{12,13,15–19} For example, Motkuri *et al.*¹⁵ have suggested that TetZB (that was synthesized using a flexible tetrahedral organic linker tetrakis[4-(carboxyphenyl)-oxamethyl]methane) has the potential of separation of variety of mixtures of polar compounds by exploiting molecular packing effects. It noteworthy that the Motkuri analysis of separations is based on the key assumption that the Ideal Adsorbed Solution Theory (IAST) theory of Myers and Prausnitz²⁰ affords an adequate description of mixture adsorption equilibrium. IAST calculations were also used by Zhang *et al.*¹¹ and

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[†] Electronic supplementary information (ESI) available: This material provides (a) structural details of CuBTC, (b) configurational-bias Monte Carlo (CBMC) and molecular dynamics (MD) simulation methodologies including specification of force fields, (c) snapshots showing the location of adsorbed molecules within CuBTC framework, (d) 2-site and 3-site Langmuir–Freundlich fit parameters for unary isotherms, (e) data on radial distribution functions (RDF) to confirm H-bonding effects, (f) details of the methodology used to calculate activity coefficients from CBMC mixture simulations, and (g) details of IAST and RAST calculation procedures. Also uploaded are video animations of MD simulations of unary diffusivities in CuBTC wherein clustering effects are visualized. See DOI: 10.1039/c5cp02726h

He *et al.*²¹ to demonstrate the potential of hydrophobic adsorbents such as ZIF-8, ZIF-71, ZIF-80, and MAF-6 for water/alcohol

separations. Strictly, the applicability of the IAST is restricted to cases in which there is a homogenous distribution of adsorbate species throughout the microporous framework; IAST predictions may fail to provide quantitative predictions when segregation or clustering effects are present.^{22–25}

The primary objective of this article is to demonstrate the exploitation of molecular packing effects to separate benzene from mixtures containing one or more of the following compounds: water, methanol, ethanol, and acetone. We choose hydrophilic CuBTC (=Cu₃(BTC)₂ with BTC = 1,3,5-benzenetricarboxylate, also known as HKUST-1) as adsorbent, used also in our earlier study on separation of water/1-alcohol mixtures.¹³ The motivation for the current study arises from the following considerations. The dehydration of ethanol/gasoline mixtures is important for avoidance of phase-separation problems during storage;²⁶ we may consider benzene to be representative of gasoline as regards its phase equilibrium thermodynamics. The separation of water/ethanol/benzene mixtures is also encountered in the distillation processes for water/ethanol separations using benzene as entrainer. The distillation process schemes are complicated due

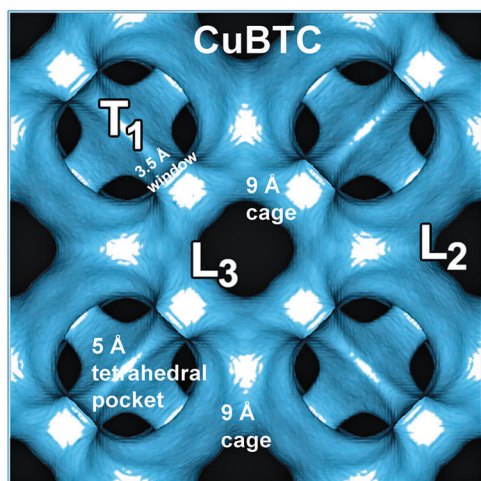


Fig. 1 Pore landscape and cage connectivity of CuBTC framework.

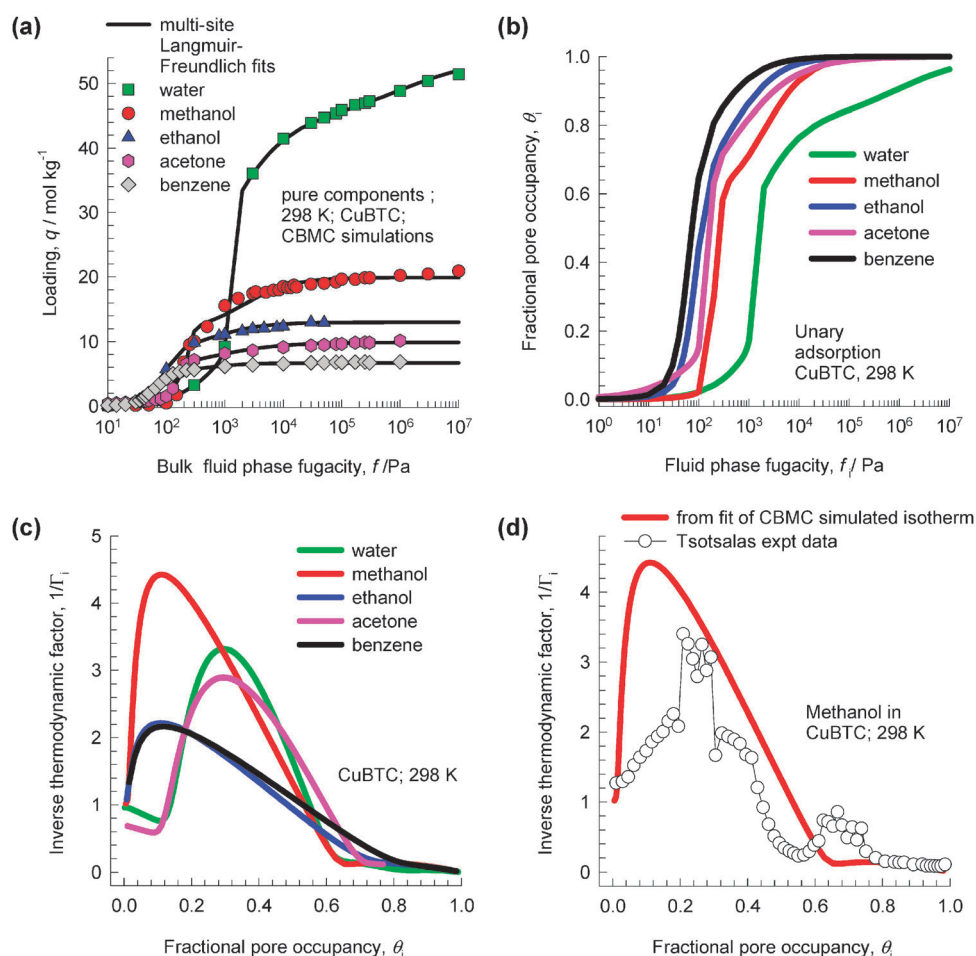


Fig. 2 (a) Comparison of the CBMC simulations for adsorption of water, methanol, ethanol, acetone, and benzene in CuBTC at 298 K with multi-site-Langmuir–Freundlich model fits. (b) Fractional pore occupancies, θ_i , versus bulk phase fluid fugacity. (c) The inverse thermodynamic factor, $1/\Gamma_i$, plotted as a function of θ_i . (d) The experimental data of Tsotsalis *et al.*³³ for $1/\Gamma_i$ vs. θ_i for methanol in CuBTC at 298 K, compared with corresponding data obtained in this work.

to the occurrence of four separate minimum boiling azeotropes: ethanol/water, ethanol/benzene, water/benzene, and water/ethanol/benzene. Acetone cannot be easily separated from benzene in high purity by distillation because of the closeness of their vapor pressures.²⁷

The secondary objective of this article is to highlight the influence of molecular clustering, resulting from hydrogen bonding, on both adsorption and diffusion of guest species in CuBTC. We aim to demonstrate that molecular clustering induces strong non-ideality effects in mixture adsorption, and the IAST fails to provide quantitative predictions of separation performance.

We use configurational-bias Monte Carlo (CBMC) simulations to generate the required information on unary and mixture isotherms in CuBTC. The CBMC and Molecular Dynamics (MD) simulation methodologies, including details of force fields used, are provided in the ESI,[†] accompanying this manuscript.

2. Steep isotherms, and molecular clustering

The CuBTC framework is composed of copper atoms connected by benzene-1,3,5-tricarboxylate (BTC) linkers, which form a characteristic paddle-wheel structure: two copper atoms bonded

to the oxygen atoms of four BTC linkers, generating four-connected square-planar vertexes. The framework contains two types of large cavities (9 Å diameter) and small cavities (of 5 Å diameter). The larger cavities (L_2 and L_3) are similar in size and shape but as a result of the paddle-wheel, the copper atoms are only accessible from the L_3 cages. L_2 and L_3 cavities are connected through triangular-shaped windows. The small cavities (T_1) are tetrahedral pockets enclosed by the benzene rings; these are connected to L_3 cages by small triangular windows (3.5 Å size), as shown in Fig. 1.

The CBMC simulated unary isotherms for water, methanol, ethanol, acetone, and benzene in CuBTC at 298 K exhibit marked inflections, requiring fitting with the multi-site Langmuir–Freundlich model; see Fig. 2a. The accuracy of the fits is excellent for all five guest molecules. Particularly noteworthy are the differences in the saturation capacities of the various guest molecules: water = 54 mol kg⁻¹; methanol = 19.9 mol kg⁻¹; ethanol = 13 mol kg⁻¹; acetone = 9.9 mol kg⁻¹; benzene = 6.7 mol kg⁻¹. Let us define the fractional pore occupancy, $\theta_i = q_i/q_{i,sat}$; the variation of the pore occupancies with bulk fluid phase fugacity, f_i , is shown in Fig. 2b. We note that the pore occupancies are close to unity for operation at ambient conditions of 100 kPa and 298 K.

A further characteristic feature of the unary isotherms is the steep increase in the loadings; this suggests the formation of

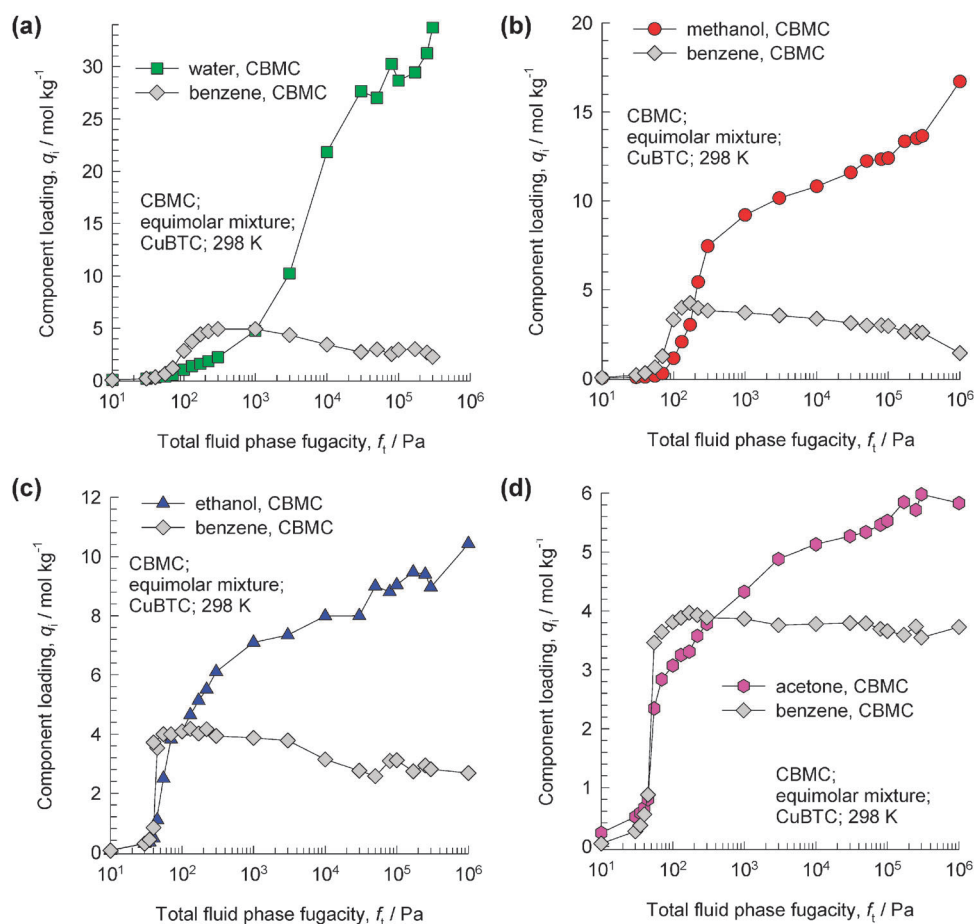


Fig. 3 CBMC simulations for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) acetone/benzene mixtures in CuBTC at 298 K.

molecular clusters, as has been argued in earlier publications.^{28–30} In order to explore cluster formation in more detail, we determine the inverse thermodynamic factor, $1/\Gamma_i$, defined by $\frac{1}{\Gamma_i} \equiv \frac{\partial \ln q_i}{\partial \ln f_i} = \frac{f_i \partial q_i}{q_i \partial f_i}$ by analytic differentiation of the Langmuir–Freundlich model fits. The data for $1/\Gamma_i$ are presented in Fig. 2c. We prefer to plot $1/\Gamma_i$ instead of Γ_i because the latter has the undesirable property of approaching infinity as saturation loading is approached; this makes the data less easy to interpret when plotted in graphical form. For the simplest scenario in which single-site Langmuir isotherm hold, we have $1/\Gamma_i = (1 - \theta_i) = (1 - q_i/q_{i,\text{sat}})$, i.e. the fractional vacancy. In previous works,^{28–32} we had argued that the condition $1/\Gamma_i > 1$ implies the increase of fractional vacancy beyond unity and this is physically rationalized if we allow for molecular clustering. We note from Fig. 2c that $1/\Gamma_i$ exceeds unity for a certain range of pore occupancies below about 0.5 for all five guest molecules. Also noteworthy, is that clustering effects seem to be more prominent for water, methanol, and ethanol; this is evidenced by larger increases in the $1/\Gamma_i$ values above unity.

Confirmation of clustering effects of polar molecules in CuBTC is provided by the experimental data of Tsotsalas *et al.*³³ Fig. 2d compares the $1/\Gamma_i$ values obtained by Tsotsalas *et al.*³³ for methanol, by numerical piece-wise differentiation of their experimental isotherms, with the values plotted in Fig. 2c. There is reasonable agreement between the two data sets.

3. CBMC simulations of mixture adsorption, and comparisons with IAST

Fig. 3, panels a, b, c, and d, present the results for CBMC simulations of the component loadings for adsorption of equimolar water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures in CuBTC at 298 K. For all four mixtures, we note a reversal in the hierarchy of component loadings as conditions approach pore saturation. From the data in Fig. 3 we conclude that CuBTC has the potential of separation of separating binary mixtures of benzene with water, methanol,

ethanol, and acetone. For operation near pore saturation conditions, the selectivity is in favor of the smaller partner molecule in the mixture with higher saturation capacity. Fig. 4 presents the CBMC simulations for equimolar quaternary

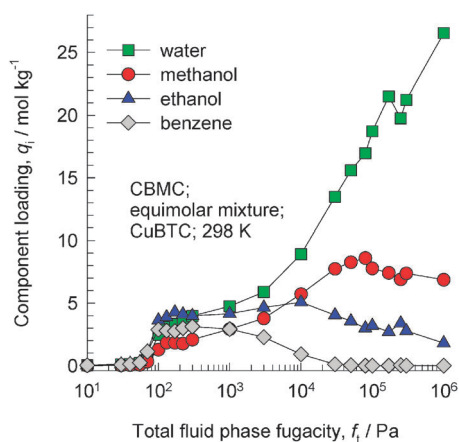


Fig. 4 CBMC simulations for equimolar water/methanol/ethanol/benzene mixtures in CuBTC at 298 K.

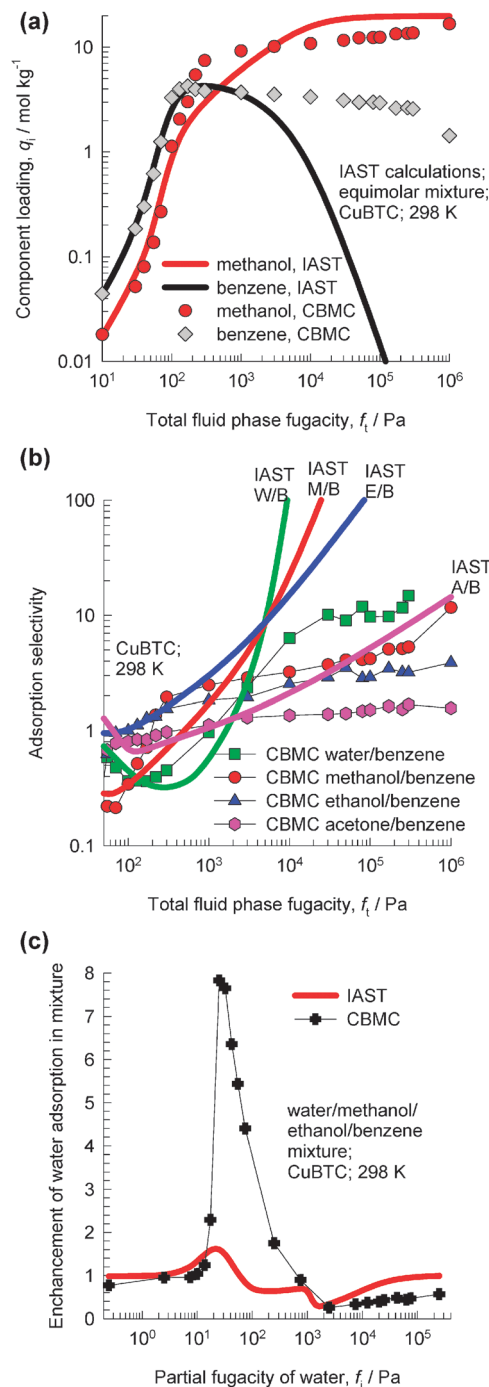


Fig. 5 (a) Comparison of CBMC simulations for equimolar methanol/benzene mixtures in CuBTC at 298 K with IAST calculations (b) Comparison of the adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures in CuBTC at 298 K determined from CBMC mixture simulations with IAST calculations. (c) CBMC simulations for the enhancement of water ingress into CuBTC from water/methanol/ethanol/benzene mixtures, as compared to that of pure water. The continuous solid line represents the IAST calculations.

water/methanol/ethanol/benzene mixtures; the data clearly indicate that water can be selectively adsorbed from a mixture containing alcohols and benzene provided the operations are close to pore saturation conditions. CuBTC is a good candidate for drying water/alcohol/benzene mixtures.

We now examine whether the IAST theory provides a quantitative representation of mixture adsorption. Fig. 5a compares the IAST calculations with CBMC simulations of component loadings of equimolar methanol/benzene mixtures. The IAST correctly anticipates that the adsorption is favorable to the component with the higher saturation capacity as saturation conditions are approached. However, except for $f_t < 100$ Pa in the Henry regime of adsorption, the quantitative agreement between the IAST and CBMC simulations is poor. Similar poor agreement between CBMC and IAST is observed for all other mixtures that have been investigated; see Fig. S22–S25 of the ESI.†

The separation performance anticipated by IAST calculations is overly optimistic; this is demonstrated by the comparisons presented in Fig. 5b for adsorption selectivities determined from CBMC mixture simulations with IAST calculations for equimolar binary mixtures. Typically, at pore saturation, the selectivities estimated by IAST are about an order of magnitude higher than those determined from CBMC mixture simulations.

A different method of underscoring the quantitative failure of IAST is afforded by the plot presented in Fig. 5c for water adsorption in CuBTC from water/methanol/ethanol/benzene mixtures. Herein, we divide the loadings of water in the mixture by the loadings of pure water, both compared at the same partial fugacity in the bulk fluid phase. The CBMC mixture simulations show that the “enhancement” factor of water reaches a value of about 8. The IAST calculations indicated by the continuous solid lines do not anticipate such a strong enhancement. Similar results are obtained for other mixtures; see Fig. S25 of ESI.† The most likely reason for this enhancement is H-bonding between water and partner molecules; the partner molecules “drag” water into the CuBTC framework.

Experimental evidence of the enhancement of water ingress into MFI zeolite due to H-bonding effects with partner alcohol molecules can be inferred from the experimental data of Farzaneh *et al.*³⁴ for water/butanol mixture adsorption in all-silica MFI zeolite at 308 K; see Fig. S44 of ESI.†

In membrane pervaporation of water/alcohol mixtures, an important consequence of enhanced water ingress into microporous adsorbents is that the water fluxes are higher than anticipated on the basis of unary isotherm data. Some experimental evidence of this is available in the work of Villegas *et al.*³⁵

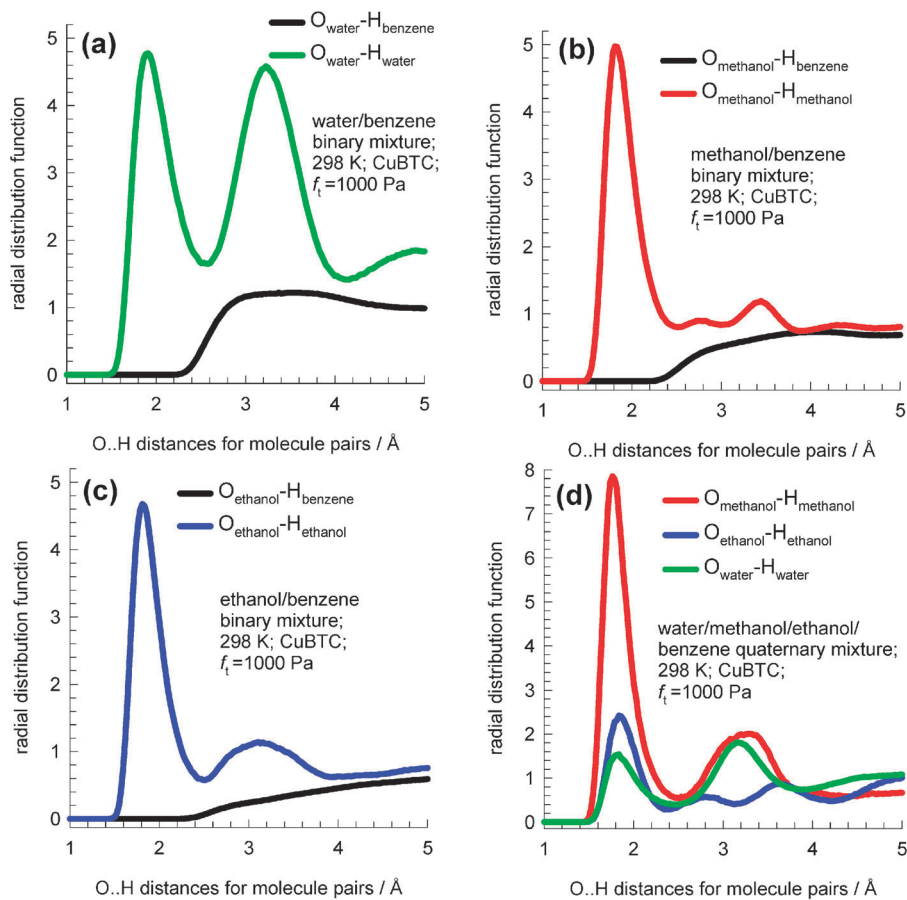


Fig. 6 (a–c) Comparing the RDFs for $H_{\text{benzene}}-O_{\text{molecule}}$ and $H_{\text{molecule}}-O_{\text{molecule}}$ distances for (a) water/benzene, (b) methanol/benzene, and (c) ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa. (d) Comparing the RDFs for $H_{\text{molecule}}-O_{\text{molecule}}$ distances for quaternary water/methanol/ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa.

4. Radial distribution functions, and evidence of H-bonding effects

The most likely reason for the failure of IAST to accurately match CBMC mixture simulations is the phenomenon of molecular clustering; cluster formation is most likely induced by hydrogen bonding. To seek confirmation of this hypothesis, we determined the radial distribution functions (RDFs) for distances between all combinations of O and H atoms of molecule pairs; the methodology used is the same as in our previous work.²⁸ Fig. 6, panels a, b, c, and d, presents comparisons of the RDFs for $H_{\text{benzene}}-O_{\text{molecule}}$ and $H_{\text{molecule}}-O_{\text{molecule}}$ distances for water/benzene, methanol/benzene, ethanol/benzene, and water/methanol/ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa. We note that the RDFs for $H_{\text{water}}-O_{\text{water}}$, $H_{\text{methanol}}-O_{\text{methanol}}$, and $H_{\text{ethanol}}-O_{\text{ethanol}}$ pairs each exhibit a first peak at an intermolecular distance of 2 Å, that is characteristic of hydrogen bonding.^{28,36} The results presented in Fig. 6d show that H-bonding between alcohol/alcohol pairs are stronger than the bonding between water/water pairs. It appears that the presence of adsorbed benzene molecules has a strong influence on clustering of water molecules.

Remarkably, the corresponding values for $H_{\text{benzene}}-O_{\text{water}}$, $H_{\text{benzene}}-O_{\text{methanol}}$, and $H_{\text{benzene}}-O_{\text{ethanol}}$ do not display any

peaks in the RDFs. This would indicate that these partner molecules do not form clusters with benzene molecules, and clustering effects are restricted to water/water, methanol/methanol, and ethanol/ethanol pairs. In order for further verify this finding we determined the RDFs for $H_{\text{benzene}}-O_{\text{molecule}}$ distances for water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures in CuBTC at 298 K and five different total fluid fugacity values; see Fig. 7. For the wide range of fugacities, $f_t = 40\text{--}10\,000$ Pa, no peaks are observed at any molecule-benzene distance, confirming that the benzene does not form clusters with partner molecules. For ethanol/benzene mixtures in the bulk fluid phase, the molecular simulations of Požar *et al.*³⁷ have revealed micro-segregation effects.

The clustering phenomena experienced by the molecules partnering benzene provides a rationalization of the reduction in the selectivity with respect to benzene when compared to the IAST predictions as witnessed in Fig. 5b. At pore saturation conditions, the separations are dictated by differences in the saturation capacities of the constituent species. The phenomenon of molecular clustering of the partner molecules water, methanol, ethanol, and acetone have the apparent effect of reducing the saturation capacity because a cluster may occupy the approximately the same site as occupied by unclustered

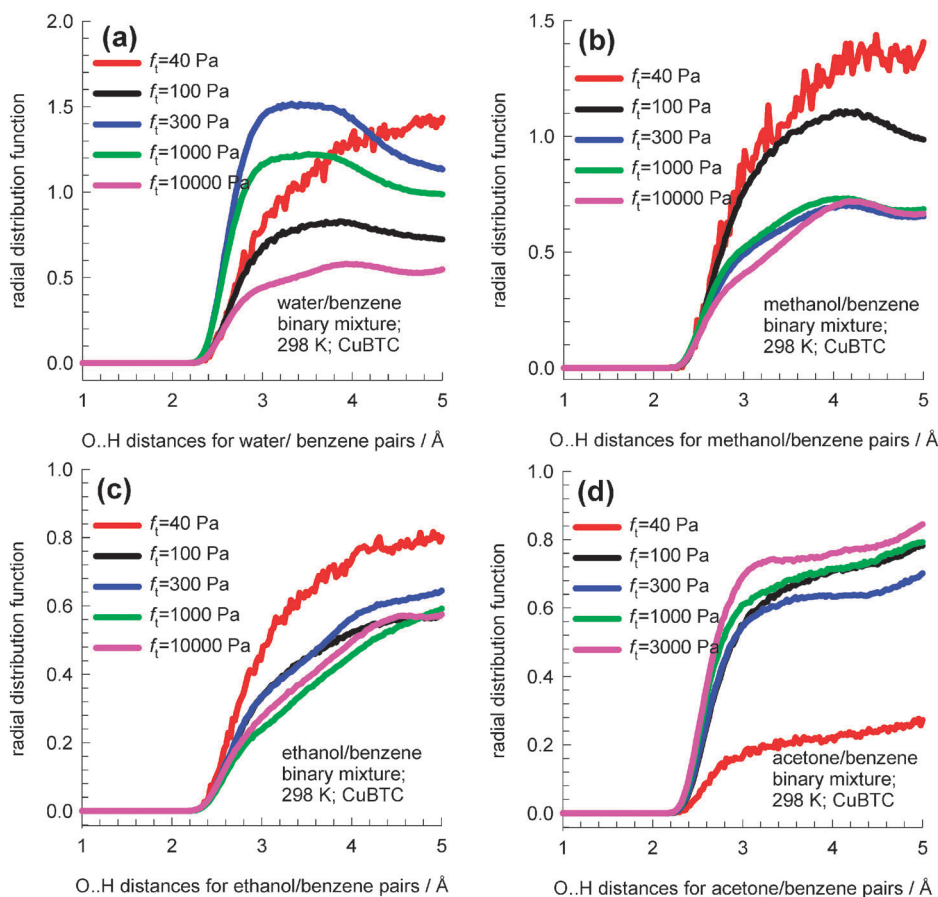


Fig. 7 Comparing the RDFs for $H_{\text{benzene}}-O_{\text{molecule}}$ distances for (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) acetone/benzene mixtures in CuBTC at 298 K and five different total fluid fugacity values.

species. This has the effect of reducing the effectiveness of adsorptive separations.

Clustering effects, resulting from H-bonding, are not catered for by IAST calculations.

5. Activity coefficients in the adsorbed phase, and modelling thereof

Using the Gibbs adsorption equation as starting point, we determined the activity coefficients in the adsorbed phase for the four binary mixtures; a detailed step-by-step calculation methodology is provided in the ESI,[†] and the results are presented in Fig. 8. The small departures from unity at low pressures is a consequence of the numerical fitting procedure employed in the calculations of the activity coefficients; the fundamentally correct limiting value of the activity coefficient

$\gamma_i \rightarrow 1$; $f_t \rightarrow 0$ cannot be prescribed in the adopted methodology. For values of the total bulk fluid phase fugacity $f_t = f_1 + f_2$ lower than about 100 Pa, the activity coefficients are practically unity. Non-ideality effects come into play as the pores become increasingly occupied. For all mixtures, the activity coefficient of benzene with the lower saturation capacity, γ_2 , reduces significantly below unity, by about 1–3 orders of magnitude, as pore saturation is approached. Concomitantly, the activity coefficient of the partner molecular with the higher saturation capacity, γ_1 , increases to values slightly exceeding unity. The characteristics of the activity coefficients observed in Fig. 8 are also found for water/alcohol mixtures in CuBTC,¹³ and in the zeolites FAU, DDR, MFI, and CHA; see Fig. S34–S47 of the ESI.[†]

In implementing the Real Adsorbed Solution Theory (RAST) including non-ideality effects,¹³ we adopted the Wilson model for the excess Gibbs free energy (see ESI,[†] for detailed derivations and analysis)

$$\ln(\gamma_1) = \left(1 - \ln(x_1 + x_2 A_{12}) - \frac{x_1}{x_1 + x_2 A_{12}} - \frac{x_2 A_{21}}{x_2 + x_1 A_{21}} \right) \left(1 - \exp\left(-C \frac{\pi A}{RT}\right) \right)$$

$$\ln(\gamma_2) = \left(1 - \ln(x_2 + x_1 A_{21}) - \frac{x_2}{x_2 + x_1 A_{21}} - \frac{x_1 A_{12}}{x_1 + x_2 A_{12}} \right) \left(1 - \exp\left(-C \frac{\pi A}{RT}\right) \right)$$
(1)

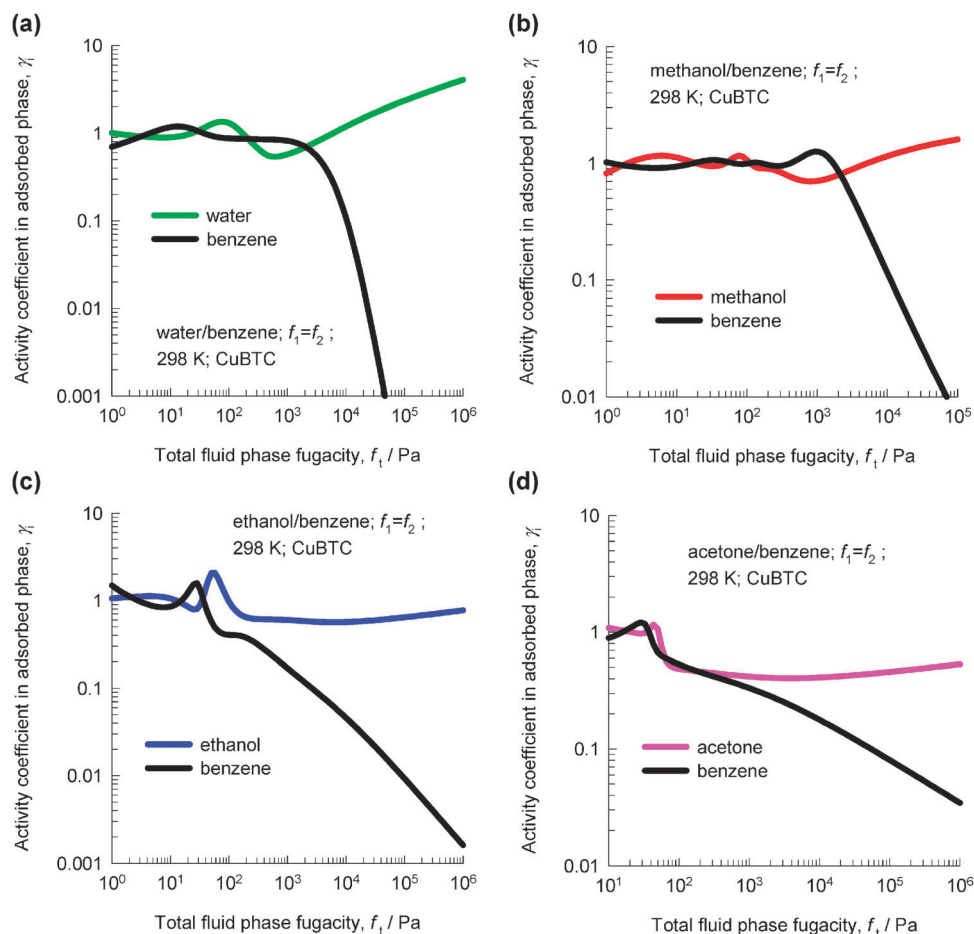


Fig. 8 Activity coefficients of the components in the adsorbed phase for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) methanol/ethanol, and (e) acetone/benzene mixtures in CuBTC at 298 K.

In eqn (1), π is the spreading pressure, A is the surface area per kg of framework, and $\pi A/RT$ is the adsorption potential.³⁸ As illustration, we present comparisons of RAST calculations

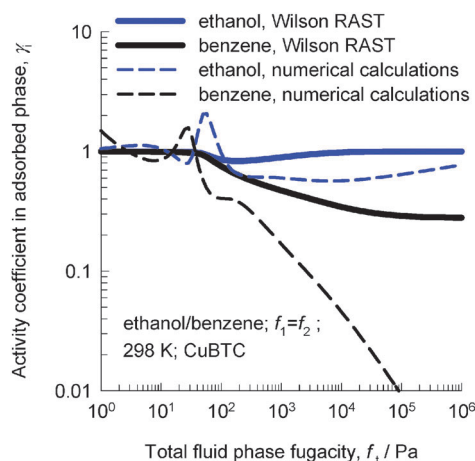


Fig. 9 RAST calculations of the activity coefficients for equimolar ethanol/benzene mixtures in CuBTC at 298 K. These calculations are based on the eqn (1) taking $A_{12} = 1$; $A_{21} = 3.6$; $C = 0.12 \text{ kg mol}^{-1}$. Further calculation details are provided in the ESI.†

following eqn (1) for ethanol/benzene mixtures with the values determined numerically from CBMC mixture simulations; see Fig. 9. While the correct qualitative trends in γ_i are captured by the Wilson model, a good quantitative fit was not achievable, irrespective of the choice of the three adjustable parameters A_{12} , A_{21} , and C . Similarly, the RAST model for water/benzene, methanol/benzene, and acetone/benzene mixtures did not offer any significant advantage over the IAST. There appears to be a need for development of models to describe mixture adsorption taking explicit account of molecular clustering effects.

6. Molecular clustering, and loading dependence of unary diffusivities

The separation performance is also influenced by intra-crystalline diffusivities, and how these depend on the occupancies. A molecule can jump from one adsorption site to an adjacent one, provided it is not already occupied. In the simplest scenario, we would expect the unary diffusivities to be proportional to the fractional vacancy.³⁹ As argued in a foregoing section, $1/\Gamma_i$ provides a quantification of the fractional vacancy when molecular clustering occurs. Consequently, the loading

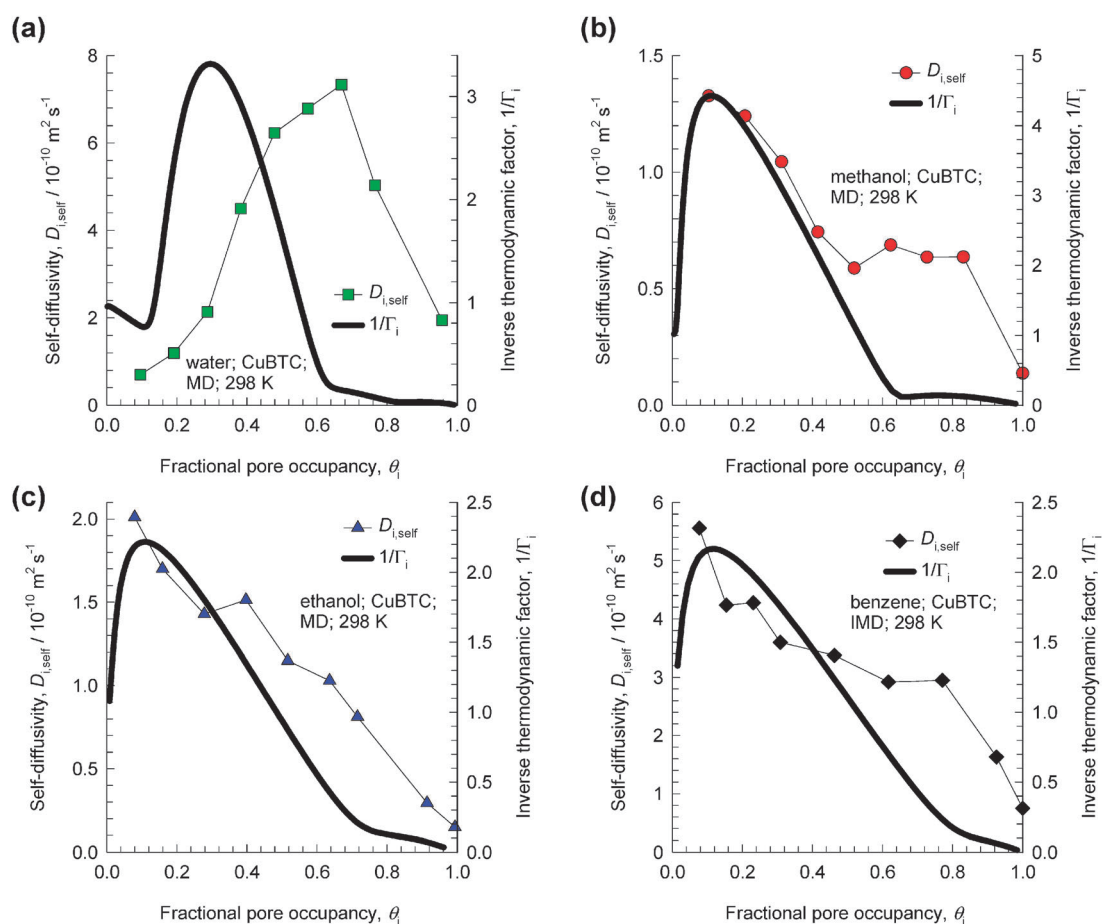


Fig. 10 MD simulations of the self-diffusivities $D_{i,\text{self}}$ and the inverse thermodynamic factor $1/\Gamma_i$ in CuBTC of (a) water, (b) methanol, (c) ethanol, and (d) benzene as a function of the fractional pore occupancy, θ_i .

dependence of the unary diffusivities are strongly influenced by the loading dependence of $1/\Gamma_i$; this influence has been highlighted in the literature for a wide variety of guest/host combinations.^{30,39–41}

MD simulations were carried to determine the self-diffusivities $D_{i,\text{self}}$, of water, methanol, ethanol, and benzene. Fig. 10, panels a, b, c, and d, presents plots comparing $D_{i,\text{self}}$ and $1/\Gamma_i$ vs. θ_i for each of the guest molecules. Even though there is no precise one-to-one correspondence between the two data sets, there is reasonable qualitative agreement between the two occupancy dependencies.

The tetrahedral pockets of CuBTC can accommodate about 9 molecules of water, and this explains the low water diffusivity values for occupancies below about 0.2. Compared at the same fractional pore occupancy, it is interesting to note that the diffusivities of benzene are higher than those for either methanol or ethanol. The most likely reason for this is that molecular clustering effects are practically non-existent for benzene molecules; this has been established earlier on the basis of RDFs.

Methanol, and ethanol, on the other hand experience strong clustering, and this explains the lower diffusivity values as compared to benzene. The molecular clustering effects for methanol are stronger than for ethanol; for this reason, the methanol diffusivities are slightly lower than that of ethanol, when compared at the same value of pore occupancy. Video animations for diffusion of water, methanol, ethanol, and benzene in CuBTC have been provided as ESI;† these provide evidence of molecular clustering, albeit qualitatively.

A further point to note is that the $D_{i,\text{self}}$ vs. θ_i data for methanol displays a distinct step-wise characteristic; the diffusivity values in the range $0.6 < \theta_i < 0.8$ are practically the same. Experimental data of Tsotsalas *et al.*³³ for transient desorption profiles for methanol in CuBTC at 298 K displays step-wise characteristics; see Fig. 11a. The explanation for the step-wise desorption is clearly to be found in the corresponding occupancy dependence of the diffusivities. This conclusion is re-enforced in Fig. 11b that presents a comparison of the experimental transient methanol desorption profile with the occupancy dependence of the self-diffusivity of methanol.

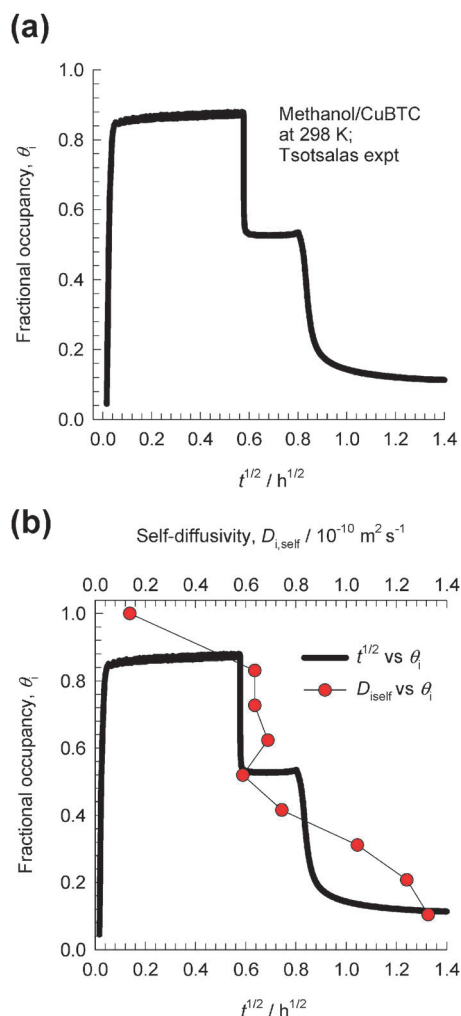


Fig. 11 (a) Transient desorption profiles for methanol in CuBTC at 298 K. Experimental data of Tsotsalas *et al.*³³ (b) Comparison of the experimental transient desorption profile with the loading dependence of the self-diffusivity.

7. Conclusions

The following major conclusions emerge from our investigations.

(1) CBMC simulations establish the potential of CuBTC for separation of water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures. For separations that operate under pore saturation conditions, the selectivity is in favor of the partner molecules because of molecular packing effects that disfavors benzene. CuBTC is well suited for drying water/alcohol/benzene mixtures.

(2) IAST calculations anticipate the right hierarchy of component loadings at pore saturation but the quantitative agreement with CBMC mixture simulations is poor in all cases. At pore saturation, the selectivities predicted by IAST are about an order of magnitude higher than those determined from CBMC simulations.

(3) The RDFs demonstrate the manifestation of hydrogen bonding between water–water, methanol–methanol, and ethanol–ethanol molecule pairs. There is however no detectable hydrogen bonding between benzene and partner molecules in the investigated mixtures.

(4) Molecular clustering induced by hydrogen bonding effects result in values of activity coefficients that deviate significantly from unity. Calculations of the activity coefficients show that the activity coefficient of benzene in water/benzene, methanol/benzene, ethanol/benzene, and acetone/benzene mixtures is lowered below unity by about 1–3 orders of magnitude at pore saturation. Such drastic reduction in the activity coefficients cannot be adequately modelled using say the Wilson equations that do not explicitly account for molecular clustering effects; there is a need for the development of improved models for activity coefficients in this respect.

(5) The occurrence of molecular clustering, and consequent failure of the IAST to provide quantitative predictions of mixture

adsorption equilibrium serve as a cautionary note to researchers who rely on IAST calculations for evaluation of separations with MOFs and ZIFs.

(6) Molecular clustering also influence the loading dependence of the diffusivities of guest molecules. The MD simulated data for methanol diffusivities serve to rationalize the transient step-wise desorption characteristics that have been observed in experiments of Tsotsalas *et al.*³³

Notation

| | |
|---------------------|--|
| A | Surface area per kg of framework, $\text{m}^2 \text{kg}^{-1}$ |
| C | Constant used in equation, kg mol^{-1} |
| $D_{i,\text{self}}$ | Self-diffusivity of species i , $\text{m}^2 \text{s}^{-1}$ |
| f_i | Partial fugacity of species i , Pa |
| f_t | Total fugacity of bulk fluid mixture, Pa |
| q_i | Component molar loading of species i , mol kg^{-1} |
| $q_{i,\text{sat}}$ | Molar loading of species i at saturation, mol kg^{-1} |
| R | Gas constant, $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ |
| T | Absolute temperature, K |

Greek letters

| | |
|------------|--|
| γ_i | Activity coefficient of component i in adsorbed phase, dimensionless |
| Γ_i | Thermodynamic factor, dimensionless |
| π | Spreading pressure, N m^{-1} |
| A_{ij} | Wilson parameters, dimensionless |
| θ_i | Fractional pore occupancy, dimensionless |

Subscripts

| | |
|-----|----------------------------|
| i | Referring to component i |
| t | Referring to total mixture |

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Electronic Supplementary Information (ESI) to accompany:

Separation of Benzene from Mixtures with Water,
Methanol, Ethanol, and Acetone: Highlighting
Hydrogen Bonding and Molecular Clustering Influences
in CuBTC

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1. Preamble

This ESI accompanying our manuscript *Separation of Benzene from Mixtures with Water, Methanol, Ethanol, and Acetone: Highlighting Hydrogen Bonding and Molecular Clustering Influences in CuBTC* provides (a) structural details of CuBTC, (b) Configurational-Bias Monte Carlo (CBMC) and Molecular Dynamics (MD) simulation methodologies with specification of force fields, (c) snapshots showing the location of adsorbed molecules within CuBTC framework, (d) 2-site and 3-site Langmuir-Freundlich fit parameters for unary isotherms, (e) data on radial distribution functions (RDF) to confirm H-bonding effects, (f) details of the methodology used to calculate activity coefficients from CBMC mixture simulations, and (g) details of IAST and RAST calculation procedures.

For ease of reading, this ESI is written as a stand-alone document. As a consequence, there is some overlap of material with the main manuscript. Researchers who are interested in specific sections can use the Table of Contents to skip to that specific section, without the need to wade through the entire material that is presented here.

2. CBMC simulation methodology

The CuBTC ($= \text{Cu}_3(\text{BTC})_2$ with BTC = 1,3,5-benzenetricarboxylate, also known as HKUST-1) framework is composed of copper atoms connected by benzene-1,3,5-tricarboxylate (BTC) linkers, which form a characteristic paddle-wheel structure: two copper atoms bonded to the oxygen atoms of four BTC linkers, generating four-connected square-planar vertexes; see Figure 1. The framework contains two types of large cavities (9 Å diameter) and small cavities (of 5 Å diameter). The larger cavities (L_2 and L_3) are similar in size and shape but as a result of the paddle-wheel, the copper atoms are only accessible from the L_3 cages. L_2 and L_3 cavities are connected through triangular-shaped windows. The small cavities (T_1) are tetrahedral pockets enclosed by the benzene rings; these are connected to L_3 cages by small triangular windows (3.5 Å in size), as shown in Figure 2.

Benzene is modeled using the full atom rigid model proposed by Rai and Siepmann.¹ In this model carbon and hydrogen atoms are considered as single Lennard-Jones interaction centers with partial charges.

Water is modeled using TIP5P-E² which has proven to be the most suitable model for water in Cu-BTC.³ Furthermore, recently, Peng *et al.*⁴ have found that at least a four sites model is needed to reproduce the right orientation of the water molecules in metal organic frameworks containing open metal sites.

Methanol, ethanol, and acetone molecules are modeled using TraPPE.^{5,6}

The Cu-BTC framework is modeled as a rigid structure based on the crystal structure of Chui *et al.*⁷ with the atoms fixed in their crystallographic position. We removed the axial oxygen atoms weakly bonded to the copper atoms that correspond to water ligands. Lennard Jones parameters for the atoms were taken from DREIDING⁸ force field except these for copper atoms that were taken from UFF⁹ force field; see Table 1. Additionally partial charges from Castillo *et al.*³ were added to the model. The unit cell of our model is a cubic cell of $a = b = c = 26.34 \text{ \AA}$. The computed helium void fraction is of 0.76, the pore volume $0.85 \text{ cm}^3/\text{g}$ and the surface area $2100 \text{ m}^2/\text{g}$. The framework density, $\rho = 879 \text{ kg m}^{-3}$.

Monte Carlo (MC) simulations were performed in the Grand Canonical (GC) Ensemble and Configurational Bias Monte Carlo (CBMC) technique was used for the insertion and deletion of molecules in and from the system. We used Lennard-Jones and electrostatic cutoffs of 12.0 \AA . Coulombic interactions were computed using the Ewald summation technique with a relative precision of 10^{-6} and using the same cut-off.

All guest molecules, with the exception of benzene, are able to access the tetrahedral cages. In practice the tetrahedral cages are inaccessible to benzene molecules because the narrow 3.5 \AA windows do not allow entry of benzene molecules that have a kinetic diameter of 5.85 \AA . To prevent the insertion of benzene molecules into the tetrahedral cages, we need to block such non-permissible MC moves. Toward this end, spherical blocks are placed in the center of these cavities. Hard spheres do not interact

with water, acetone, and alcohols molecules in such a way that the spherical blocks do not affect the adsorption of these guest molecules.

Simulations were performed using the RASPA code developed by D. Dubbeldam, S. Calero, D. E. Ellis, and R.Q. Snurr. The code and most of the force fields and models used in this work have been extensively tested and validated with a large number of experimental and simulation data.¹⁰⁻¹²

3. Vapor and liquid phase transitions

It is essential to gain an understanding of vapor/liquid phase transitions for water, alcohols, and benzene. Figure 3a presents calculations of the molar densities of water, methanol, ethanol, and benzene as a function of the bulk fluid phase fugacity using the Peng-Robinson equation of state. For fugacities below about 100 kPa, each of the components is in the gaseous phase. For fugacities in excess of 2 MPa, each of the substances water, methanol, ethanol, and benzene is predominantly in the liquid state with molar densities in the range of 20 – 55 mol L⁻¹. For fugacities in the range of 700 kPa to 2 MPa, both vapor and liquid phases co-exist. A similar scenario holds for equimolar ethanol/benzene mixtures; see Figure 3b.

The important message we wish to draw from the calculations in Figure 3 is that care needs to be taken when interpreting unary isotherms of water, alcohols, and benzene to be presented later. In our molecular simulations, we consistently use fugacities rather than “pressures” when plotting unary adsorption isotherms. This is vital because the bulk fluid phase could be either in the vapor phase, in the liquid phase, or a mixture of vapor and liquid phases.

4. Unary isotherms in CuBTC

Let us first consider the adsorption isotherms for water, plotted as a function of the fluid phase fugacity ranging to 10 MPa; see Figure 4.

The pure component isotherm data for water show marked inflections. The reason for these inflections can be traced to the location of water molecules within the tetrahedral pockets, and within the larger

cages. In order to correctly capture these inflections the unary isotherm data of water were fitted with the 3-site Langmuir-Freundlich model:

$$q^0 = q_{A,sat} \frac{b_A f^{v_A}}{1 + b_A f^{v_A}} + q_{B,sat} \frac{b_B f^{v_B}}{1 + b_B f^{v_B}} + q_{C,sat} \frac{b_C f^{v_C}}{1 + b_C f^{v_C}} \quad (1)$$

The saturation capacities q_{sat} , Langmuir constants b , and the Freundlich exponents v , are provided in Table 3. The superscript 0 emphasizes that the loadings are for pure component water.

Figure 4 presents a comparison of the CBMC simulations for water adsorption in CuBTC with 3-site Langmuir-Freundlich model. Also shown are the experimental isotherm data of Zhao et al.,¹³ Yazaydin et al.,¹⁴ and Küsgens et al.¹⁵ measured at 298 K. Our CBMC simulations are in reasonable agreement with the experimental data; in particular, the steep portion of the isotherm is correctly reproduced. This corresponds to the filling up of the larger cages of CuBTC.

The unary isotherms for methanol, ethanol, acetone, and benzene were fitted with good accuracy with the dual-Langmuir-Freundlich model

$$q^0 = q_{A,sat} \frac{b_A f^{v_A}}{1 + b_A f^{v_A}} + q_{B,sat} \frac{b_B f^{v_B}}{1 + b_B f^{v_B}} \quad (2)$$

with the fits parameters as specified in Table 4.

Figure 5 provides a comparison of the CBMC simulated isotherms for water, methanol, ethanol, acetone, and benzene with 3-site, and 2-site Langmuir-Freundlich fits. The accuracy of the fits is excellent for all five guest molecules. Particularly noteworthy are the differences in the saturation capacities, $q_{sat} = q_{A,sat} + q_{B,sat} + q_{C,sat}$, of the various guest molecules: water = 54 mol kg⁻¹; methanol = 19.9 mol kg⁻¹; ethanol = 13 mol kg⁻¹; acetone = 9.9 mol kg⁻¹; benzene = 6.7 mol kg⁻¹.

For comparison purposes, the corresponding saturation capacities in TetZB are: water = 21 mol kg⁻¹; methanol = 10.6 mol kg⁻¹; ethanol = 6.8 mol kg⁻¹; acetone = 5.6 mol kg⁻¹; benzene = 3.3 mol kg⁻¹. The point we wish to stress here is that CuBTC has higher saturation capacities, a desirable feature for use in fixed-bed adsorber separations.

Let us define the fractional occupancy within the pores, θ_i , for each of the five guest molecules

$$\theta_i = \frac{q^0}{q_{sat}} \quad (3)$$

where q^0 is the molar loading of species i that is determined from the multi-site Langmuir-Freundlich fits. The variation of the pore occupancies with bulk fluid phase fugacity, f_i , are shown in Figure 6. We note that the pore occupancies are close to unity for operation at ambient conditions of 100 kPa and 298 K.

Most commonly, industrial separations are anticipated to operate with bulk liquid mixtures; this ensures that pore saturation conditions are reached.¹⁶ This is an important aspect of this work, because the separations are dictated by molecular packing effects that manifest at pore saturation conditions.

An important feature of the unary isotherms for water, methanol, ethanol, acetone, and benzene is the steep increase in the loadings; this suggests the formation of molecular clustering as a consequence of hydrogen bonding effects.¹⁷⁻¹⁹ In order to explore cluster formation in more detail, we determine the inverse thermodynamic factor, $1/\Gamma_i$, defined by

$$\frac{1}{\Gamma_i} \equiv \frac{\partial \ln q_i}{\partial \ln f_i} = \frac{f_i}{q_i} \frac{\partial q_i}{\partial f_i} \quad (4)$$

by analytic differentiation of eq. (1). The data for $1/\Gamma_i$ are presented in Figure 7. We prefer to plot $1/\Gamma_i$ instead of Γ_i because the latter has the undesirable property of approaching infinity as saturation loading is approached; this makes the data less easy to interpret when plotted in graphical form. For a single-site Langmuir isotherm, we have $1/\Gamma_i = (1 - \theta_i) = (1 - q_i/q_{i,sat})$, i.e. the fractional vacancy. In previous work we had argued that the condition $1/\Gamma_i > 1$ implies the increase of fractional vacancy beyond unity and this is physically rationalized if we allow for molecular clustering¹⁷⁻²¹ We note from Figure 7 that $1/\Gamma_i$ exceeds unity for a certain range of pore occupancies below about 0.5.

Experimental confirmation of clustering effects is provided by the experimental data of Tsotsalas et al.²² Figure 8 compares the $1/\Gamma_i$ values obtained by Tsotsalas et al.²² for methanol by numerical piecewise differentiation of their experimental isotherms, with the values obtained from dual-Langmuir-Freundlich fits of CBMC simulated isotherms. There is reasonably good qualitative agreement with the two sets of data.

5. CBMC simulations of mixture adsorption

Figure 9, panels a, b, c, d, and e, present the results for CBMC simulations of the component loadings for adsorption of equimolar water/benzene, methanol/benzene, ethanol/benzene, methanol/ethanol, and acetone/benzene mixtures in CuBTC at 298 K. The data for methanol/ethanol mixtures that is presented here is the same as that reported in our earlier work;²³ it is included here for comparison purposes. Figure 9f presents the calculations of the corresponding adsorption selectivities for the five equimolar binary mixtures in CuBTC. In all cases, we note a reversal in the hierarchy of component loadings as conditions approach pore saturation. In all cases, we note that at conditions close to pore saturation, the adsorption is in favor of the component with the higher saturation capacity. For water/benzene mixtures, the selectivity is in favor of water at fugacities $f_i > 10$ kPa. For methanol/benzene and ethanol/benzene mixtures, the selectivity is in favor of the alcohol as pore saturation conditions are approached. For methanol/ethanol mixtures, the adsorption is in favor of the shorter alcohol as pore saturation is approached. For acetone/benzene mixtures, the selectivity is in favor of acetone as pore saturation conditions are approached.

For mixture adsorption, let us define the fractional occupancy within the pores, θ

$$\theta_t = \sum_{i=1}^n \frac{q_i}{q_{i,sat}} \quad (5)$$

where q_i is the molar loading of species i in the mixture, and $q_{i,sat}$ is its saturation capacity. Figure 10 shows the fractional pore occupancy θ for adsorption of equimolar water/benzene, methanol/benzene, ethanol/benzene, acetone/benzene, and methanol/ethanol mixtures as a function of the bulk fluid phase

fugacity, f_t . We note that the pores are nearly saturated when the bulk fluid phase fugacity exceeds about 10 kPa.

From the data in Figure 9 we conclude that CuBTC has the potential of separating binary mixtures of benzene with water, methanol, ethanol, and acetone. For operation at pore saturation the selectivity is in favor of the smaller partner molecule in the mixture. Figure 11 presents the CBMC simulations for equimolar quaternary water/methanol/ethanol/benzene mixtures in CuBTC at 298 K. These results clearly indicate that water can be selectively adsorbed from a mixture containing alcohols, and benzene provided the operation is close to pore saturation conditions. Operation at 298 K, and $f_t > 10$ kPa ensures pore saturation.

Figure 12, 13, 14, 15, and 16 present snapshots showing the average occupation profiles of constituents in, respectively, water/benzene, methanol/benzene, ethanol/benzene, acetone/benzene, and water/methanol/ethanol/benzene mixtures in CuBTC at 298 K. The large cages become increasingly populated with increasing total fugacity.

6. Unary vs Mixture Adsorption: Entropy effects, H-bonding effects

To get a feel for molecular packing effects, also called entropy effects, we can compare the loadings of pure components with the loadings in mixtures at the same partial fugacity in the bulk fluid phase. Figure 17a compares CBMC simulations of adsorption of pure water with CBMC simulations of adsorption of mixtures containing water; we have included also the CBMC mixture simulations that were reported in our previous work.²³ For all aqueous mixtures, entropy effects favor water for partial fugacities exceeding 1 kPa. Figure 17b presents the same set of data plotted in Figure 17a in a different manner; herein we divide the loadings of water in the mixture by the loadings of pure water, both compared at the same partial fugacity in the bulk fluid phase. The “enhancement” factor of water reaches a value of 8; see the shaded region. The most likely reason for this enhancement is hydrogen bonding between water and partner molecules; the partner molecules “drag” water into CuBTC. Hydrogen bonding between water and benzene is negligible, and therefore there is no enhancement of water ingress..

Figure 18 compares CBMC simulations of adsorption of pure methanol with CBMC simulations of adsorption of mixtures containing methanol. For water/methanol mixtures, entropy effects favor water in this range of partial fugacities indicated by the arrow. For other mixtures, entropy effects favor methanol.

Figure 19 compares CBMC simulations of adsorption of pure ethanol with CBMC simulations of adsorption of mixtures containing ethanol. For ethanol/benzene mixtures, entropy effects favor ethanol in this range of partial fugacities indicated by the arrow. For other mixtures, entropy effects cause the ethanol loading in the mixture to reduce in favor of partner molecules.

Figure 20 compares CBMC simulations of adsorption of pure 1-propanol with CBMC simulations of adsorption of mixtures containing 1-propanol. For the range of partial fugacities indicated by the arrow, entropy effects disfavor 1-propanol adsorption in mixtures. This is due to the lower saturation capacity of 1-propanol compared to partner molecules.

Figure 21 compares CBMC simulations of adsorption of pure benzene with CBMC simulations of adsorption of mixtures containing benzene. For the range of partial fugacities indicated by the arrow, entropy effects disfavor benzene adsorption in mixtures. This is due to the lower saturation capacity of benzene compared to partner molecules.

Let us now investigate whether IAST calculations are able to model entropy effects.

7. Summary of IAST calculation methodology

Briefly, the basic equation of Ideal Adsorbed Solution Theory (IAST) theory of Myers and Prausnitz²⁴ is the analogue of Raoult's law for vapor-liquid equilibrium, i.e.

$$f_i = P_i^0 x_i; \quad i = 1, 2, \dots, n \quad (6)$$

where x_i is the mole fraction in the adsorbed phase

$$x_i = \frac{q_i}{q_1 + q_2 + \dots + q_n} \quad (7)$$

and P_i^0 is the pressure for sorption of every component i , which yields the same spreading pressure, π for each of the pure components, as that for the mixture:

$$\frac{\pi A}{RT} = \int_0^{P_1^0} \frac{q_1^0(f)}{f} df = \int_0^{P_2^0} \frac{q_2^0(f)}{f} df = \int_0^{P_3^0} \frac{q_3^0(f)}{f} df = \dots \quad (8)$$

where R is the gas constant ($= 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$), and $q_i^0(f)$ is the *pure* component adsorption isotherm given by Equations (1) or Equation (2). The molar loadings $q_i^0(f)$ are expressed in the units of moles adsorbed per kg of framework, i.e. mol kg^{-1} . The units of the spreading pressure π is the same as that for surface tension, i.e. N m^{-1} ; indeed the spreading pressure is the negative of the surface tension.²⁴ The quantity A on the left side of Equation (8) is the surface area per kg of framework, with units of $\text{m}^2 \text{ kg}^{-1}$. The units of $\frac{\pi A}{RT}$, also called the adsorption potential,²⁵ are mol kg^{-1} .

Each of the integrals in Equation (8) can be evaluated analytically. For the 3-site Langmuir-Freundlich isotherm, the integration yields

$$\int_{f=0}^P \frac{q^0(f)}{f} df = \frac{q_{A,sat}}{v_A} \ln(1 + b_A P^{v_A}) + \frac{q_{B,sat}}{v_B} \ln(1 + b_B P^{v_B}) + \frac{q_{C,sat}}{v_C} \ln(1 + b_C P^{v_C}) \quad (9)$$

The right hand side of equation (9) is a function of P . For multicomponent mixture adsorption, each of the equalities on the right hand side of Equation (8) must be satisfied. These constraints may be solved using a suitable root-finder, to yield the set of values of $P_1^0, P_2^0, P_3^0, \dots, P_n^0$, all of which satisfy Equation (8). The corresponding values of the integrals using these as upper limits of integration must yield the same value of $\frac{\pi A}{RT}$ for each component; this ensures that the obtained solution is the correct one.

The adsorbed phase mole fractions x_i are then determined from

$$x_i = \frac{f_i}{P_i^0}; \quad i = 1, 2, \dots, n \quad (10)$$

The total amount adsorbed is calculated from

$$q_i \equiv q_1 + q_2 \dots + q_n = \frac{1}{\frac{x_1}{q_1^0(P_1^0)} + \frac{x_2}{q_2^0(P_2^0)} + \dots + \frac{x_n}{q_n^0(P_n^0)}} \quad (11)$$

The set of equations (1), (2), (6), (7), (8) (9), and (11) need to be solved numerically to obtain the loadings, q_i of the individual components in the mixture.

8. Mixture adsorption equilibrium: CBMC vs IAST

Figures 22 and 23 compare the IAST calculations with CBMC simulations of component loadings of equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, (d) methanol/ethanol, (e) acetone/benzene, and (f) water/methanol/ethanol/benzene mixtures in CuBTC at 298 K.

The same data is plotted in Figures 22 and 23, using linear y -axes, and logarithmic y -axes, respectively. In all cases, the IAST correctly anticipates that the adsorption is favorable to the component with the higher saturation capacity as saturation conditions are approached. However, the quantitative agreement between the CBMC mixtures simulations and IAST is not of sufficient accuracy near saturation conditions. For water/benzene, methanol/benzene, ethanol/benzene, acetone/benzene, and water/methanol/ethanol/benzene mixtures, the agreement between the IAST and CBMC simulations is good in the Henry regime at total fluid phase fugacities below about 10 Pa. For methanol/ethanol mixtures, the agreement between the IAST and CBMC simulations is excellent for $f_t < 1$ kPa. For f_t higher than the values indicated in the foregoing, there are significant quantitative departures between CBMC simulations and IAST predictions. The reasons for the deviations are most likely attributed to the influence of molecular clustering engendered by hydrogen bonding effects, as explained in detail in our earlier work.¹⁷

The separation performance anticipated by IAST calculations is overly optimistic; this is demonstrated by the comparisons presented in Figure 24 for adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and methanol/ethanol, and acetone/benzene mixtures in CuBTC at 298 K determined from (a) CBMC mixture simulations, and (b) IAST

calculations. Typically, at pore saturation, the selectivities estimated by IAST are about an order of magnitude higher than those determined from CBMC mixture simulations.

A different way to highlight the inadequacies of IAST, is to compare the data on the enhancement of water ingress in mixtures, as presented in Figure 17b, with the corresponding IAST calculations. Figure 25 presents such comparisons for (a) water/methanol, (b) water/ethanol, (c) water/1-propanol, (d) water/benzene, (e) water/methanol/ethanol/1-propanol, and (f) water/methanol/ethanol/benzene mixtures. In all six mixtures, the CBMC simulations show larger enhancement of water ingress in CuBTC than predicted by IAST calculations. This enhancement of water ingress for mixture adsorption is most likely attributable to H-bonding, as we shall demonstrate in the section below.

Figure 26 presents calculations of the adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and methanol/ethanol, and acetone/benzene mixtures in TetZB at 298 K determined from IAST calculations using the pure component isotherm data fit parameters presented in Table 5. For all these mixtures, the component with the higher saturation capacity is preferentially adsorbed from the mixture.

For a total fluid phase fugacity $f_t = 100$ kPa, the adsorption selectivities with CuBTC are comparable to the corresponding IAST-calculated selectivities obtained with TetZB, as presented in Figure 26. It must be remarked here that the IAST estimates for TetZB are most likely to be optimistic with regard to the magnitudes of the selectivities.

9. Radial distribution functions, and evidence of H-bonding effects

We now demonstrate the manifestation of molecular clustering effects induced by hydrogen bonding. For this purpose, we determined the radial distribution functions (RDFs) for distances between all combinations of O and H atoms of molecule pairs. Figure 27, panels a, b, c, and d, presents a comparison of the RDFs for $H_{\text{benzene-O}_{\text{molecule}}}$ and $H_{\text{molecule-O}_{\text{molecule}}}$ distances for water/benzene, methanol/benzene, ethanol/benzene, and water/methanol/ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa. We note that the RDFs for $H_{\text{water-O}_{\text{water}}}$, $H_{\text{methanol-O}_{\text{methanol}}}$, and $H_{\text{ethanol-O}_{\text{ethanol}}}$ pairs each exhibit a first peak at an intermolecular distance of 2 Å, that is characteristic

of hydrogen bonding.^{17, 26} The results presented in Figure 27d show that H-bonding between alcohol/alcohol pairs are stronger than the bonding between water/water pairs.

Remarkably, the corresponding values for $H_{\text{benzene-O}_{\text{water}}}$, $H_{\text{benzene-O}_{\text{methanol}}}$, and $H_{\text{benzene-O}_{\text{ethanol}}}$ do not display any peaks in the RDFs. This would indicate that guest molecules do not form clusters with benzene molecules, and clustering effects are restricted to water/water, methanol/methanol, and ethanol/ethanol pairs. In order to further verify this finding we determined the RDFs for $H_{\text{benzene-O}_{\text{molecule}}}$ distances for (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) acetone/benzene mixtures in CuBTC at 298 K and five different total fluid fugacity values; see Figure 28. For the wide range of fugacities, $f_t = 40 \text{ Pa} - 10000 \text{ Pa}$, no peaks are observed at any molecule-benzene distance, confirming that the benzene does not form clusters with partner molecules.

Figure 29 presents the data of Krishna and van Baten¹⁷ for RDF of $H_{\text{water-O}_{\text{water}}}$, $H_{\text{methanol-O}_{\text{methanol}}}$, and $H_{\text{ethanol-O}_{\text{ethanol}}}$ distances for (a) water, (b) methanol, and (c) ethanol at 300 K in ZIF-8, LTA, FAU, DDR, and MFI. These data indicate that cluster formation due to hydrogen bonding occurs in other host materials.

10. Calculation of activity coefficients using CBMC mixture simulations

It is clear from the results presented in Figures 22, 23, 24, and 25 that the assumption of an *ideal* adsorbed phase breaks down as saturation conditions are approached. Let us quantify these deviations by introducing activity coefficients following Myers and Prausnitz.²⁴

To account for non-ideality effects in mixture adsorption, we introduce activity coefficients γ_i into Equation (6).

$$f_i = P_i^0 x_i \gamma_i \quad (12)$$

The CBMC mixture simulations provide information on the mole fractions of the adsorbed phase, x_i , but the activity coefficients γ_i are not known *a priori*.

We discuss a procedure by which the activity coefficients γ_i can be determined using as data inputs, the CBMC simulated component loadings in the mixture as a function of the partial fugacities, f_i , in the

bulk fluid phase. We illustrate this procedure for binary ethanol/benzene mixture. This procedure is exactly the same as the one that we had used in our earlier work.²³

Using the Gibbs adsorption equation for mixture adsorption as starting point (cf. Equations (3.52) of Ruthven²⁷), we can write the differential of the spreading pressure as

$$\frac{Ad\pi}{RT} = q_1 d \ln f_1 + q_2 d \ln f_2 \quad (13)$$

Integrating equation (13) from 0 to f_1 , and f_2

$$\frac{\pi A}{RT} = \int_0^{f_1, f_2} (q_1 d \ln f_1 + q_2 d \ln f_2) = \int_0^{f_t} (q_1 + q_2) d \ln f_t \quad (14)$$

The integral in equation (14) can be determined using an appropriate quadrature formula. The approach we use here is to fit the loadings q_1 , for the component 1 with the higher saturation capacity, and the total mixture loading $q_t = q_1 + q_2$ as functions, respectively, of the partial fugacities, f_1 , and total mixture fugacity f_t .

The P_i^0 can be determined for each of the two components by setting the equalities:

$$\frac{\pi A}{RT} = \int_0^{f_t} (q_1 + q_2) d \ln f_t = \int_0^{P_1^0} \frac{q_1^0(f)}{f} df = \int_0^{P_2^0} \frac{q_2^0(f)}{f} df \quad (15)$$

Equation (15) can be solved to determine P_1^0 , and P_2^0 as a function of the total mixture fugacity f_t . Combining the obtained values of P_1^0 , and P_2^0 with Equation (12), we can determine the activity coefficients γ_i as a function of the total mixture fugacity, f_t . The adopted procedure is illustrated, step-by-step, for the CBMC ethanol/benzene mixture data reported in Figure 9c.

Step 1. We first fit the component ethanol loadings q_1 , and the total mixture loading $q_t = q_1 + q_2$ as functions, respectively, of the partial fugacities, f_1 , and total fugacity f_t using the Dual-Langmuir-Freundlich model. The fit parameters are specified in Table 6. To demonstrate the goodness of the fits,

Figure 30 compares the CBMC mixture simulation data with the fits for water loadings q_1 , and the total mixture loading $q_t = q_1 + q_2$ with fitted model. The fits are of excellent accuracy.

From these fits, we can determine the mole fraction of ethanol in the adsorbed phase, x_1 , from the DLF fits of CBMC data using the parameter values listed, for example, in Table 6:

$$x_1 = \frac{q_1}{q_t} \quad (16)$$

The mole fraction of benzene in the adsorbed phase, $x_2 = 1 - x_1$.

Step 2. We determine the value of $\frac{\pi A}{RT}$ by analytic integration of the first right member of Equation (15). The formula for analytic integration is as follows

$$\frac{\pi A}{RT} = \int_0^{f_t} (q_1 + q_2) d \ln f_t = \frac{q_{A,sat}}{V_A} \ln(1 + b_A f_t^{V_A}) + \frac{q_{B,sat}}{V_B} \ln(1 + b_B f_t^{V_B}) \quad (17)$$

In determining the right member of equation (17) we use the DLF fit parameters for the mixture loadings as specified in Table 6.

Step 3. We determine P_1^0 , and P_2^0 as a function of f_t by solving Equation (12) an appropriate root-finder routine.

Step 4. The activity coefficient of ethanol in the adsorbed phase is calculated from

$$\gamma_1 = \frac{f_1}{P_1^0 x_1} \quad (18)$$

The value of x_1 used in the calculations is from equation (16). The activity coefficient of benzene in the adsorbed phase is calculated from

$$\gamma_2 = \frac{f_2}{P_2^0 (1 - x_1)} \quad (19)$$

Figure 31 presents the activity coefficients γ_i for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, (d) methanol/ethanol, and (e) acetone/benzene mixtures in CuBTC at 298 K. For

values of the total bulk fluid phase fugacity $f_t = f_1 + f_2$ lower than about 100 Pa, the activity coefficients are practically unity. In other words, non-ideality effects come into play as the pores become increasingly occupied. For all mixtures, the activity coefficient of the component 2 with the lower saturation capacity, γ_2 , reduces significantly below unity as pore saturation is approached. Concomitantly, the activity coefficient of the component 1 with the higher saturation capacity, γ_1 , increases to values slightly exceeding unity.

The deviations of activity coefficients from unity values are most likely correlated with the hydrogen bonding effects.¹⁷

11. Modelling non-ideality effects for binary mixture adsorption

For quantifying non-ideality effects we need to model the excess Gibbs free energy

$$\frac{G^{excess}}{RT} = x_1 \ln(\gamma_1) + x_2 \ln(\gamma_2) \quad (20)$$

We extend the approaches of Talu and Myers^{28, 29} and Siperstein and Myers²⁵ by adopting the Wilson model for the activity coefficients, along with the correction factor $\left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right)$ where C is a constant to be determined from data fitting.

$$\frac{G^{excess}}{RT} = \left[-x_1 \ln(x_1 + x_2 \Lambda_{12}) - x_2 \ln(x_2 + x_1 \Lambda_{21})\right] \left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right) \quad (21)$$

The activity coefficients are given by

$$\begin{aligned} \ln(\gamma_1) &= \left(1 - \ln(x_1 + x_2 \Lambda_{12}) - \frac{x_1}{x_1 + x_2 \Lambda_{12}} - \frac{x_2 \Lambda_{21}}{x_2 + x_1 \Lambda_{21}}\right) \left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right) \\ \ln(\gamma_2) &= \left(1 - \ln(x_2 + x_1 \Lambda_{21}) - \frac{x_2}{x_2 + x_1 \Lambda_{21}} - \frac{x_1 \Lambda_{12}}{x_1 + x_2 \Lambda_{12}}\right) \left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right) \end{aligned} \quad (22)$$

The choice of $\Lambda_{12} = \Lambda_{21} = 1$ in Equation (22) yields unity values for the activity coefficients.

The introduction of $\left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right)$ imparts the correct limiting behaviors $\gamma_i \rightarrow 1$; $f_i \rightarrow 0$ for the activity coefficients in the Henry regime. As pore saturation conditions are approached, this correction factor tends to unity $\left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right) \rightarrow 1$. To illustrate this, we present calculations of the correction factor for ethanol/benzene mixtures; see Figure 32. These calculations are based on the calculations taking $\Lambda_{12} = 1$; $\Lambda_{21} = 3.6$; $C = 0.12 \text{ kg mol}^{-1}$; these values are reasonable representations of the CBMC mixture simulations for ethanol/benzene mixture.

The excess reciprocal loading for the mixture can be defined as

$$\frac{1}{q^{excess}} = \frac{1}{q_i} - \left(\frac{x_1}{q_1^0(P_1^0)} + \frac{x_2}{q_2^0(P_2^0)} \right) \quad (23)$$

The excess reciprocal loading for the mixture can be related to the partial derivative of the Gibbs free energy with respect to the adsorption potential at constant composition

$$\frac{1}{q^{excess}} = \frac{\partial \left(\frac{G^{excess}}{RT} \right)}{\partial \left(\frac{\pi A}{RT} \right)} \Bigg|_{T,x} = [-x_1 \ln(x_1 + x_2 \Lambda_{12}) - x_2 \ln(x_2 + x_1 \Lambda_{21})] C \exp\left(-C \frac{\pi A}{RT}\right) \quad (24)$$

For calculation of the total mixture loading we need to replace Equation (11) by

$$q_i \equiv q_1 + q_2 = \frac{1}{\frac{x_1}{q_1^0(P_1^0)} + \frac{x_2}{q_2^0(P_2^0)} + [-x_1 \ln(x_1 + x_2 \Lambda_{12}) - x_2 \ln(x_2 + x_1 \Lambda_{21})] C \exp\left(-C \frac{\pi A}{RT}\right)} \quad (25)$$

The parameters Λ_{12} , Λ_{21} , and C can be fitted to match the CBMC mixture simulations. Table 13 lists the parameter values for methanol/ethanol and ethanol/benzene mixtures obtained in this manner.

Figures 33a,b compare the RAST estimations with CBMC simulations of component loadings of the (a) ethanol/benzene, and (b) methanol/ethanol mixtures. We see that the RAST calculations offer only slight improvement over the corresponding IAST calculations. It is not possible to obtain good

agreement with CBMC mixture calculations for total fugacities significantly higher than 10 kPa. The corresponding RAST calculations of the activity coefficients are shown in Figures 33c,d. While the correct qualitative trends in γ_i are captured by the Wilson model, a good quantitative fit was not achievable, irrespective of the choice of the three parameters Λ_{12} , Λ_{21} , and C . Similarly, the RAST model for water/benzene, methanol/benzene, and acetone/benzene mixtures did not offer any significant advantage over the IAST. There appears to be a need for development of models to describe mixture adsorption taking explicit account of molecular clustering effects.

12. Non-ideality effects for mixture adsorption in FAU zeolite

Using published data on CBMC mixture simulations we shall examine the non-ideality effects for mixture adsorption in four different zeolites, FAU, DDR, MFI, and CHA.

Let us consider the adsorption of water/methanol, and water/ethanol mixtures in all-silica FAU zeolite that consists of 786 Å³ cages, that are separated by 7.3 Å size windows. Figure 34 shows CBMC simulations of Krishna and van Baten¹⁷ for pure component adsorption isotherms for water, methanol, and ethanol in all-silica FAU zeolite at 300 K. Above fluid phase fugacities of 10⁴ Pa, pore saturation is reached and the hierarchy of saturation capacities water >> methanol > ethanol is a reflection of the size of the molecules.

Figure 35a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/methanol mixtures in FAU zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of the alcohol. However, we note that at partial fluid phase fugacities, $f_i > 5 \times 10^3$ Pa, the adsorption is in favor of water, a consequence of entropy effects. The continuous solid lines are the IAST calculations using the pure component isotherm fits. IAST calculations are able to provide a reasonably good description of mixture adsorption equilibrium for partial fugacities $f_i < 1 \times 10^3$ Pa. For $f_i > 2 \times 10^3$ Pa, there are significant quantitative deviations between IAST calculations and CBMC simulations of water loadings.

Figure 35b and Figure 35c present CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in FAU. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. The CBMC data show enhancements ranging to 5 or 10, significantly higher than the corresponding enhancements calculated from IAST. This suggests that H-bonding and clustering effects are in play. Such clustering effects have the effect of dragging water molecules into the FAU framework.

The departures of CBMC simulations from IAST get reflected in the values of activity coefficients that depart from unity. Figure 35d presents the calculations of the activity coefficients γ_i of individual components in the mixture as a function of the total fluid phase fugacity, f_1+f_2 . We note that in the range of fugacities wherein enhancements are higher than unity, the activity coefficients are lower than unity.

Figure 36a presents CBMC simulations for adsorption of water/methanol mixtures in FAU zeolite at 300 K at a constant total fugacity of 1000 Pa. The continuous solid lines are the IAST calculations using the pure component fits in Table 7. The agreement between the IAST calculations and CBMC mixture simulations is not perfect. To quantify the deviations from IAST, Figures 36b, and 36c present values of the enhancement factors for water and methanol ingress, both from CBMC simulations and from IAST. The enhancement factors determined from CBMC simulations are higher than the predictions of IAST. The IAST predicts enhancement of water and methanol ingress to be both unity, whereas CBMC simulations show enhancements higher than unity. Values of enhancement factor larger than unity also get reflected in activity coefficients, γ_i , that are lower than unity; see Figure 36d.

Figure 37a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/ethanol mixture in FAU zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of the alcohol. However, we note that at partial phase fugacities, $f_i > 8 \times 10^3$ Pa, the adsorption is in favor of water, a consequence of entropy effects. The continuous solid lines are the IAST calculations using the pure component isotherm fits. IAST calculations are able to provide a reasonably good description of mixture adsorption equilibrium for $f_i < 3 \times 10^2$ Pa. For $f_i > 3 \times 10^2$ Pa, there

are significant quantitative deviations between IAST calculations and CBMC simulations of water loadings.

Figure 37b and Figure 37c present CBMC simulations of the enhancement of (b) water, and (c) ethanol ingress in FAU. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. The enhancement factor for ethanol is close to unity for the entire range of fugacities. The CBMC data for water show enhancements ranging to 8, significantly higher than the enhancements calculated from IAST. This suggests that H-bonding and clustering effects are in play; water is dragged into the FAU framework due to clustering with partner ethanol molecules.

For water, the departures of CBMC simulations from IAST get reflected in the values of activity coefficients that depart from unity. Figure 37d presents the calculations of the activity coefficients γ_i of individual components in the mixture as a function of the total fluid phase fugacity, f_1+f_2 . We note that in the range of fugacities wherein enhancements of water ingress are higher than unity, the activity coefficients for water are lower than unity.

13. Non-ideality effects for mixture adsorption in DDR zeolite

Consider the adsorption of water/methanol, and water/ethanol mixtures in all-silica DDR zeolite that consists of 278 \AA^3 cages, that are separated by $3.65 \text{ \AA} \times 4.37 \text{ \AA}$ size windows. Figure 38 shows CBMC simulations of Krishna and van Baten¹⁷ for pure component adsorption isotherms for water, methanol, and ethanol in DDR at 300 K. Above fluid phase fugacities of 10^5 Pa, pore saturation is reached and the hierarchy of saturation capacities water \gg methanol $>$ ethanol is a reflection of the size of the molecules.

Figure 39a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/methanol mixture in DDR zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of methanol. However, we note that at partial fugacities, $f_i > 8 \times 10^3$ Pa, the adsorption is in favor of water, a consequence of entropy effects. The continuous solid lines are the IAST calculations using pure component isotherm fits. IAST calculations are able to provide a

reasonably good description of mixture adsorption equilibrium for $f_i < 20$ Pa. For $f_i > 20$ Pa, there are significant quantitative deviations between IAST calculations and CBMC simulations of water loadings in the mixture.

Figure 39b and Figure 39c present CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in DDR. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. The CBMC data show enhancements ranging to 20 for water, significantly higher than the enhancements calculated from IAST. This suggests that H-bonding and clustering effects are in play; water ingress is much more significantly influenced than methanol ingress.

The departures of CBMC simulations from IAST get reflected in the values of activity coefficients that depart from unity. Figure 39d presents the calculations of the activity coefficients γ_i of individual components in the mixture as a function of the total fluid phase fugacity, f_1+f_2 . We note that the activity coefficient for water is significantly lower than unity in the range of fugacities for which the enhancement in water ingress exceeds unity.

Figure 40a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/ethanol mixture in DDR zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of ethanol. However, we note that at partial fugacities, $f_i = 8 \times 10^3$ Pa, the loading of water equals that of ethanol. The continuous solid lines are the IAST calculations using pure component isotherm fits. IAST calculations are able to provide a reasonably good description of mixture adsorption equilibrium for $f_i < 10$ Pa. For $f_i > 10$ Pa, there are significant quantitative deviations between IAST calculations and CBMC simulations of water loadings in the mixture.

Figure 40b and Figure 40c present CBMC simulations of the enhancement of (b) water, and (c) ethanol ingress in DDR. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. The CBMC data show enhancements ranging to 40 for water,

significantly higher than the enhancements calculated from IAST. This suggests that H-bonding and clustering effects are in play; water ingress is much more significantly influenced than ethanol ingress.

The departures of CBMC simulations from IAST get reflected in the values of activity coefficients that depart from unity. Figure 40d presents the calculations of the activity coefficients γ_i of individual components in the mixture as a function of the total fluid phase fugacity, f_1+f_2 . We note that the activity coefficient for water is significantly lower than unity in the range of fugacities for which the enhancement in water ingress exceeds unity.

14. Non-ideality effects for mixture adsorption in MFI zeolite

Consider the adsorption of water/methanol, and water/ethanol mixtures in all-silica MFI zeolite that consists of intersecting channels of 5.5 Å. Figure 41 shows CBMC simulations of Krishna and van Baten¹⁷ for pure component adsorption isotherms for water, methanol, and ethanol in MFI at 300 K. Above fluid phase fugacities of 10^5 Pa, pore saturation is reached and the hierarchy of saturation capacities water \gg methanol $>$ ethanol is a reflection of the size of the molecules.

Figure 42a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/methanol mixture in MFI zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of methanol. However, we note that at partial fugacities, $f_i > 2 \times 10^4$ Pa, the adsorption is in favor of water, a consequence of entropy effects. The continuous solid lines are the IAST calculations using pure component isotherm fits. IAST calculations are able to provide a reasonably good description of mixture adsorption equilibrium for $f_i < 10$ Pa. For $f_i > 10$ Pa, there are significant quantitative deviations between IAST calculations and CBMC simulations of water loadings in the mixture.

Figure 42b and Figure 42c present CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in MFI. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. For $10 \text{ Pa} < f_i < 100 \text{ Pa}$, the CBMC data show enhancements ranging to 8 for water, significantly higher than the enhancements calculated from IAST. This suggests that H-

bonding and clustering effects are in play; water ingress is much more significantly influenced than methanol ingress.

Figure 43a presents CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/ethanol mixture in MFI zeolite at 300 K. In the Henry regime of adsorption, the water loading is significantly below that of ethanol.

Figures 43b and 43c present CBMC simulations of the enhancement of (b) water, and (c) ethanol ingress in MFI. The enhancement factor is defined as the loading of a component in the mixture divided by the loadings of that pure component determined at the same partial fugacity of that component in the bulk fluid phase. For $10 \text{ Pa} < f_i < 50 \text{ Pa}$, the CBMC data show enhancements ranging to 12 for water, significantly higher than the enhancements calculated from IAST. This suggests that H-bonding and clustering effects are in play at For $f_i > 10 \text{ Pa}$; water ingress is much more significantly influenced than ethanol ingress.

Experimental evidence of the enhancement of water ingress into MFI zeolite due to H-bonding effects with partner alcohol molecules can be inferred from the experimental data of Farzaneh et al.³⁰ for water/butanol mixture adsorption in all-silica MFI zeolite at 308 K. The set of three experimental data points for butanol/water and water/butanol selectivities are plotted in Figures 44a, and 44b. Comparisons with IAST calculations using unary isotherm fits (unary isotherm fit parameters reported in Table 10), clearly demonstrate that the water/butanol selectivity is significantly higher in the experiments than predicted by IAST calculations. This is indicative of enhanced water ingress into MFI due to H-bonding with butanol molecules. It must be stressed that these conclusions are based on our interpretation of the Farzaneh et al.³⁰ experiments; these authors do not draw such conclusions and no IAST calculations were presented by them.

15. Non-ideality effects for mixture adsorption in CHA zeolite

Let us examine the data on the pure component isotherms for a series of 1-alcohols in CHA, which is a cage type zeolite that consists of 316 \AA^3 sized cages separated by $3.8 \text{ \AA} \times 4.2 \text{ \AA}$ sized windows. CBMC simulations of pure component 1-alcohols with C atoms in the 1 – 6 range in CHA at 300 K, as

reported in the work of Krishna and van Baten,³¹ are shown in Figure 45a. The continuous solid lines in Figure 45a are fits using the dual-Langmuir-Freundlich model with parameters as specified in Table 12. The saturation capacities, $\Theta_{i,\text{sat}}$, decreases from 5.4 molecules per cage for methanol to 1 molecule per cage for 1-hexanol; see data in Figure 45b. Figure 45c presents snapshots of the location, and conformations, of the 1-alcohols within the cages of CHA at saturation conditions. Except for methanol, the saturation cage capacity has an integer value because 1-alcohol molecules cannot locate at the window regions.

Consider adsorption of binary equimolar fluid mixtures of methanol and ethanol in CHA. The saturation capacities are 5.5 and 4 molecules per cage, respectively. CBMC simulations on the component loadings in equilibrium with an equimolar methanol-ethanol mixture is shown in Figure 46a for varying partial fluid phase fugacities, f_i .

At $f_i < 5$ kPa, the selectivity is in favor of the component with the longer chain length, ethanol; this is “normal” behavior for mixture adsorption. However, for $f_i > 5$ kPa selectivity reversal occurs and methanol is preferentially adsorbed due to its higher packing efficiency. The IAST calculations are shown by the continuous solid lines. For partial fugacities, $f_i < 10$ kPa, the IAST calculations are in good agreement with CBMC mixture simulations.

In order to quantify the deviations between CBMC and IAST, we calculate the enhancement factors for methanol and ethanol; see Figures 46b, and 46c. The deviations between the two sets become increasingly significant for $f_i > 10$ kPa. Correspondingly, the activity coefficients are lowered below unity for $f_i > 20$ kPa; see Figure 46d.

The CBMC simulations for ethanol - 1-propanol mixtures are shown in Figure 47a. For total fluid phase fugacities, $f_t < 300$ kPa, the adsorption selectivity is strongly in favor of the longer 1-propanol molecule. However, when the total fluid phase fugacity f_t exceeds 600 kPa, we find a reversal of selectivity. This selectivity reversal is entropy-based and is ascribable to the significantly higher saturation capacity of ethanol (4 molecules per cage) in comparison to that of 1-propanol (2 molecules per cage).

The CBMC simulations for ethanol - 1-hexanol mixtures are shown in Figure 47b. For total fluid phase fugacities, $f_t < 100$ kPa, the adsorption selectivity is strongly in favor of the longer 1-hexanol molecule. However, when the total fluid phase fugacities, f_t exceed 200 kPa, we find a reversal of selectivity. This selectivity is entropy-based and is ascribable to the significantly higher saturation capacity of ethanol (4 molecules per cage) in comparison to that of 1-hexanol (1 molecule per cage).

The continuous solid lines in Figures 47a,b are the predictions of the Ideal Adsorbed Solution Theory (IAST) of Myers and Prausnitz²⁴ using pure component isotherm fits. The IAST calculations have been presented here to demonstrate that selectivity reversal is not an unexpected phenomenon, but is a natural result that is obtained for a mixture of two species having (1) lower adsorption strength, but higher saturation capacity, and (2) higher adsorption strength, but lower saturation capacity. When saturation conditions are approached the component with the higher saturation capacity is invariably preferred. This is due to the fact that vacant “sites” are more easily filled by the smaller molecule at near-saturation conditions. Though the predictions of the IAST are in general qualitative agreement with CBMC simulations, the agreement is not quantitatively perfect. Figures 47c,d present the calculations of the activity coefficient. The trends in the values of activity coefficients γ_i are similar to that observed for methanol/ethanol mixtures in CHA.

16. MD simulation methodology

Diffusion is simulated using Newton’s equations of motion until the system properties, on average, no longer change in time. The Verlet algorithm is used for time integration. A time step of 1 fs was used in all simulations. For each simulation, *initializing* CBMC moves are used to place the molecules in the domain, minimizing the energy. Next, follows an *equilibration* stage. These are essentially the same as the production cycles, only the statistics are not yet taken into account. This removes any initial large disturbances in the system that do not affect statistics on molecular displacements. After a fixed number of initialization and equilibrium steps, the MD simulation *production* cycles start. For every cycle, the statistics for determining the mean square displacements (MSDs) are updated. The MSDs are determined for time intervals ranging from 2 fs to 1 ns. In order to do this, an order- N algorithm, as

detailed in Chapter 4 of Frenkel and Smit³² is implemented. The Nosé-Hoover thermostat is applied to all the diffusing particles.

The self-diffusivities $D_{i,\text{self}}$ for species i are computed from MD simulations by analyzing the mean square displacement for each coordinate direction

$$D_{i,\text{self}} = \frac{1}{2n_i} \lim_{\Delta t \rightarrow \infty} \frac{1}{\Delta t} \left\langle \left(\sum_{l=1}^{n_i} (\mathbf{r}_{l,i}(t + \Delta t) - \mathbf{r}_{l,i}(t))^2 \right) \right\rangle \quad (26)$$

CuBTC is isotropic, and the mean-square-displacements can be averaged over the three coordinate directions. Figures 48, 49, 50, and 51 present plots of the mean-square-deviations

$$\frac{1}{n_i} \left\langle \left(\sum_{l=1}^{n_i} (\mathbf{r}_{l,i}(t + \Delta t) - \mathbf{r}_{l,i}(t))^2 \right) \right\rangle, \text{ for diffusion of water, methanol, ethanol, and benzene in CuBTC at 298}$$

K. For the calculation of the $D_{i,\text{self}}$ using Equation (26), the slopes of the MSD vs time plots were determined for the time interval $t = 100$ ps to $t = 1000$ ps; in this time interval the plots are linear.

For single component diffusion, the Maxwell-Stefan diffusivity can be determined for each of the coordinate directions from

$$D_i = \frac{1}{2} \lim_{\Delta t \rightarrow \infty} \frac{1}{n_i} \frac{1}{\Delta t} \left\langle \left(\sum_{l=1}^{n_i} (\mathbf{r}_{l,i}(t + \Delta t) - \mathbf{r}_{l,i}(t)) \right)^2 \right\rangle \quad (27)$$

If we define the self-exchange coefficient D_{ii} as a diffusivity characteristic of molecule-molecule interactions, we get the interpolation formula for self-diffusivity

$$1/D_{i,\text{self}} = 1/D_i + 1/D_{ii} \quad (28)$$

Equation (28), formally valid for *both* micro- and meso-porous materials, will be derived in a later section starting with the M-S equations for binary mixture diffusion for identical species, tagged, and un-tagged. At any loading $D_{i,\text{self}} \leq D_i$; this is because individual jumps of molecules are *correlated* due to re-visitation of sites that have been recently abandoned. The D_i , reflecting *collective* motion of molecules is free from such correlation effects; it is for this reason that the D_i are amenable to simpler interpretation, and modeling, than the $D_{i,\text{self}}$.

In this work, we determined only the self-diffusivities of water, methanol, ethanol, and benzene in CuBTC at 298 K; the data are summarized in Figure 52.

17. Loading dependence of unary diffusivities in CuBTC

The simplest model to describe the occupancy dependence of the Maxwell-Stefan diffusivity is

$$D_i = D_i(0)(1 - \theta_i) \quad (29)$$

where $D_i(0)$ is the diffusivity in the limiting case of vanishingly small *fractional occupancy*, defined by

$$\theta_i \equiv c_i / c_{i,sat} \quad (30)$$

The key to the quantification of the concentration dependence of D_i is to determine how the vacancy $(1 - \theta_i)$ changes with increased pore concentration. This information is contained in the *inverse thermodynamic factor* $1/\Gamma_i$. If the adsorbed phase concentration follows a single-site Langmuir isotherm

$$c_i = c_{i,sat} \frac{b_i f_i}{1 + b_i f_i} \quad (31)$$

we obtain from eqn (4)

$$1/\Gamma_i = (1 - c_i/c_{i,sat}) = (1 - \theta_i) \quad (32)$$

Equation (32) shows that inverse thermodynamic factor, $1/\Gamma_i$, equals the fractional *vacancy* $(1 - \theta_i)$. In the general case where the component adsorption exhibits inflection behavior, due perhaps to second-order phase transitions, $1/\Gamma_i$ provides a good indicator of how the availability of adsorption sites changes with increased bulk fluid phase fugacity. We can generalize eqn (29) to cater for more complex adsorption isotherm characteristics by writing

$$D_i = D_i(0) \frac{1}{\Gamma_i} \quad (33)$$

Equation (33) would lead us to expect that that the sharp peak in the loading dependence of $1/\Gamma_i$ would cause a corresponding peak in the loading dependence of D_i . This expectation is fulfilled for the

experimental data of Chmelik et al.³³, obtained by transient uptake within crystals of CuBTC using Infrared Microscopy (IRM), of n-butane (nC4, $T_c = 425$ K), iso-butane (iC4, $T_c = 408$ K), neopentane (neo-P, $T_c = 434$ K), and 2-methylbutane (2MB, $T_c = 460$ K) at $T = 298$ K, significantly lower than the critical temperatures of each of the four guest species; see Figure 53. The observed behaviors of $1/\Gamma_i$ and D_i for loadings $\Theta_i < 8$ molecules per unit cell needs special attention and explanation. The CuBTC structure consists of two types of “cages” and two types of “windows” separating these cages. Large cages are inter-connected by 9 Å windows of square cross-section. The large cages are also connected to tetrahedral-shaped pockets of ca. 6 Å size through triangular-shaped windows of ca. 4.6 Å size. There are 8 tetrahedral pockets per unit cell, and these are preferred locations of molecules at low loadings. Each pocket can accommodate only one of nC4, iC4, neo-P or 2MB; this is illustrated by the snapshot in Figure 54 for neo-P adsorbed in CuBTC. For loadings $\Theta_i < 8$ molecules per unit cell, the alkanes prefer location in the pockets, and the diffusion characteristics are dictated by hops across triangular windows of 4.6 Å. Consequently, the diffusivities tend to be low. The diffusivities of molecules inhabiting the larger cages are about an order of magnitude higher because they correspond to hops across larger 9 Å windows. As the molecules begin to populate the larger cages, the D_i increase sharply till a maximum is reached.

With the above background information using experimental data from the literature, let us analyze the characteristics of self-diffusivities of water, methanol, ethanol, and benzene in CuBTC at 298 K presented in Figure 52.

The tetrahedral pockets can accommodate about 9 molecules of water (see Table 2), and this explains the low diffusivity values for occupancies below about 0.2.

Compared at the same fractional pore occupancy, it is interesting to note that the diffusivities of benzene are higher than those for either methanol or ethanol. The most likely reason for this is the molecular clustering effects are practically non-existent for benzene molecules. Methanol, and ethanol, on the other hand experience strong clustering, and this explains the lower diffusivity values. The molecular clustering effects for methanol are stronger than for ethanol; for this reason, the methanol

diffusivities are slightly lower than that of ethanol, when compared at the same value of pore occupancy.

In order to rationalize the loading dependences of the diffusivities, let us compare $D_{i,\text{self}}$ vs q_i data with $1/\Gamma_i$ vs. q_i data. Figure 55 present plots of MD simulations of the self-diffusivities $D_{i,\text{self}}$, and the inverse thermodynamic factor $1/\Gamma_i$ in CuBTC of (a) water, (b) methanol, (c) ethanol, and (d) benzene as a function of the component loading, q_i . Figure 56 presents the corresponding plots using the fractional pore occupancy, θ_i , on the x -axis.

The characteristics of the $D_{i,\text{self}}$ vs q_i are largely derived from the corresponding characteristics of $1/\Gamma_i$ vs. q_i data. This finding is in agreement with the corresponding observation made in respect of the D_i vs, q_i data for n-butane, iso-butane, neopentane, and 2-methylbutane in CuBTC.^{33, 34}

A further point to note is that the $D_{i,\text{self}}$ vs θ_i data for methanol displays a step-wise characteristic; the diffusivity values in the range $0.6 < \theta_i < 0.8$ are practically the same. Experimental data of Tsotsalas et al.²² for transient desorption profiles for methanol in CuBTC at 298 K was found to display step-wise characteristics; see Figure 57a. The explanation for the step-wise desorption is clearly to be found in the correspond loading dependence of the diffusivities that is strongly influenced by molecular clustering; this conclusion is re-enforced in Figure 57b that presents a comparison of the experimental transient desorption profile with the loading dependence of the self-diffusivity.

18. Notation

| | |
|-----------------------|--|
| A | surface area per kg of framework, $\text{m}^2 \text{kg}^{-1}$ |
| b_A | Langmuir-Freundlich constant for adsorption site A, $\text{Pa}^{-\nu_A}$ |
| b_B | Langmuir-Freundlich constant for adsorption site B, $\text{Pa}^{-\nu_B}$ |
| b_C | Langmuir-Freundlich constant for adsorption site C, $\text{Pa}^{-\nu_C}$ |
| C | constant used in equation (22), kg mol^{-1} |
| D_i | Maxwell-Stefan diffusivity, $\text{m}^2 \text{s}^{-1}$ |
| D_i | Fick diffusivity of species i , $\text{m}^2 \text{s}^{-1}$ |
| $D_{i,\text{self}}$ | self-diffusivity of species i , $\text{m}^2 \text{s}^{-1}$ |
| f_i | partial fugacity of species i , Pa |
| f_t | total fugacity of bulk fluid mixture, Pa |
| n | number of species in the mixture, dimensionless |
| P_i^0 | sorption pressure, Pa |
| q_i | component molar loading of species i , mol kg^{-1} |
| q_t | total molar loading for mixture adsorption, mol kg^{-1} |
| $q_{i,\text{sat}}$ | molar loading of species i at saturation, mol kg^{-1} |
| Q_{st} | isosteric heat of adsorption, J mol^{-1} |
| $\mathbf{r}_{l,i}(t)$ | position vector for molecule l of species i at any time t , m |
| R | gas constant, $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ |
| t | time, s |
| T | absolute temperature, K |
| V_p | pore volume, $\text{m}^3 \text{kg}^{-1}$ |

Greek letters

| | |
|------------|--|
| γ_i | activity coefficient of component i in adsorbed phase, dimensionless |
| Γ_i | thermodynamic factor, dimensionless |

| | |
|----------------|--|
| ν | exponent in multi-site-Langmuir-Freundlich isotherm, dimensionless |
| π | spreading pressure, N m^{-1} |
| Λ_{ij} | Wilson parameters, dimensionless |
| θ_i | fractional occupancy of component i , dimensionless |
| θ_t | fractional occupancy for mixture adsorption, dimensionless |

Subscripts

| | |
|-----|----------------------------|
| i | referring to component i |
| t | referring to total mixture |

Table 1. Lennard Jones parameters and point charges for the Cu-BTC and adsorbates.

| Atom types | Epsilon/ k_B (K) | Sigma (Å) | Charge (e) |
|-----------------------|-----------------------|--------------|----------------|
| Adsorbates | | | |
| CH ₃ _C_ol | 98.0 | 3.75 | - |
| CH ₃ _O_ol | 98.0 | 3.75 | 0.265 |
| CH ₂ _C_ol | 46.0 | 3.95 | - |
| CH ₂ _O_ol | 46.0 | 3.95 | 0.265 |
| CH ₃ _C_ke | 98.0 | 3.75 | - |
| C_O_ke | 40.0 | 3.82 | 0.424 |
| O_ke | 79.0 | 3.05 | -0.424 |
| O_ol | 93.0 | 3.02 | -0.7 |
| H_ol | - | - | 0.435 |
| O_water | 89.516 | 3.097 | - |
| H_water | - | - | 0.241 |
| Dummy_water | - | - | -0.241 |
| C_benzene | 30.7 | 3.6 | -0.095 |
| H_benzene | 25.45 | 2.36 | 0.095 |
| Cu-BTC | | | |
| MOF-Cu | 2.518 | 3.114 | 1.248 |
| MOF-O | 48.19 | 3.03 | -0.624 |
| MOF-C1 | 47.86 | 3.47 | 0.494 |
| MOF-C2 | 47.86 | 3.47 | 0.13 |
| MOF-C3 | 47.86 | 3.47 | -0.156 |
| MOF-H | 7.65 | 2.85 | 0.156 |

Table 2. Number of molecules that can be located in the tetrahedral pockets.

| | f kPa | Loading /molec uc ⁻¹ | Loading in T1 cages/ molec uc ⁻¹ | Tetrahedral cages molec/T1 cage |
|------------|------------|------------------------------------|--|------------------------------------|
| Methanol | 10000 | 202 | 29 | 3-4 |
| Ethanol | 50 | 125 | 21 | 2-3 |
| 1-Propanol | 30000 | 98 | 8 | 1 |
| Water | 30000 | 512 | 72 | 9 |

No benzene molecules can be located within the tetrahedral cages.

Table 3. 3-site Langmuir-Freundlich isotherm fits for adsorption of water in CuBTC at 298 K.

| | Site A | | | Site B | | | Site C | | |
|-------|---------------------------------------|---|-------|---------------------------------------|---|-------|---------------------------------------|--|-------|
| | $q_{A,sat} /$ mol kg ⁻¹ | $b_A /$ Pa ^{-v_{iA}} | v_A | $q_{B,sat} /$ mol kg ⁻¹ | $b_B /$ Pa ^{-v_{iB}} | v_B | $q_{C,sat} /$ mol kg ⁻¹ | $b_C /$ Pa ^{-v_C} | v_C |
| water | 22 | 5.48 ×10 ⁻⁴ | 1 | 22 | 6.24 ×10 ⁻³² | 10 | 10 | 2.51 ×10 ⁻⁴ | 0.6 |

Table 4. Dual-site Langmuir-Freundlich parameters for adsorption of methanol, ethanol, acetone, and benzene at 298 K in CuBTC.

| Adsorbate | Site A | | | Site B | | |
|-----------|-------------------------------------|---|------------------------|-------------------------------------|---|------------------------|
| | $q_{A,sat}$ mol kg ⁻¹ | b_{A0} Pa ^{-v_A} | v_A dimensionless | $q_{B,sat}$ mol kg ⁻¹ | b_{B0} Pa ^{-v_B} | v_B dimensionless |
| methanol | 8.4 | 3.82×10^{-4} | 1.03 | 11.5 | 9.3×10^{-16} | 6.5 |
| ethanol | 5 | 2.29×10^{-3} | 0.97 | 8 | 6.41×10^{-7} | 3.2 |
| acetone | 5 | 4.83×10^{-17} | 7.5 | 4.9 | 1.39×10^{-2} | 0.7 |
| benzene | 4.6 | 2.76×10^{-6} | 3.1 | 2.1 | 3.96×10^{-3} | 1 |

Table 5. Dual-site Langmuir-Freundlich parameters for adsorption of water, methanol, ethanol, 1-propanol, 2-propanol, chloroform, benzene, and acetone at 298 K in TetZB. These fits are for the “adsorption” branch of the isotherms. The data are from Motkuri et al.³⁵

| Adsorbate | Site A | | | Site B | | |
|------------|-------------------------------------|---|------------------------|-------------------------------------|---|------------------------|
| | $q_{A,sat}$ mol kg ⁻¹ | b_{A0} Pa ^{-v_A} | v_A dimensionless | $q_{B,sat}$ mol kg ⁻¹ | b_{B0} Pa ^{-v_B} | v_B dimensionless |
| water | 3 | 4.01×10^{-5} | 0.94 | 18 | 3.02×10^{-46} | 13 |
| methanol | 4.6 | 1.28×10^{-36} | 10 | 6 | 5.08×10^{-3} | 0.62 |
| ethanol | 3.6 | 3.97×10^{-38} | 12 | 3.2 | 8.4×10^{-3} | 0.7 |
| 1-propanol | 2.7 | 5.92×10^{-35} | 12.5 | 2.5 | 2.79×10^{-2} | 0.6 |
| 2-propanol | 2.7 | 4.83×10^{-27} | 7.8 | 1.7 | 4.43×10^{-2} | 0.6 |
| chloroform | 1.75 | 1.22×10^{-39} | 13.2 | 2.7 | 4.76×10^{-2} | 0.4 |
| benzene | 1.6 | 1×10^{-36} | 17.5 | 17 | 2.97×10^{-2} | 0.12 |
| acetone | 3 | 6.48×10^{-14} | 4 | 2.6 | 2.49×10^{-1} | 0.2 |

Table 6. Dual-site Langmuir-Freundlich parameters for ethanol/benzene mixture adsorption at 298 K in CuBTC.

| Adsorbate | Site A | | | Site B | | |
|--------------------------------------|-------------------------------------|---|------------------------|-------------------------------------|---|------------------------|
| | $q_{A,sat}$ mol kg ⁻¹ | b_{A0} Pa ^{-v_A} | v_A dimensionless | $q_{B,sat}$ mol kg ⁻¹ | b_{B0} Pa ^{-v_B} | v_B dimensionless |
| ethanol | 4.5 | 2.57×10^{-3} | 0.9 | 4.7 | 2.04×10^{-5} | 2.8 |
| Total loading of ethanol and benzene | 4.4 | 2.1×10^{-3} | 1.1 | 7.5 | 2.33×10^{-14} | 8 |

Table 7. Dual-site Langmuir-Freundlich parameters for adsorption of water, methanol, and ethanol at 300 K in all-silica FAU zeolite. The fit parameters are based on the CBMC simulations of pure component isotherms presented in earlier work.¹⁷

| Adsorbate | Site A | | | Site B | | |
|-----------|--|---|--------------------------|--|---|--------------------------|
| | $q_{A,\text{sat}}$ mol kg ⁻¹ | b_{A0} Pa ^{-ν_A} | ν_A dimensionless | $q_{B,\text{sat}}$ mol kg ⁻¹ | b_{B0} Pa ^{-ν_B} | ν_B dimensionless |
| water | 16 | 1.54×10^{-121} | 33 | 4.6 | 624×10^{-5} | 1 |
| methanol | 3.4 | 6.36×10^{-16} | 4.6 | 5.8 | 1.68×10^{-4} | 1 |
| ethanol | 2.5 | 3.19×10^{-13} | 4.9 | 2.9 | 1×10^{-3} | 1.05 |

Table 8. Dual-site Langmuir-Freundlich parameters for pure component water, methanol, and ethanol at 300 K in all-silica DDR zeolite. The fit parameters are based on the CBMC simulations of pure component isotherms presented in earlier work.¹⁷ Note that the saturation capacities are specified in molecules per cage; multiply these by 0.832157 to obtain the values in mol per kg framework.

| | Site A | | | Site B | | |
|----------|---|--|----------------------------|---|--|----------------------------|
| | $\Theta_{i,A,sat}$ Molecules cage ⁻¹ | $b_{i,A}$ Pa ^{-v_i} | $v_{i,A}$ dimensionless | $\Theta_{i,B,sat}$ molecules cage ⁻¹ | $b_{i,B}$ Pa ^{-v_i} | $v_{i,B}$ dimensionless |
| water | 8.083 | 3.85×10^{-16} | 4 | 2.667 | 1.73×10^{-5} | 1 |
| methanol | 2.1667 | 1.49×10^{-4} | 1.25 | 1.9167 | 6×10^{-4} | 0.77 |
| ethanol | 1.8167 | 7.66×10^{-3} | 1 | 0.775 | 8.59×10^{-6} | 1 |

Table 9. Dual-site Langmuir-Freundlich parameters for adsorption of water, methanol, and ethanol at 300 K in all-silica MFI zeolite. The fit parameters are based on CBMC simulations of Krishna and van Baten.¹⁷

| Adsorbate | Site A | | | Site B | | |
|-----------|-------------------------------------|---|------------------------|-------------------------------------|---|------------------------|
| | $q_{A,sat}$ mol kg ⁻¹ | b_{A0} Pa ^{-v_A} | v_A dimensionless | $q_{B,sat}$ mol kg ⁻¹ | b_{B0} Pa ^{-v_B} | v_B dimensionless |
| water | 6.7 | 6.37×10^{-24} | 6.2 | 3.6 | 1.09×10^{-5} | 1.04 |
| methanol | 2.4 | 1×10^{-4} | 1.64 | 1.4 | 1.92×10^{-3} | 0.7 |
| ethanol | 1.1 | 2.82×10^{-4} | 2.7 | 1.7 | 1.91×10^{-2} | 0.9 |

Table 10. Dual-site Langmuir parameters for adsorption of water, and butanol at 308 K in all-silica MFI zeolite. The parameter values are from Table 1 of Farzaneh et al.³⁰

| Adsorbate | Site A | | Site B | |
|-----------|-------------------------------------|------------------------------|-------------------------------------|------------------------------|
| | $q_{A,sat}$ mol kg ⁻¹ | b_{A0} Pa ⁻¹ | $q_{B,sat}$ mol kg ⁻¹ | b_{B0} Pa ⁻¹ |
| water | 0.23 | 48.38×10^{-3} | 2.96 | 0.17×10^{-3} |
| butanol | 1.8 | 860×10^{-3} | | |

Table 11. Experimental data of Farzaneh et al.³⁰ for water(1)/butanol(2) mixture adsorption in all-silica MFI zeolite, along with comparisons with IAST calculations using the unary isotherm fit parameters in Table 10.

| Vapor phase partial pressures | | Vapor phase mole fraction of butanol | Experimental data | | IAST calculations | |
|-------------------------------|---------------|--------------------------------------|--|--|--|--|
| $f_1/$ kPa | $f_2/$ kPa | y_2 | Butanol/ Water selectivity Experiment | Water/ Butanol selectivity Experiment | Butanol/ Water selectivity IAST | Water/ Butanol selectivity IAST |
| 2.04 | 0.35 | 0.146 | 107 | 264.7 | 0.009345794 | 0.003778191 |
| 2.03 | 0.57 | 0.219 | 84 | 218.5 | 0.011904762 | 0.00457721 |
| 1.8 | 0.7 | 0.28 | 62 | 199.5 | 0.016129032 | 0.005013702 |

Table 12. Dual-site Langmuir-Freundlich parameters for pure component water, and 1-alcohols in CHA at 300 K. The fit parameters are based on the CBMC simulations of pure component isotherms presented in earlier work.³¹ Note that the saturation capacities are specified in molecules per cage; multiply these by 1.387 to obtain the values in mol per kg framework.

$$\Theta_i = \Theta_{i,A,sat} \frac{b_{i,A} f_i^{V_{i,A}}}{1 + b_{i,A} f_i^{V_{i,A}}} + \Theta_{i,B,sat} \frac{b_{i,B} f_i^{V_{i,B}}}{1 + b_{i,B} f_i^{V_{i,B}}}$$

| | Site A | | | Site B | | |
|------------|---|--|----------------------------|---|--|----------------------------|
| | $\Theta_{i,A,sat}$ Molecules cage ⁻¹ | $b_{i,A}$ Pa ^{-v_i} | $v_{i,A}$ dimensionless | $\Theta_{i,B,sat}$ molecules cage ⁻¹ | $b_{i,B}$ Pa ^{-v_i} | $v_{i,B}$ dimensionless |
| methanol | 12 | 7.86×10^{-59} | 17 | 9 | 8.32×10^{-6} | 1 |
| methanol | 2.7 | 6.77×10^{-11} | 3.3 | 2.7 | 4.45×10^{-4} | 1 |
| ethanol | 2 | 7.93×10^{-5} | 0.87 | 2 | 3.6×10^{-3} | 1.14 |
| 1-propanol | 1 | 1.28×10^{-2} | 1.8 | 1 | 9.11×10^{-2} | 1 |
| 1-butanol | 1 | 0.231 | 1.46 | 1 | 0.5066 | 1 |
| 1-pentanol | 0.5 | 19.26 | 1.72 | 0.5 | 6.91 | 1 |
| 1-hexanol | 0.5 | 2561 | 2.4 | 0.5 | 24.8 | 1 |

Table 13. Wilson non-ideality parameters for binary mixtures in CuBTC at 298 K.

| | Λ_{12} | Λ_{21} | C |
|------------------|----------------|----------------|-------|
| methanol/ethanol | 1.1 | 3.5 | 0.028 |
| ethanol/benzene | 1 | 3.6 | 0.12 |

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20. Caption for Figures

Figure 1. Paddle-wheel chemical structure of CuBTC.

Figure 2. Cage connectivity of CuBTC framework.

Figure 3. (a) Molar densities of pure water, methanol, ethanol, and 1-propanol as a function of the bulk fluid phase fugacities. (b) Molar densities of equimolar water/ethanol mixtures as a function of the bulk fluid phase fugacity, f_t . These calculations are based on the Peng-Robinson equation of state.

Figure 4. Comparison of the CBMC simulations for water adsorption in CuBTC with 3-site Langmuir-Freundlich model. Also shown are the experimental isotherm data of Zhao et al.,¹³ Yazaydin et al.,¹⁴ and Küsgens et al.¹⁵ measured at 298 K.

Figure 5. (a) Comparison of the CBMC simulations for adsorption of water, methanol, ethanol, acetone, and benzene in CuBTC with multi-site-Langmuir-Freundlich model.

Figure 6. The fractional occupancy within the pores, θ_i , for guest molecules as a function of the bulk fluid phase fugacity, f_i .

Figure 7. The inverse thermodynamic factor, $1/\Gamma_i$, plotted as a function of the (a) molar loading, and (b) fractional pore occupancy for water, methanol, ethanol, acetone, and benzene in CuBTC at 298 K. The $1/\Gamma_i$ are calculated by differentiation of multi-site-Langmuir-Freundlich fits of the isotherms.

Figure 8. Variation of the inverse thermodynamic correction factor with fractional occupancy for methanol in CuBTC at 298 K. The experimental data of Tsotsalas et al.²² are compared with the $1/\Gamma_i$ obtained from dual-Langmuir-Freundlich fits of the CBMC simulated isotherms.

Figure 9. CBMC simulations for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, (d) methanol/ethanol, and (e) acetone/benzene mixtures in CuBTC at 298 K. The CBMC simulations for equimolar methanol/ethanol mixtures, already reported in earlier work,²³ are also included here for comparison purposes. (f) Adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and methanol/ethanol, and acetone/benzene mixtures in CuBTC at 298 K.

Figure 10. Calculations of total pore occupancy, θ_t , for adsorption of equimolar water/benzene, methanol/benzene, ethanol/benzene, acetone/benzene and methanol/ethanol mixtures in CuBTC at 298 K.

Figure 11. CBMC simulations for equimolar water/methanol/ethanol/benzene mixtures in CuBTC at 298 K.

Figure 12. Average occupation profiles of water (top) and benzene (bottom) in the binary water/benzene mixture.

Figure 13. Average occupation profiles of methanol (top) and benzene (bottom) in the binary methanol/benzene mixture.

Figure 14. Average occupation profiles of ethanol (top) and benzene (bottom) in the binary ethanol/benzene mixture.

Figure 15. Average occupation profiles of acetone (top) and benzene (bottom) in the binary acetone/benzene mixture.

Figure 16. Average occupation profiles of benzene, methanol, ethanol, and water in the quaternary mixture.

Figure 17. (a) CBMC simulations of adsorption of pure water with CBMC simulations of adsorption of mixtures containing water. The comparisons are on the basis of the same partial fugacity of water in the bulk fluid phase. (b) CBMC simulations of the enhancement of water ingress in CuBTC. The enhancement factor is defined as the loading of water in the mixture divided by the loadings of pure water.

Figure 18. CBMC simulations of adsorption of pure methanol with CBMC simulations of adsorption of mixtures containing methanol. The comparisons are on the basis of the same partial fugacity of methanol in the bulk fluid phase.

Figure 19. CBMC simulations of adsorption of pure ethanol with CBMC simulations of adsorption of mixtures containing ethanol. The comparisons are on the basis of the same partial fugacity of ethanol in the bulk fluid phase.

Figure 20. CBMC simulations of adsorption of pure 1-propanol with CBMC simulations of adsorption of mixtures containing 1-propanol. The comparisons are on the basis of the same partial fugacity of 1-propanol in the bulk fluid phase.

Figure 21. CBMC simulations of adsorption of pure benzene with CBMC simulations of adsorption of mixtures containing benzene. The comparisons are on the basis of the same partial fugacity of benzene in the bulk fluid phase.

Figure 22. Comparison of CBMC simulations for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, (d) methanol/ethanol, (e) acetone/benzene, and (f) water/methanol/ethanol/benzene mixtures in CuBTC at 298 K with IAST calculations. In these plots the component loadings are represented on linear y -axes.

Figure 23. Comparison of CBMC simulations for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, (d) methanol/ethanol, (e) acetone/benzene, and (f) water/methanol/ethanol/benzene mixtures in CuBTC at 298 K with IAST calculations. In these plots the component loadings are represented on logarithmic y -axes.

Figure 24. Adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and methanol/ethanol, and acetone/benzene mixtures in CuBTC at 298 K determined from (a) CBMC mixture simulations, and (b) IAST calculations. (c) Comparison of selectivities obtained from CBMC with IAST calculations.

Figure 25. Comparison of CBMC simulations and IAST calculations of the enhancement of water ingress in CuBTC. The enhancement factor is defined as the loading of water in the mixture divided by the loadings of pure water, both compared at the same partial fugacity in the bulk fluid phase. The calculations are for (a) water/methanol, (b) water/ethanol, (c) water/1-propanol, (d) water/benzene, (e) water/methanol/ethanol/1-propanol, and (f) water/methanol/ethanol/benzene mixtures.

Figure 26. Adsorption selectivities for equimolar water/benzene, methanol/benzene, ethanol/benzene, and methanol/ethanol, and acetone/benzene mixtures in TetZB at 298 K determined from IAST calculations using the pure component isotherm data fit parameters presented in Table 5.

Figure 27. (a, b, c) Comparing the RDFs for $H_{\text{benzene-O}_{\text{molecule}}}$ and $H_{\text{molecule-O}_{\text{molecule}}}$ distances for (a) water/benzene, (b) methanol/benzene, and (c) ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa. (d) Comparing the RDFs for $H_{\text{molecule-O}_{\text{molecule}}}$ distances for quaternary water/methanol/ethanol/benzene mixtures in CuBTC at 298 K and total fluid fugacity of 1000 Pa.

Figure 28. Comparing the RDFs for $H_{\text{benzene-O}_{\text{molecule}}}$ distances for (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) acetone/benzene mixtures in CuBTC at 298 K and five different total fluid fugacity values.

Figure 29. Comparison of RDF of $H_{\text{molecule-O}_{\text{molecule}}}$ distances for (a) water, (b) methanol, and (c) ethanol at 300 K in ZIF-8, LTA, FAU, DDR, and MFI. These data are from Krishna and van Baten.¹⁷

Figure 30. (a) Comparison of the CBMC simulation data for component loading, q_1 , of ethanol in ethanol/benzene mixture with dual-Langmuir fits using the parameters specified in Table 6. (b) Comparison of the CBMC simulation data for total mixture loading, q_t , with dual-Langmuir fits using the parameters specified in Table 6.

Figure 31. Activity coefficients of the components in the adsorbed phase for equimolar (a) water/benzene, (b) methanol/benzene, (c) ethanol/benzene, and (d) methanol/ethanol, and (e) acetone/benzene mixtures in CuBTC at 298 K.

Figure 32. Correction factor $\left(1 - \exp\left(-C \frac{\pi A}{RT}\right)\right)$ for ethanol/benzene mixture adsorption in CuBTC at 298 K. These calculations are based on the equation (22) taking $\Lambda_{12} = 1$; $\Lambda_{21} = 3.6$; $C = 0.12 \text{ kg mol}^{-1}$.

Figure 33. (a, b) Comparison of CBMC simulations for equimolar (a) ethanol/benzene, and (b) methanol/ethanol mixtures in CuBTC at 298 K with RAST calculations. (c, d) RAST calculations of the activity coefficients for equimolar (a) ethanol/benzene, and (b) methanol/ethanol mixtures in CuBTC at 298 K.

Figure 34. CBMC simulations of pure component adsorption isotherms for water, methanol, and ethanol in all-silica FAU zeolite at 300 K. The CBMC data are from Krishna and van Baten.¹⁷ The continuous solid lines are the Dual-Langmuir-Freundlich fits using the parameters specified in Table 7.

Figure 35. (a) CBMC simulations for adsorption of equimolar ($f_1=f_2$) water/methanol mixture in FAU zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 7. (b, c) CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in FAU, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for water and methanol.

Figure 36. (a) CBMC simulations for adsorption of water/methanol mixtures in FAU zeolite at 300 K at a constant total fugacity of 1000 Pa. The continuous solid lines are the IAST calculations using the pure component fits in Table 7. (b, c) CBMC simulations of the enhancement of (b) water, and (c) methanol

ingress in FAU, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for water and methanol as a function of mole fraction of water in the bulk fluid phase.

Figure 37. (a) CBMC simulations for adsorption of equimolar ($f_1=f_2$) water/ethanol mixture in FAU zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 7. (b, c) CBMC simulations of the enhancement of (c) water, and (b) ethanol ingress in FAU, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for water and ethanol.

Figure 38. CBMC simulations of pure component adsorption isotherms for water, methanol, and ethanol in all-silica DDR zeolite at 300 K. The CBMC data are from Krishna and van Baten.¹⁷ The continuous solid lines are the Dual-Langmuir-Freundlich fits using the parameters specified in Table 8.

Figure 39. (a) CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/methanol mixture in DDR zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 8. (b, c) CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in DDR, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for water and methanol.

Figure 40. (a) CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/ethanol mixture in DDR zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 8. (b, c) CBMC simulations of the enhancement of (c) water, and (b) ethanol ingress in DDR, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for water and ethanol.

Figure 41. CBMC simulations of pure component adsorption isotherms for water, methanol, and ethanol in all-silica MFI zeolite at 300 K. The CBMC data are from Krishna and van Baten.¹⁷ The continuous solid lines are the Dual-Langmuir-Freundlich fits using the parameters specified in Table 9.

Figure 42. (a) CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/methanol mixture in MFI zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 9. (b, c) CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in MFI, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase.

Figure 43. (a) CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) water/ethanol mixture in MFI zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 9. (b, c) CBMC simulations of the enhancement of (c) water, and (b) ethanol ingress in MFI, compared with IAST calculations. The enhancement factor is defined as the loading the

mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase.

Figure 44. Experimental data of Farzaneh et al.³⁰ for (a) butanol/water, and (b) water/butanol selectivities in all-silica MFI zeolite at 308 K. Also shown are the IAST calculations using the unary isotherm fit parameters reported in Table 10. The plotted data points are summarized in Table 11.

Figure 45. (a) CBMC simulations³¹ of pure component adsorption isotherms for water, and 1-alcohols in CHA at 300 K. Table 12 provides the pure component isotherm fit parameters. (b) Saturation capacities for adsorption of 1-alcohols in CHA at 300 K. (c) Snapshots showing the conformations of 1-alcohols in CHA at saturation conditions.

Figure 46. (a) CBMC simulations for adsorption of equimolar (partial fugacities $f_1=f_2$) methanol/ethanol mixture in CHA zeolite at 300 K. The continuous solid lines are the IAST calculations using the pure component fits in Table 12. (b, c) CBMC simulations of the enhancement of (b) water, and (c) methanol ingress in CHA, compared with IAST calculations. The enhancement factor is defined as the loading the mixture divided by the loadings of pure component determined at the same partial fugacity in the bulk fluid phase. (d) Activity coefficients γ_i for methanol and ethanol.

Figure 47. CBMC mixture simulations for (a) ethanol - 1-propanol, (b) ethanol -1-hexanol mixtures in CHA at 300 K. The partial fugacities in the bulk fluid phase are taken to be equal, i.e. $f_1=f_2$. The continuous solid lines represent calculations of the Ideal Adsorbed Solution Theory (IAST)²⁴ using

dual-Langmuir-Freundlich fits of pure component isotherms. Table **12** provides the pure component isotherm fit parameters. (c, d) Activity coefficients for (c) ethanol - 1-propanol, (d) ethanol -1-hexanol mixtures.

Figure 48. Mean-square-deviations for diffusion of water in CuBTC at 298 K, averaged over the x, y, and z directions. The values of the loadings are expressed per unit cell of CuBTC.

Figure 49. Mean-square-deviations for diffusion of methanol in CuBTC at 298 K, averaged over the x, y, and z directions. The values of the loadings are expressed per unit cell of CuBTC.

Figure 50. Mean-square-deviations for diffusion of ethanol in CuBTC at 298 K, averaged over the x, y, and z directions. The values of the loadings are expressed per unit cell of CuBTC.

Figure 51. Mean-square-deviations for diffusion of benzene in CuBTC at 298 K, averaged over the x, y, and z directions. The values of the loadings are expressed per unit cell of CuBTC.

Figure 52. (a) MD simulations of the self-diffusivities $D_{i,\text{self}}$ of water in CuBTC at 298 K as a function of the component loading q_i . (b) MD simulations of the self-diffusivities $D_{i,\text{self}}$ of water, methanol, ethanol, and benzene as a function of the fractional pore occupancy, θ_i .

Figure 53. Loading dependence of the Maxwell-Stefan diffusivity D_i , and the inverse thermodynamic factor $1/\Gamma_i$ in CuBTC of (a) n-butane (nC4), (b) iso-butane (iC4), (c) 2,2-dimethylpropane (= neopentane = neoP), and (d) 2-methylbutane (=2MB). The symbols represent D_i values backed out from

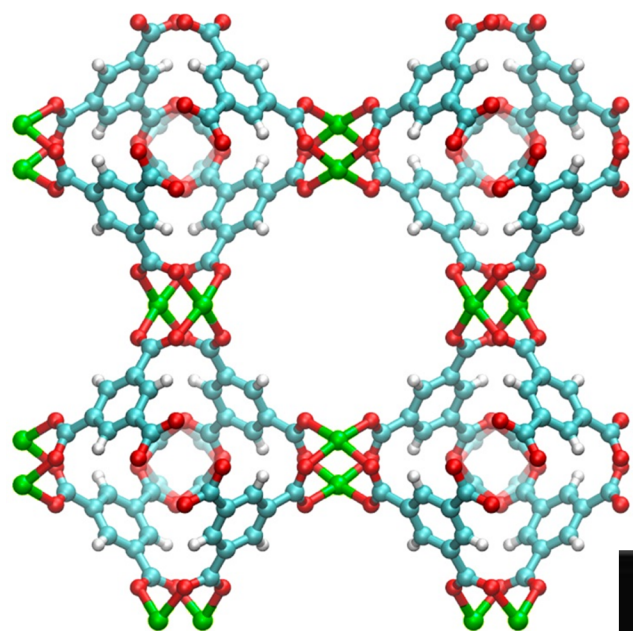
IRM experiments, and the continuous solid lines are derived from IRM isotherm fits. These data are re-plotted using the information contained in Chmelik et al.³³

Figure 54. (a) Pore landscape of CuBTC showing the adsorbed neopentane (neo-P) molecules. (b) Snapshot showing the location of neo-pentane lodged within a tetrahedral pocket.

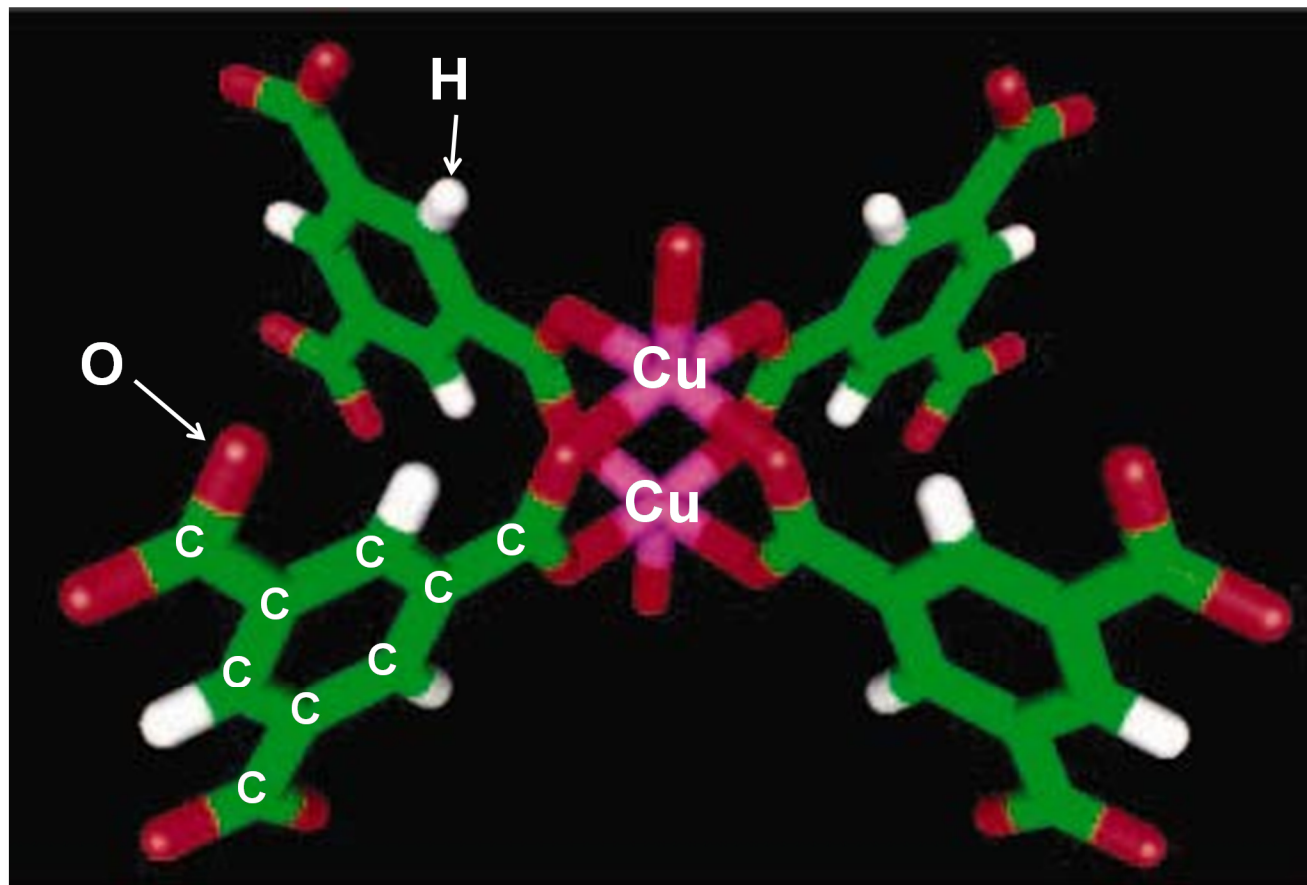
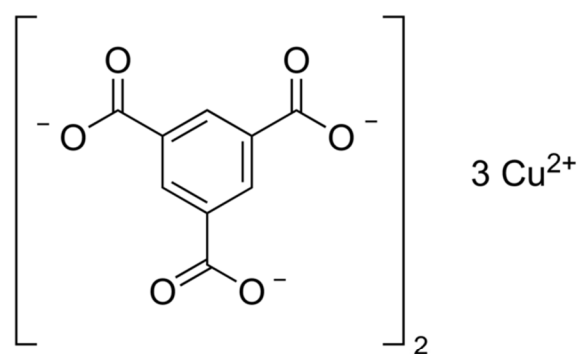
Figure 55. MD simulations of the self-diffusivities $D_{i,\text{self}}$, and the inverse thermodynamic factor $1/\Gamma_i$ in CuBTC of (a) water, (b) methanol, (c) ethanol, and (d) benzene as a function of the component loading q_i .

Figure 56. MD simulations of the self-diffusivities $D_{i,\text{self}}$, and the inverse thermodynamic factor $1/\Gamma_i$ in CuBTC of (a) water, (b) methanol, (c) ethanol, and (d) benzene as a function of the fractional pore occupancy, θ .

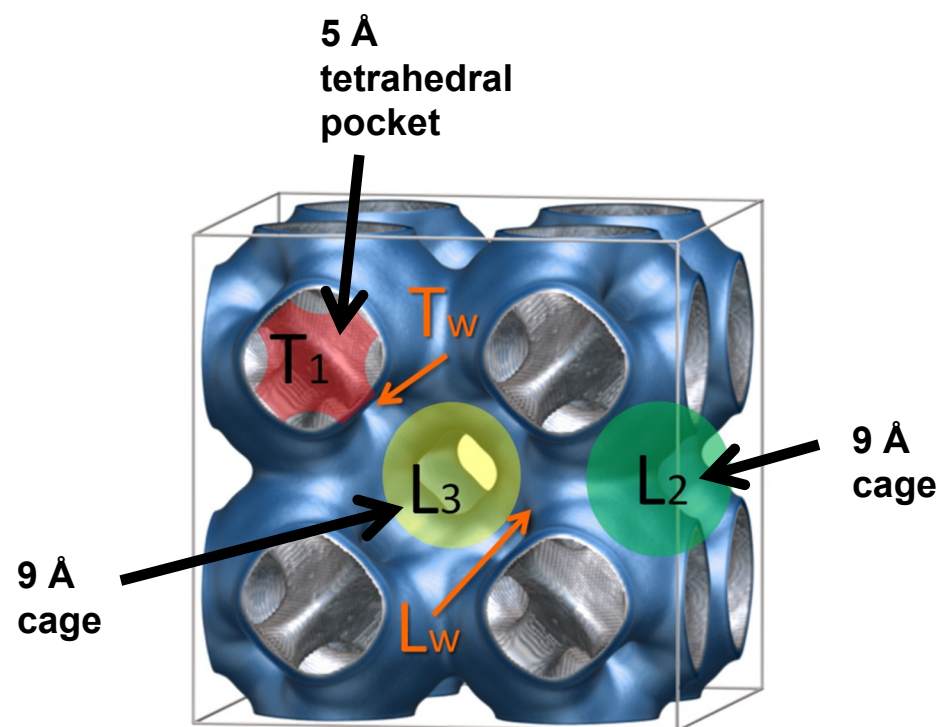
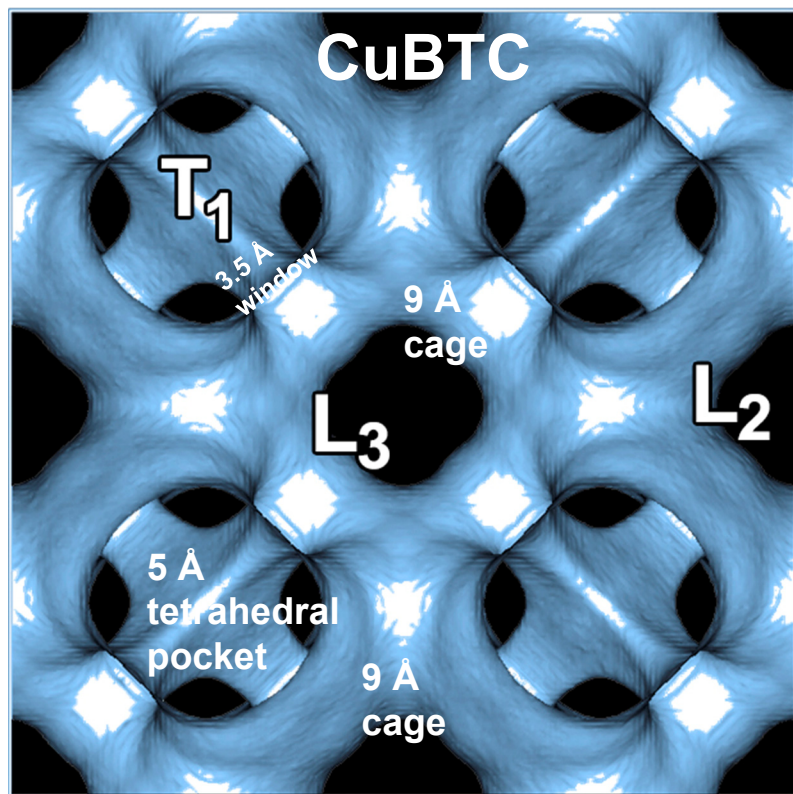
Figure 57. (a) Transient desorption profiles for methanol in CuBTC at 298 K. Experimental data of Tsotsalas et al.²² (b) Comparison of the experimental transient desorption profile with the loading dependence of the self-diffusivity.



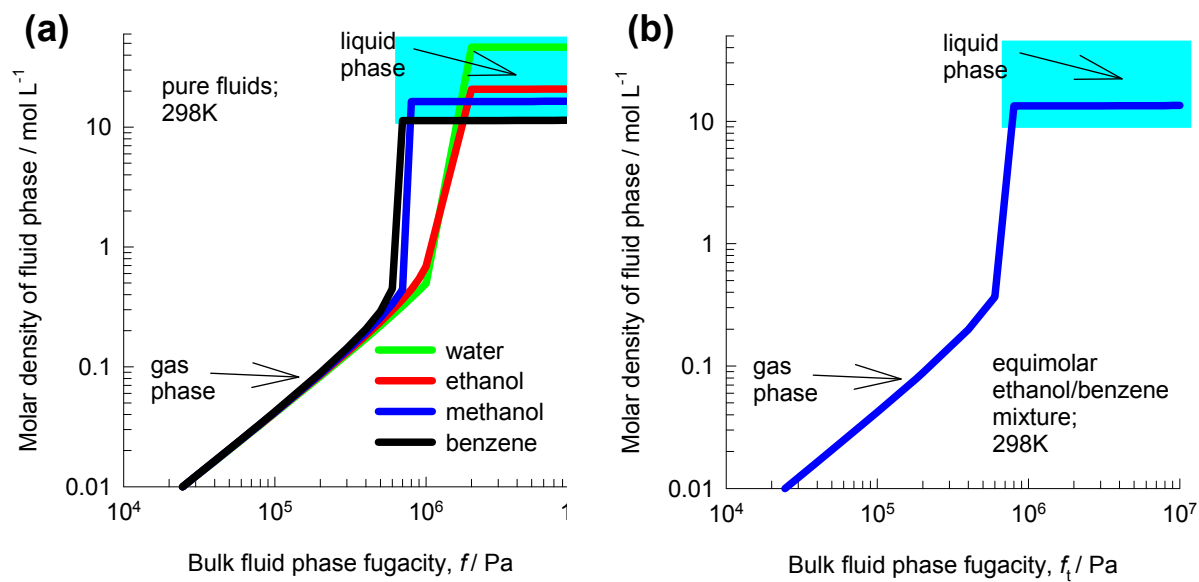
CuBTC: atomic structure



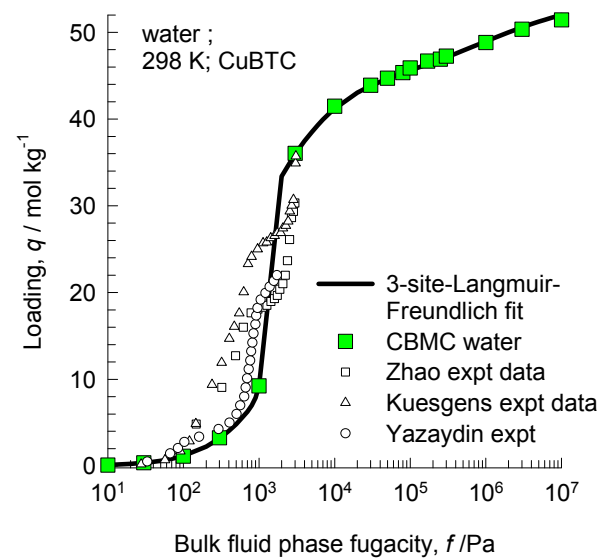
CuBTC framework



Molar densities of fluids

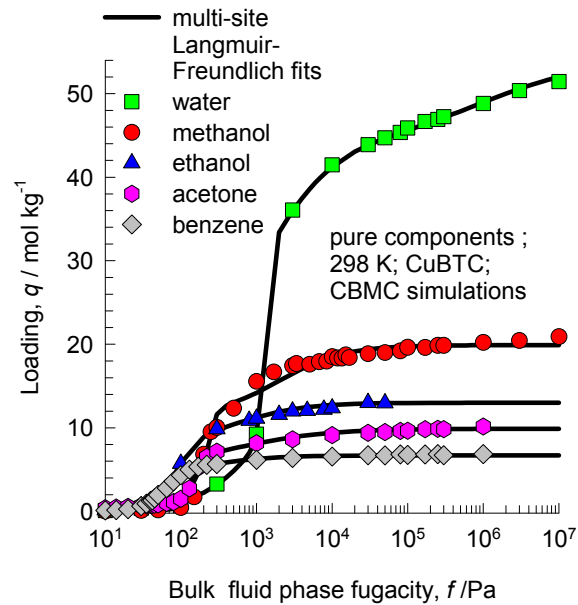


Adsorption of water in CuBTC: validation

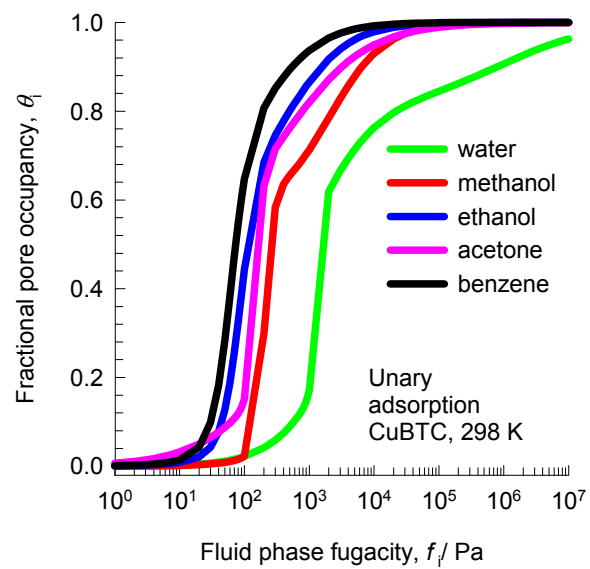


Unary isotherms: water, alcohols, acetone, and benzene in CuBTC

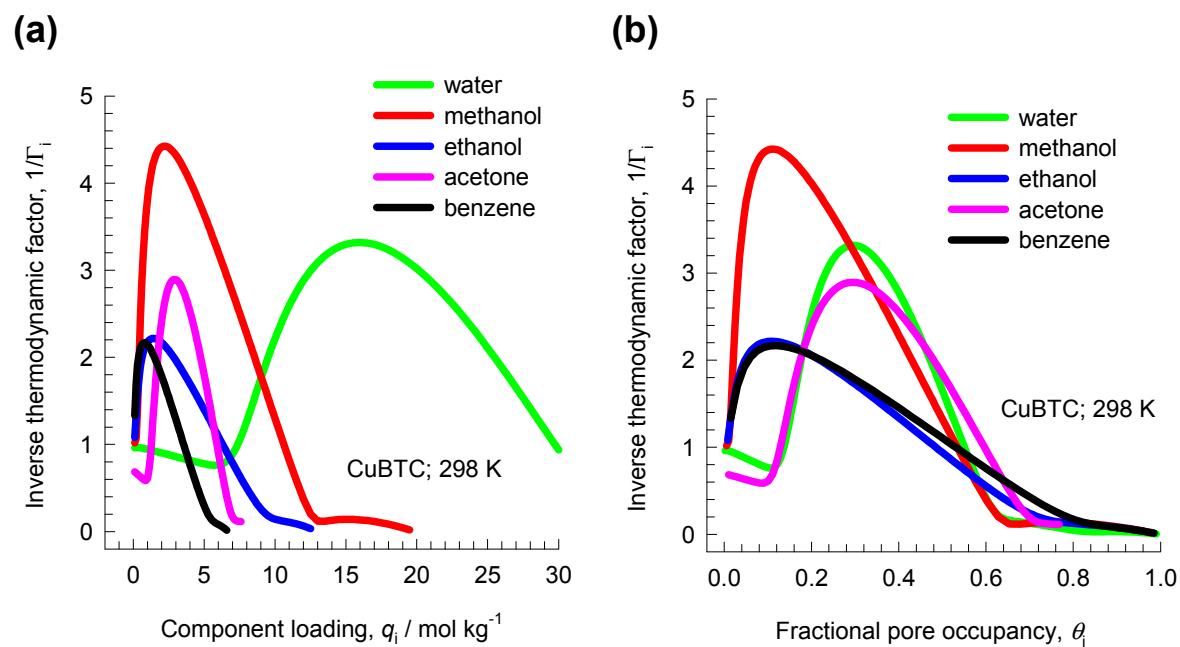
Figure ESI 6



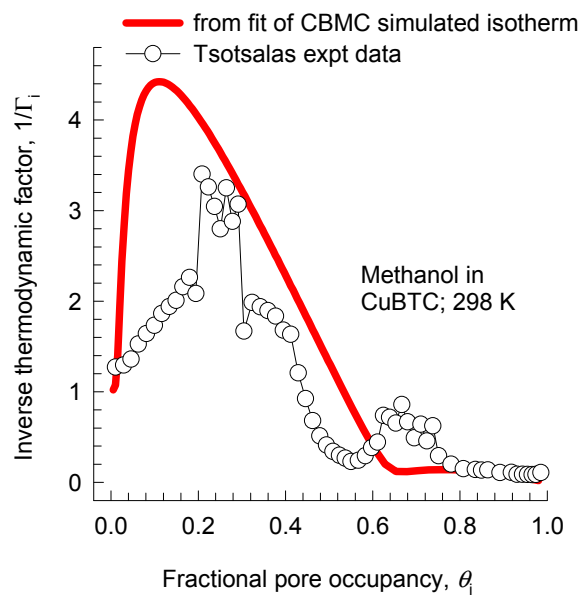
Fractional pore occupancies



Inverse Thermodynamic Factor

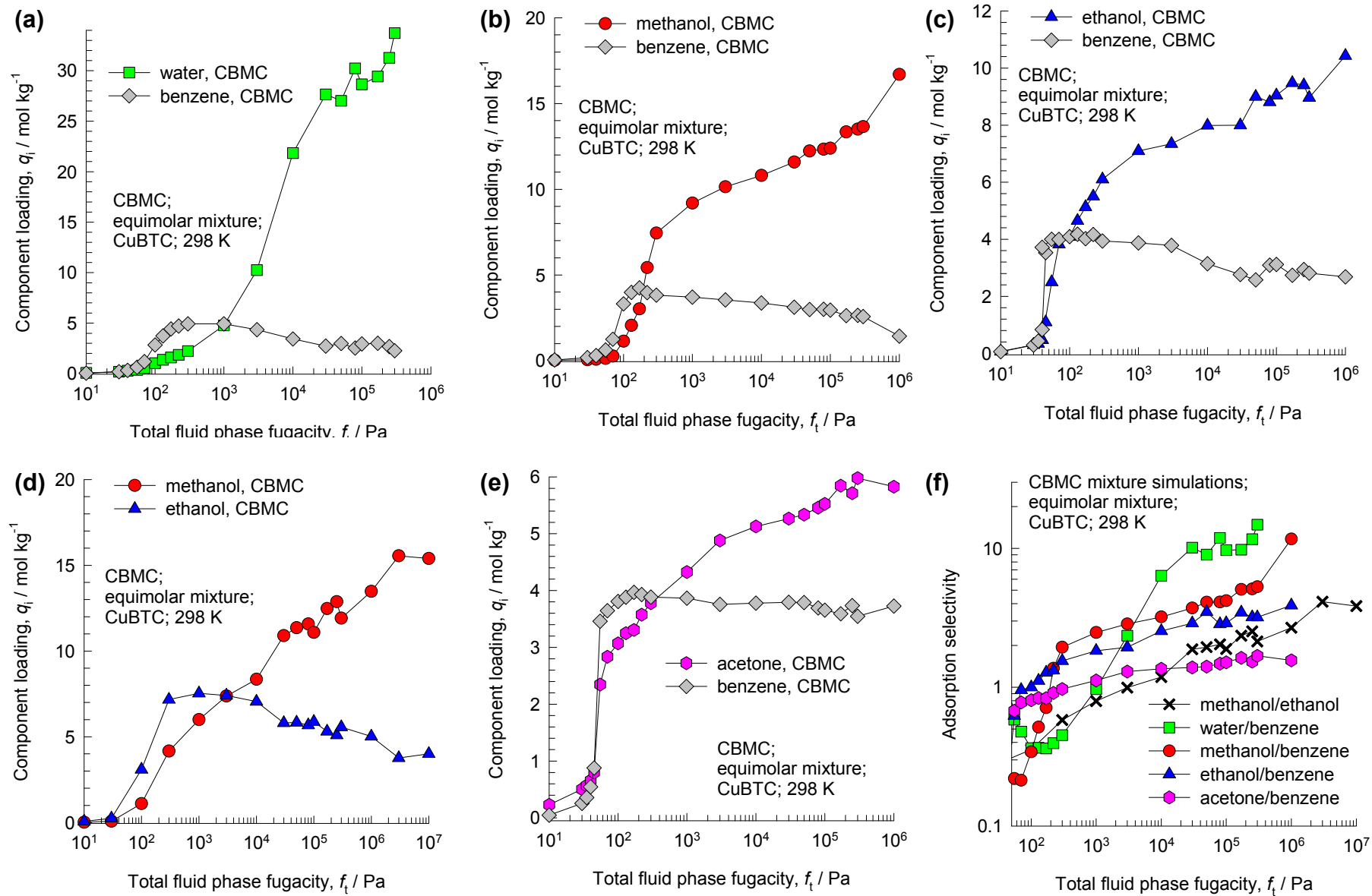


Inverse Thermodynamic Factor: Methanol

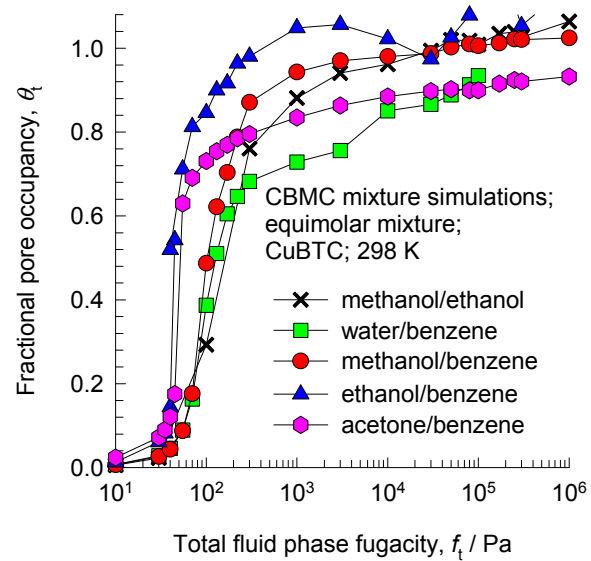


CBMC binary mixture simulations

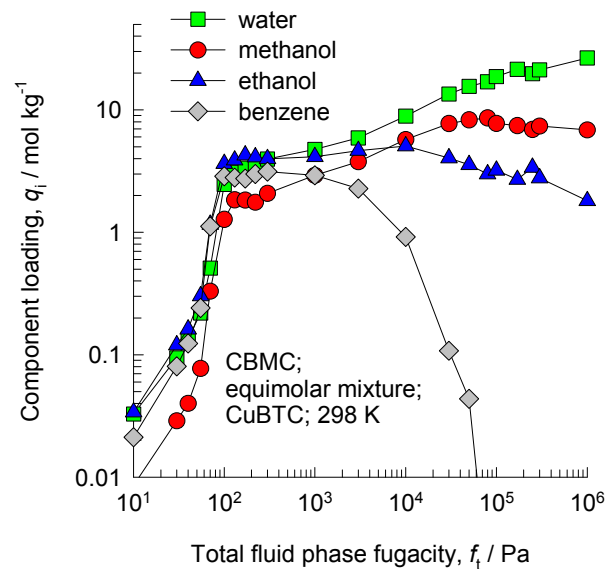
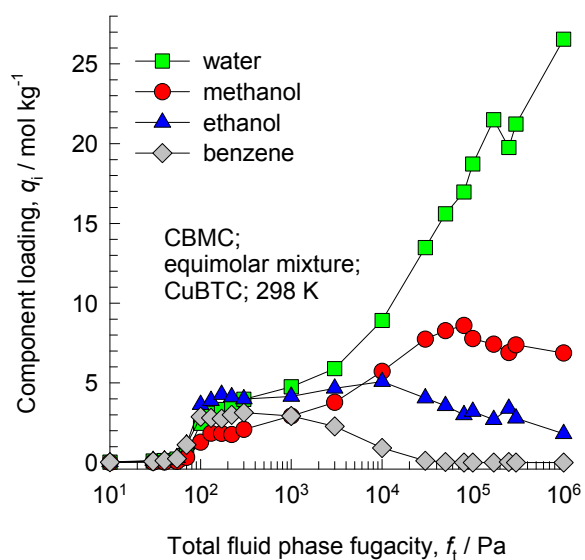
Figure ESI 9



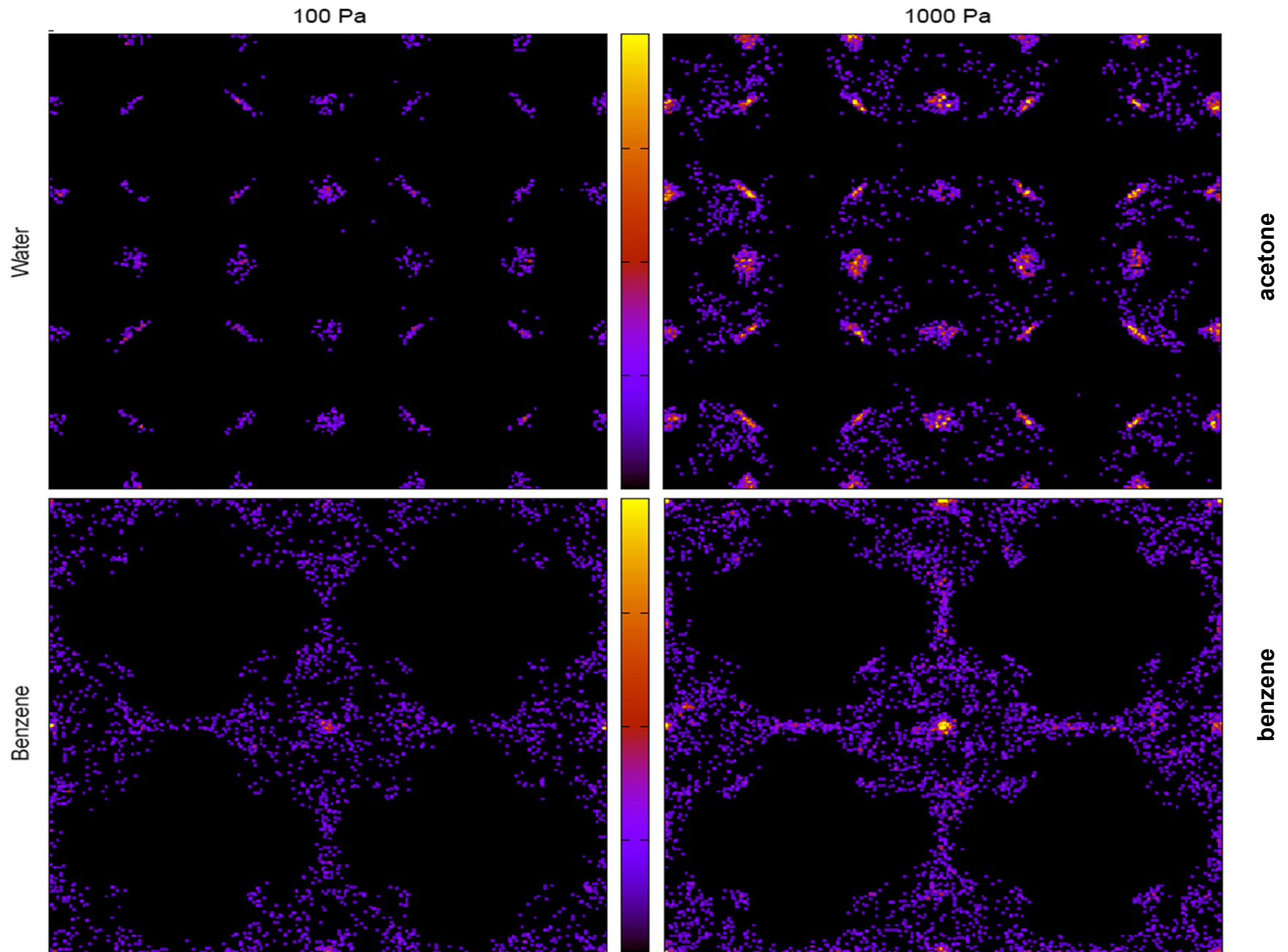
Fractional pore occupancies



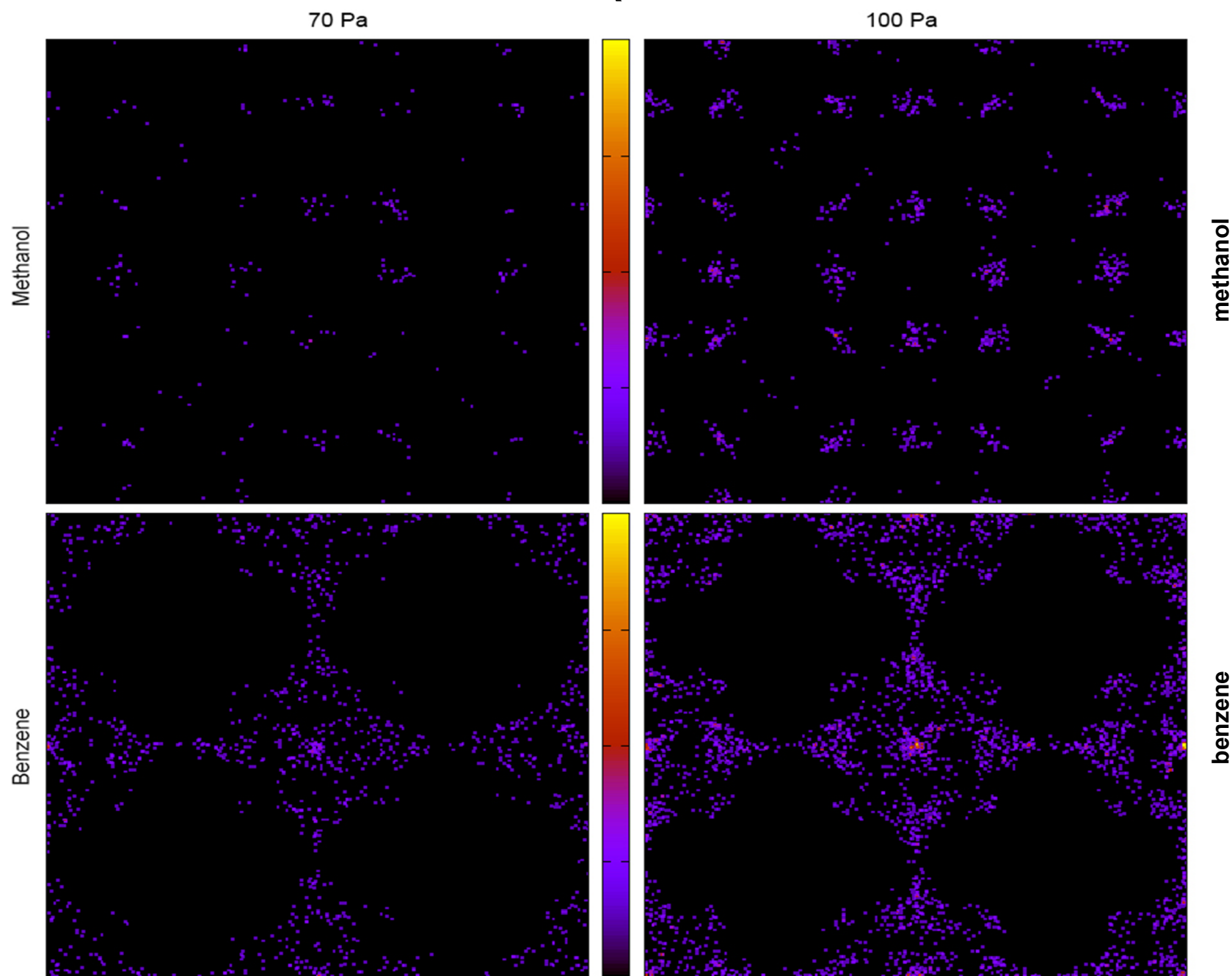
CBMC quaternary mixture simulations Figure ESI 11



snaps

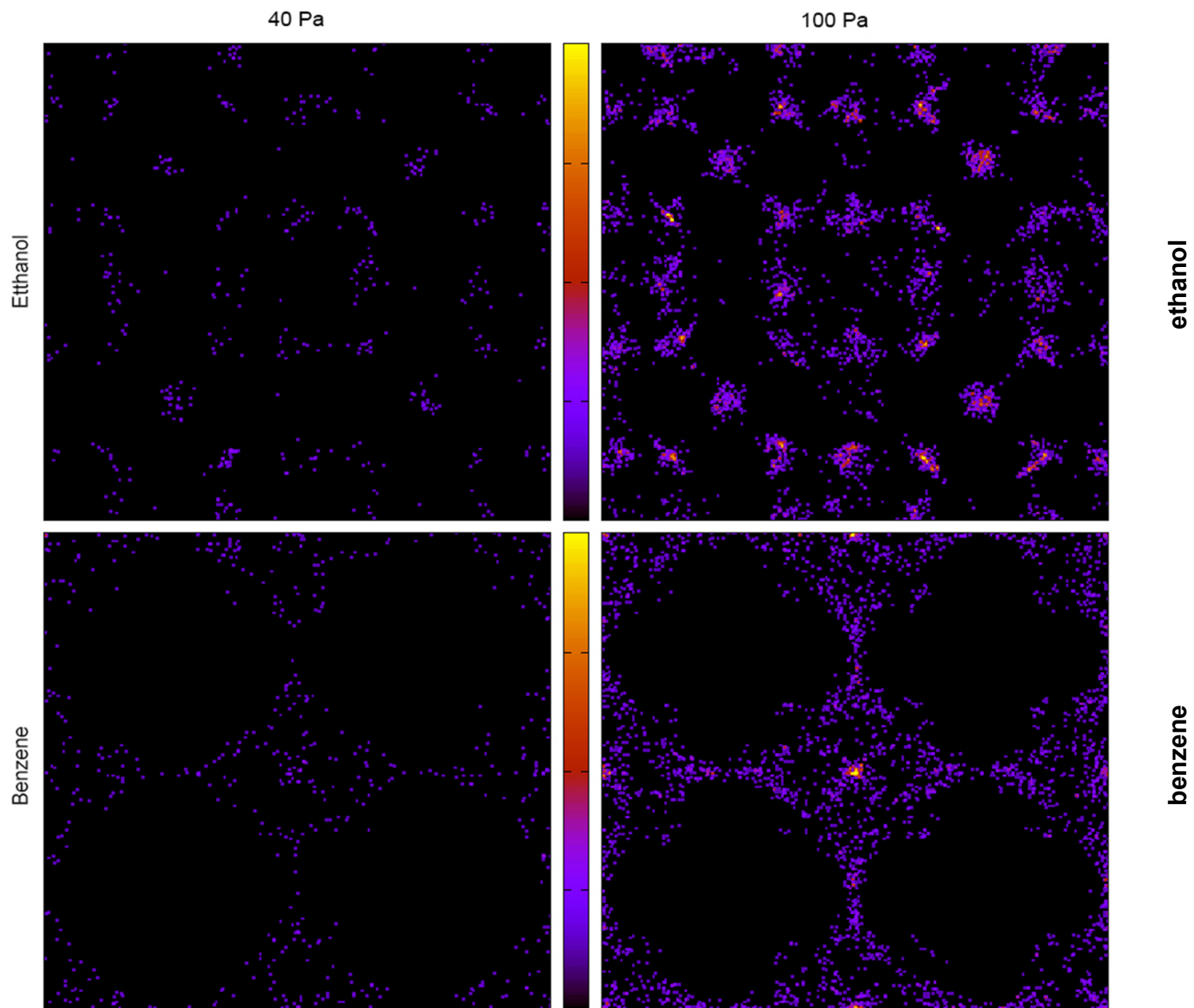


snaps



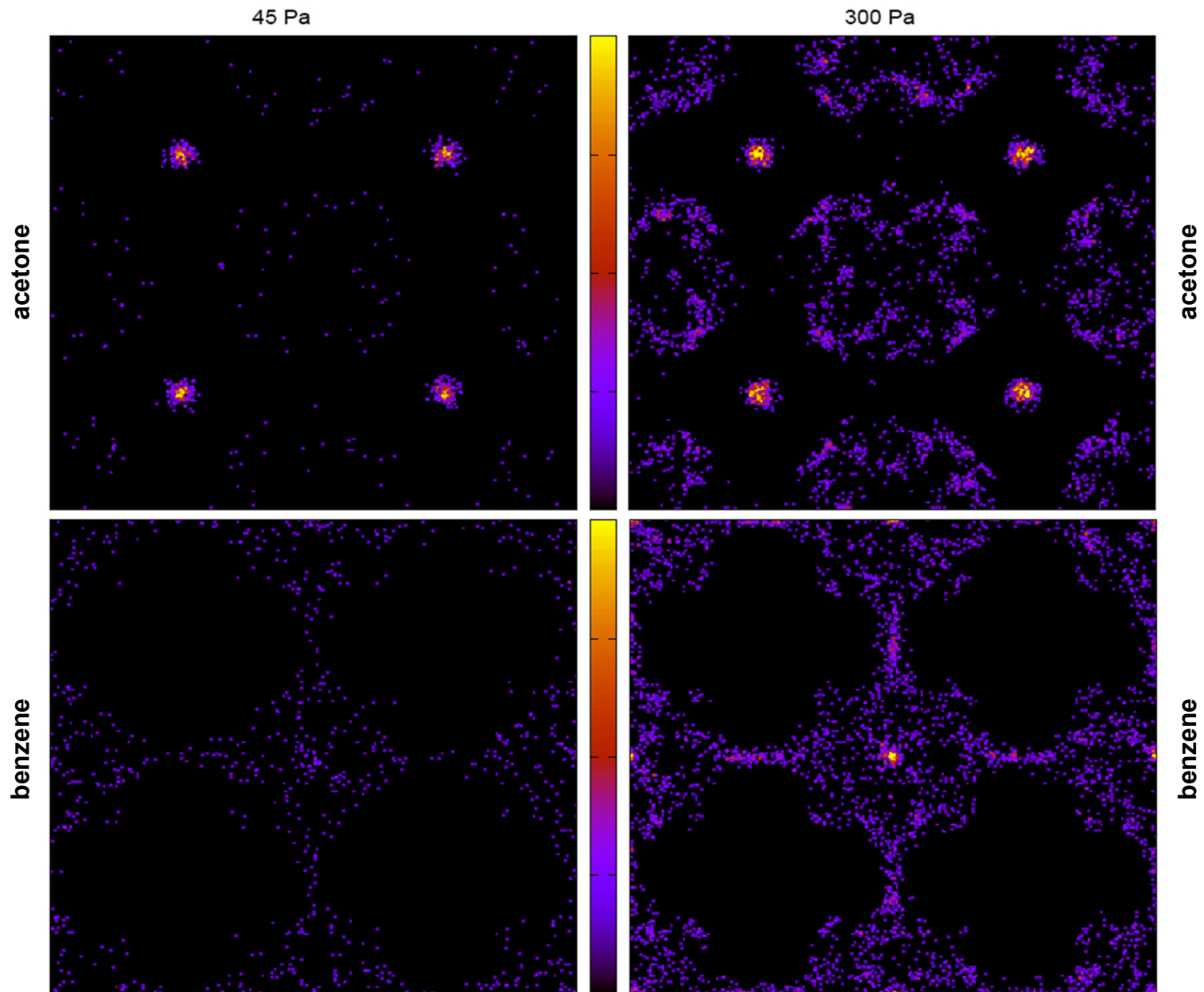
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Figure ESI 14



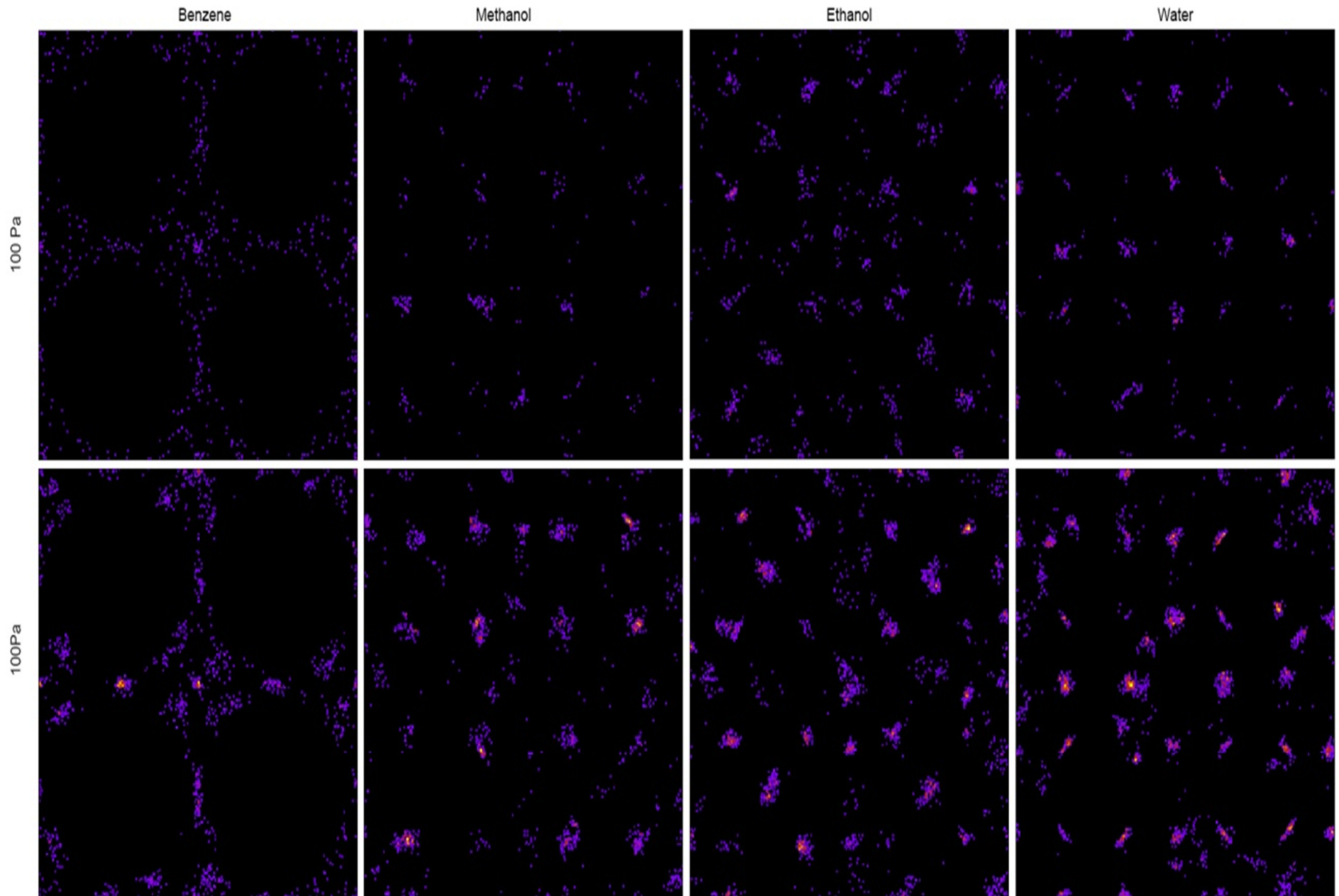
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Figure ESI 15

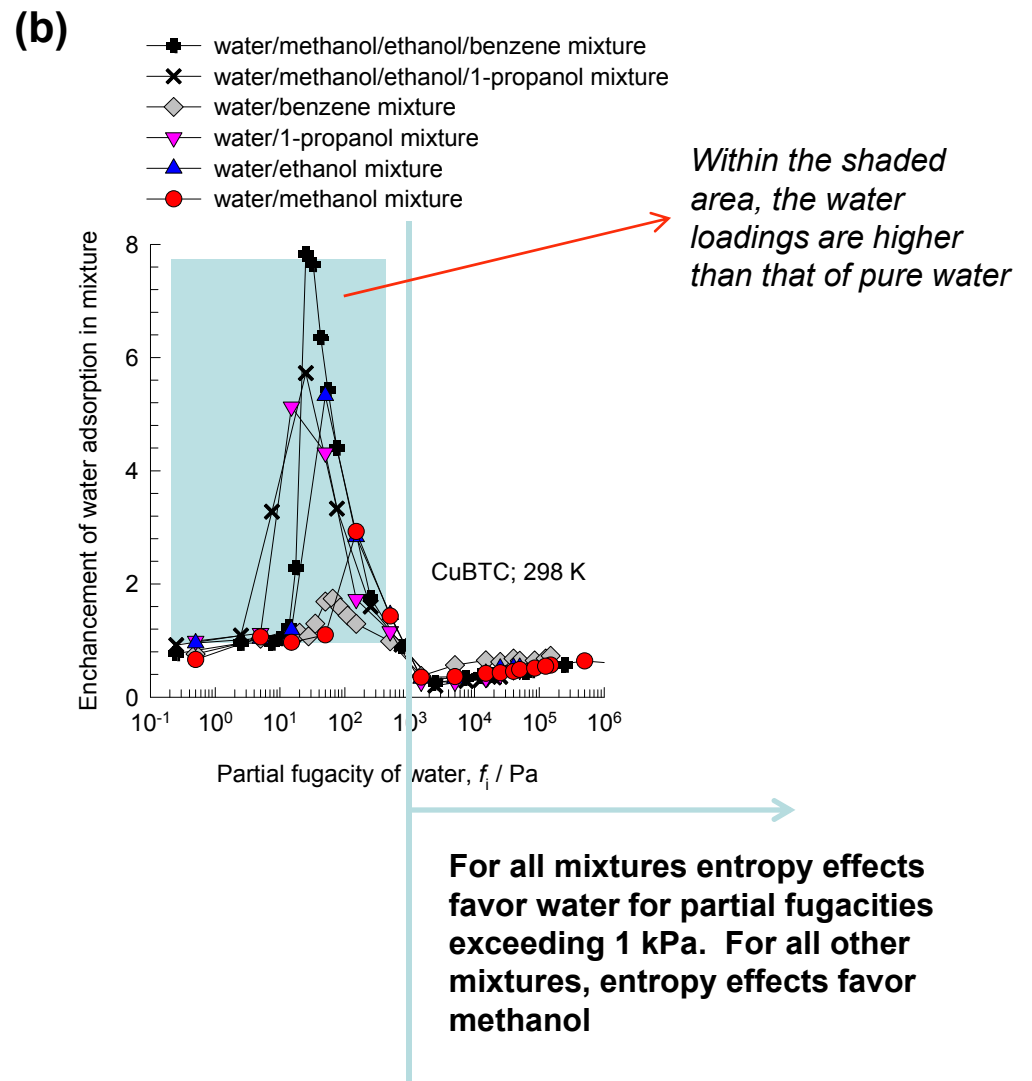
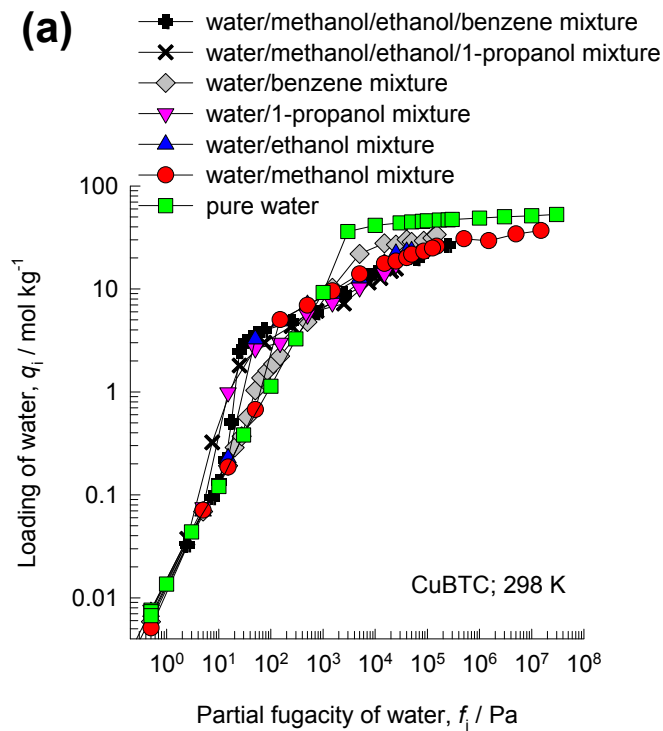


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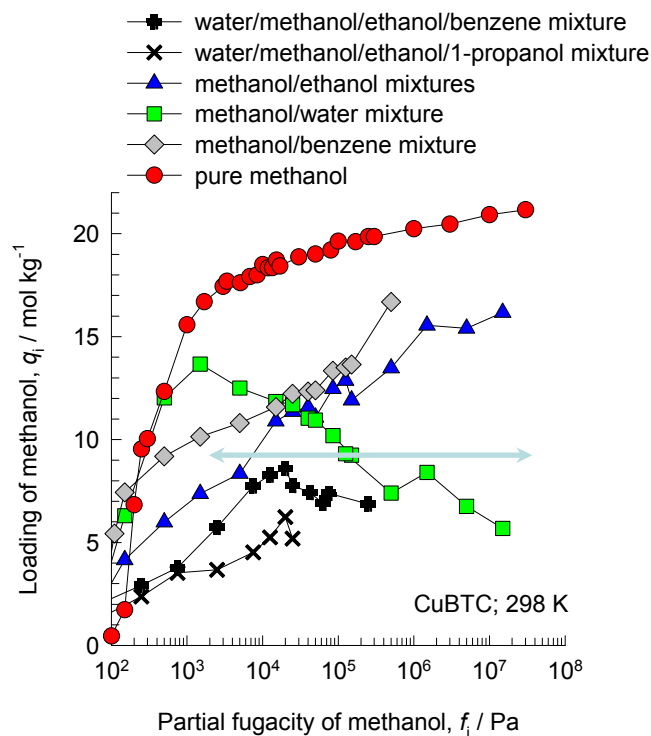
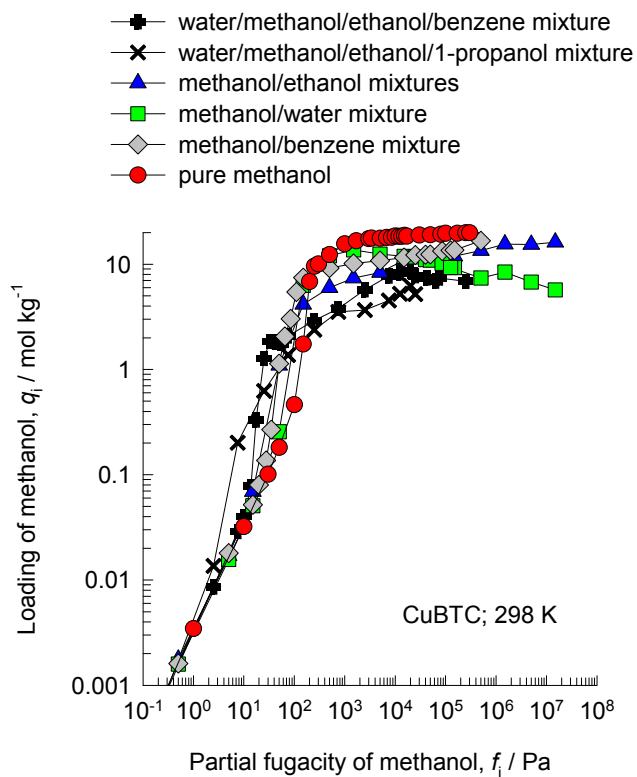
Figure ESI 16



Entropy effects: water adsorption in mixtures Figure ESI 17

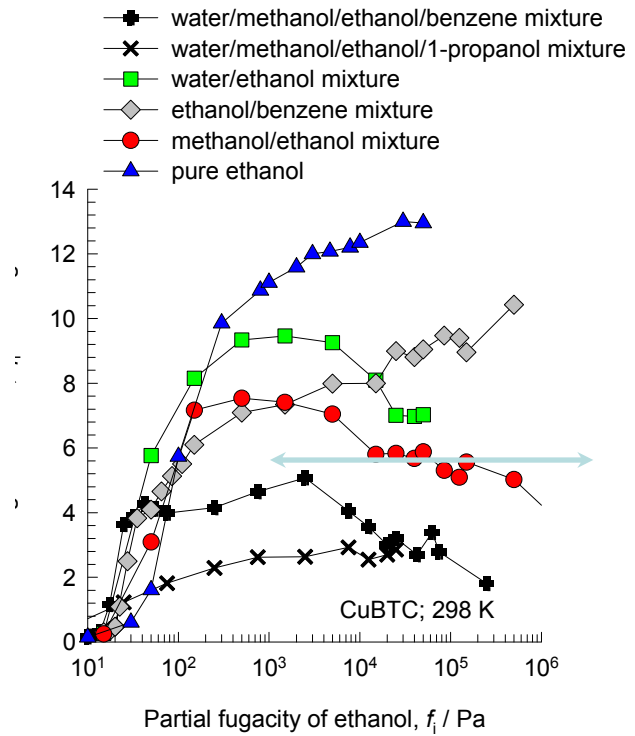
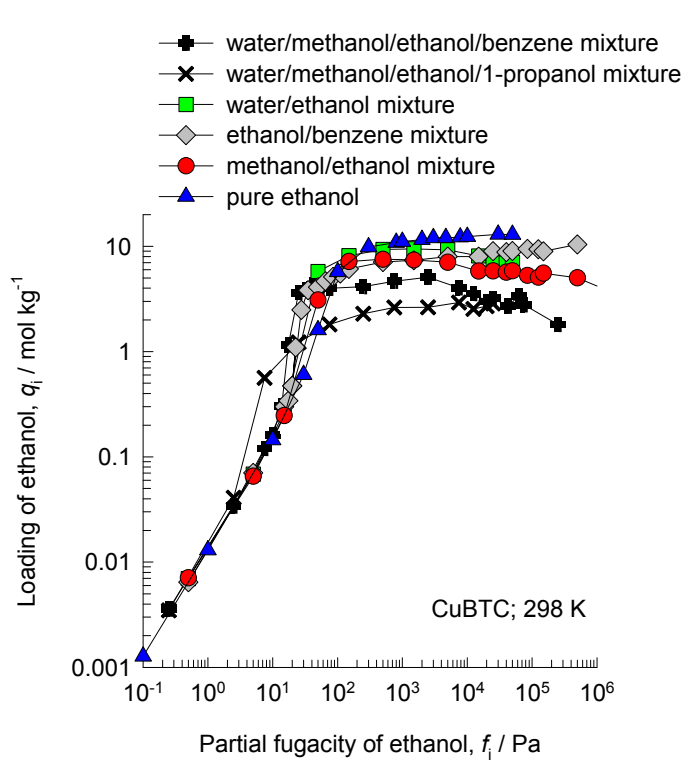


Entropy effects: methanol adsorption in mixtures Figure ESI 18



**For water/methanol mixtures
 entropy effects favor water. For
 all other mixtures, entropy
 effects favor methanol**

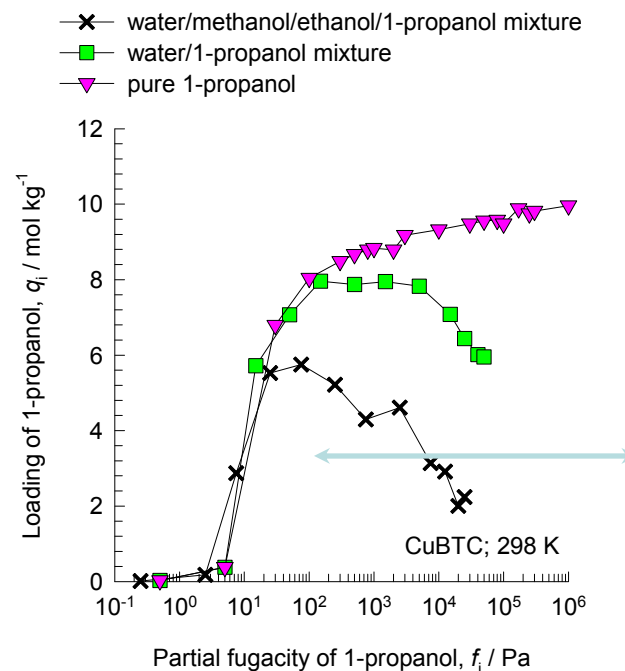
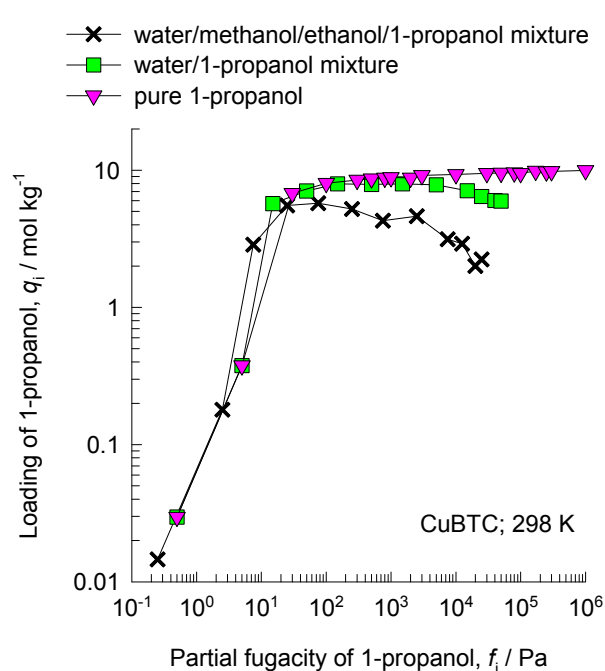
Entropy effects: ethanol adsorption in mixtures



Except for ethanol/benzene mixtures, in this range of partial fugacities, entropy effects cause the ethanol loading in the mixture to reduce in favor of partner molecules

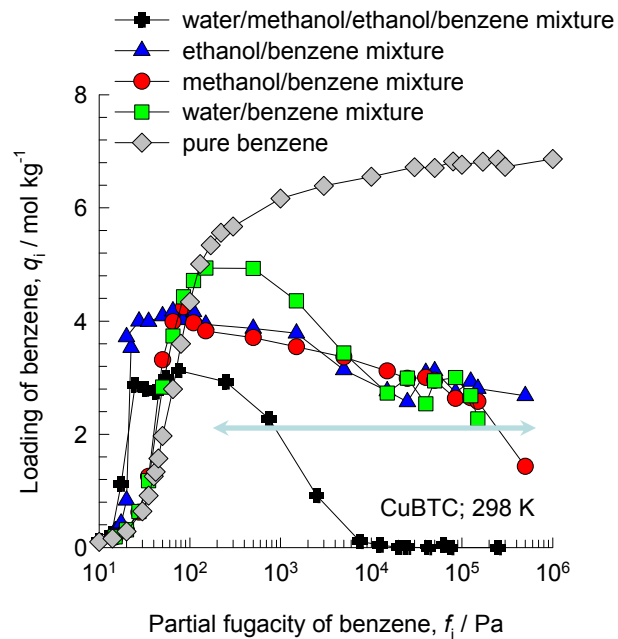
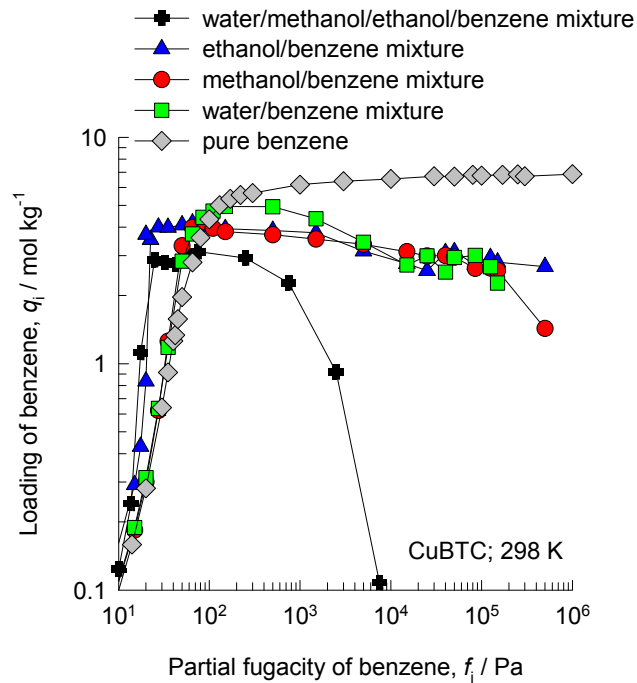
Entropy effects: 1-propanol adsorption in mixtures

Figure ESI 20



In this range of partial fugacities, entropy effects cause the 1-propanol loading in the mixture to reduce in favor of partner molecules

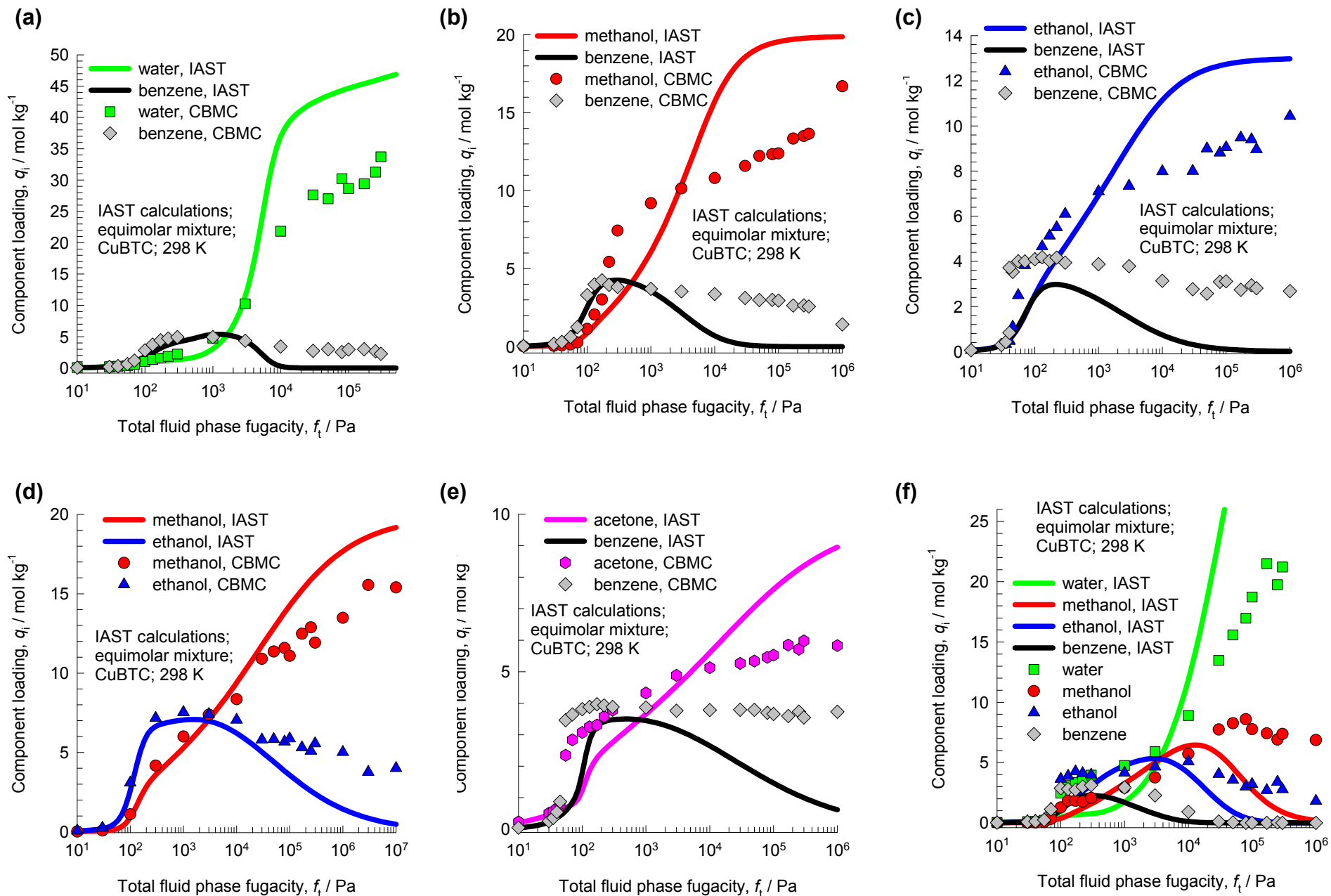
Entropy effects: benzene adsorption in mixtures



**In this range of partial fugacities,
 entropy effects cause the
 benzene loading in the mixture
 to reduce in favor of partner
 molecules**

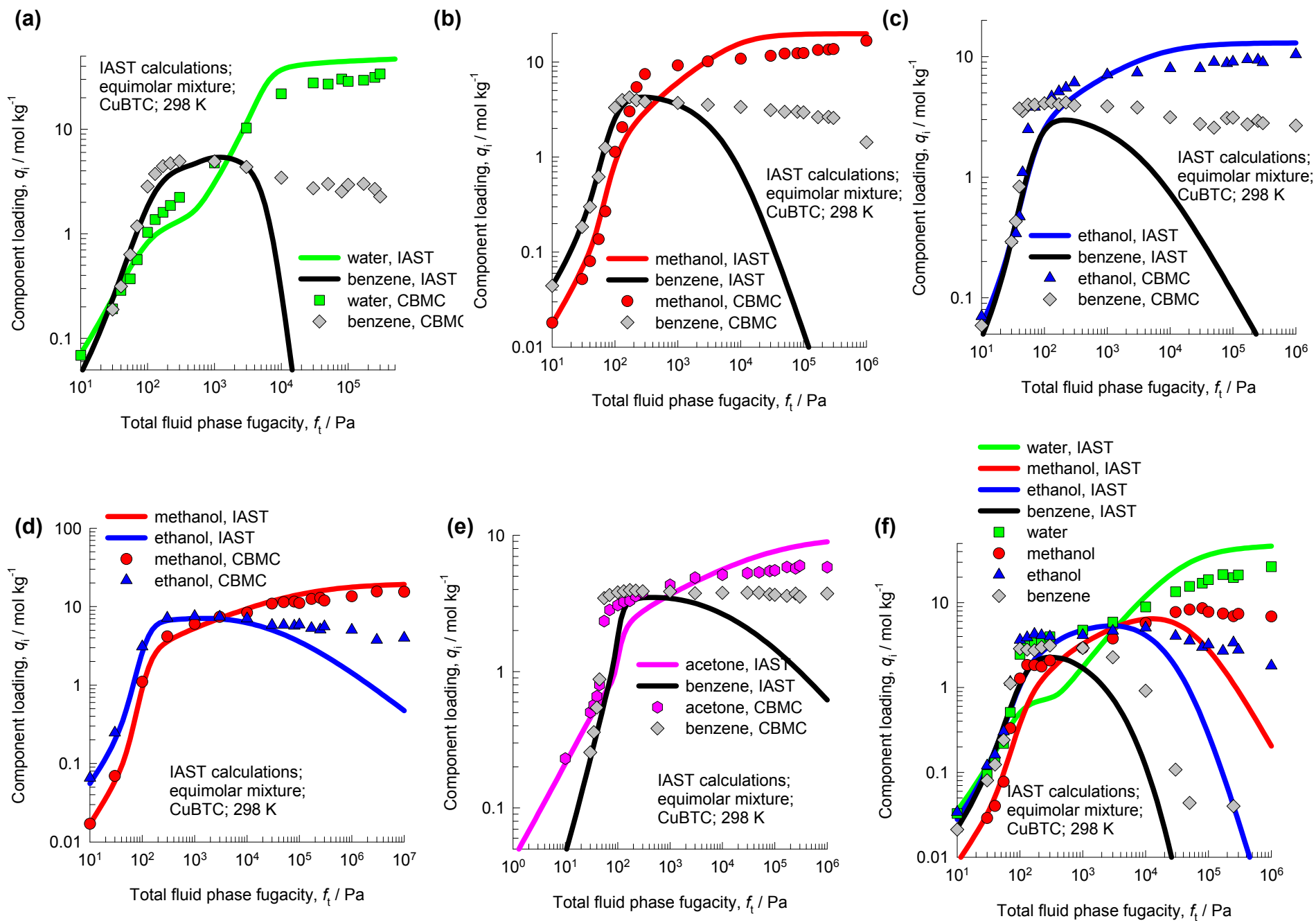
IAST vs CBMC mixture

Figure ESI 22



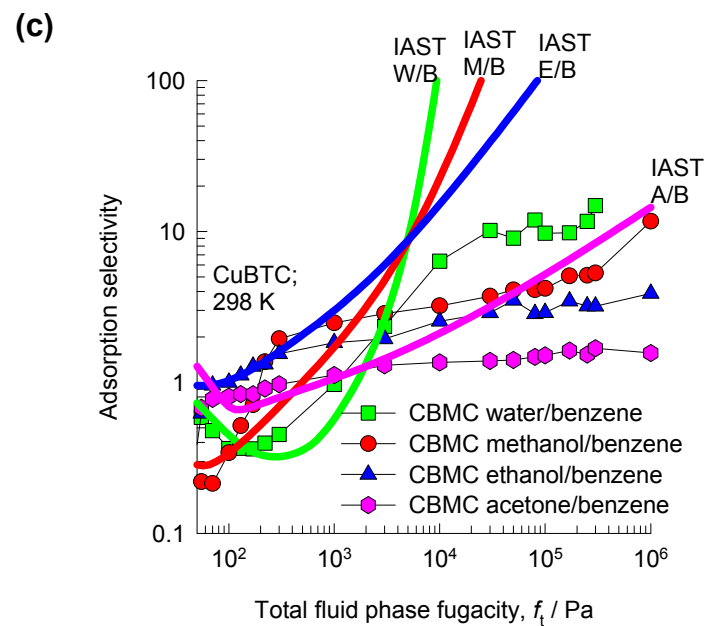
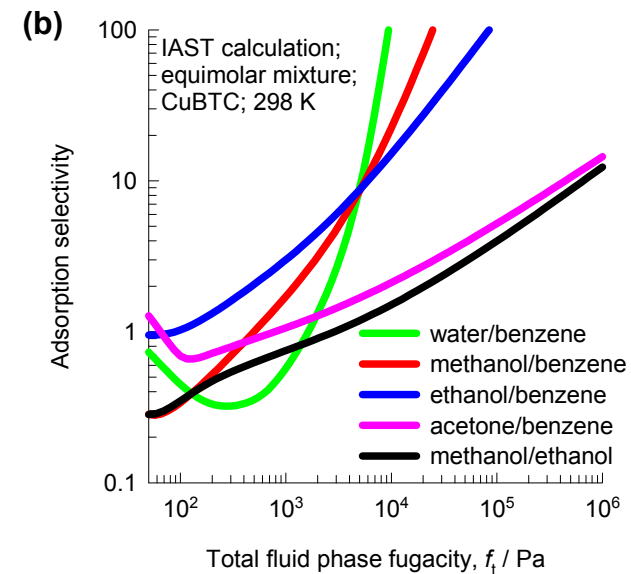
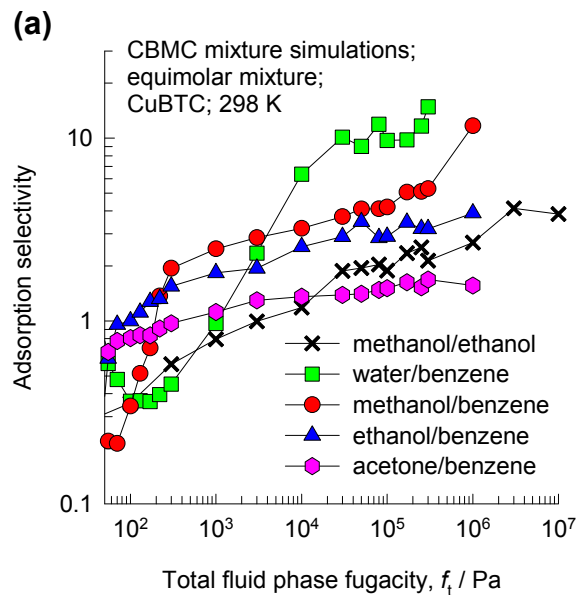
IAST vs CBMC mixture

Figure ESI 23



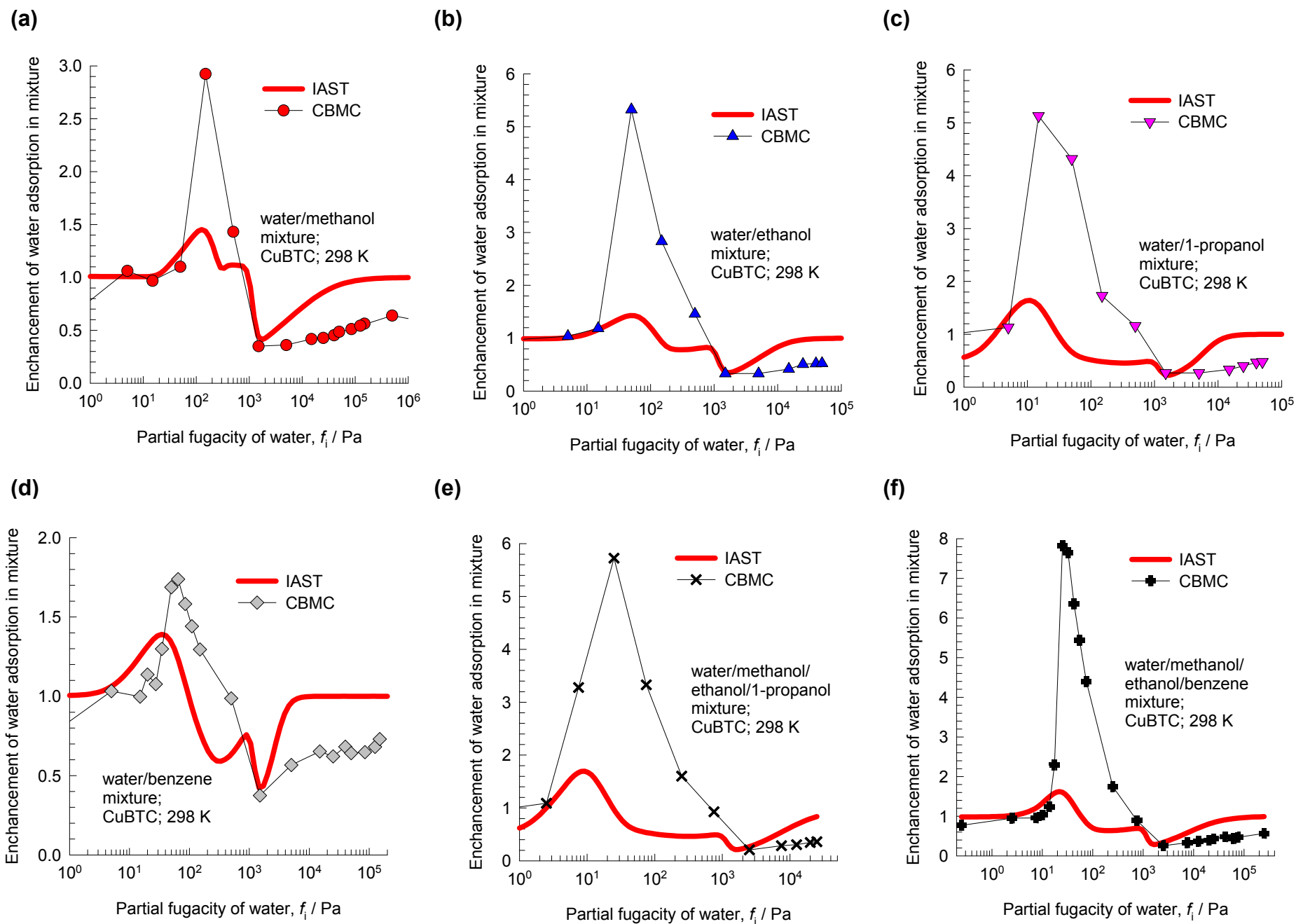
IAST vs CBMC mixture

Figure ESI 24

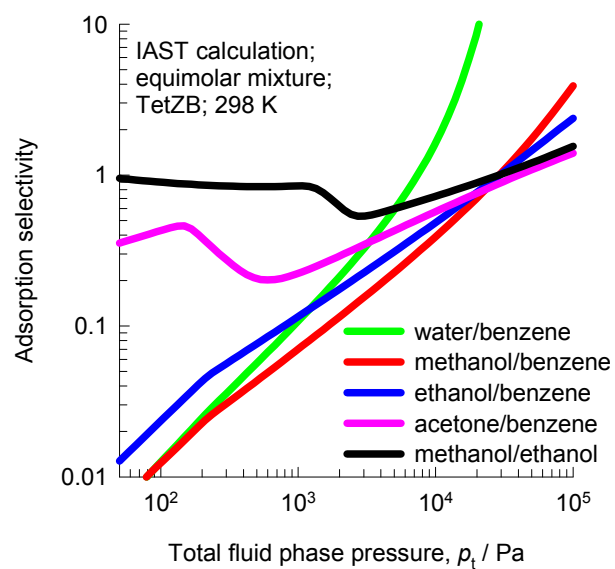


IAST vs CBMC mixture

Figure ESI 25

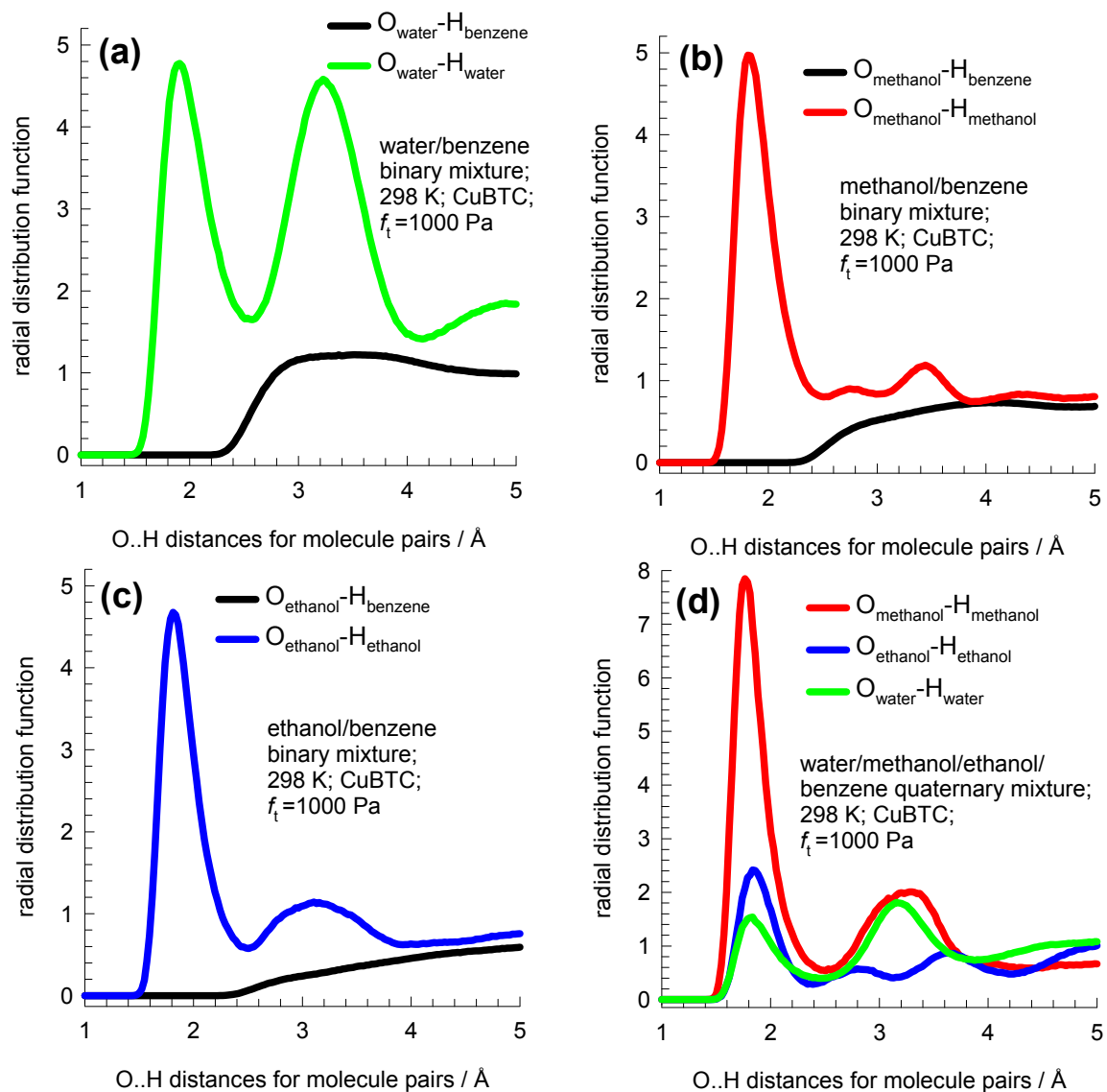


Adsorption selectivities with TetZB



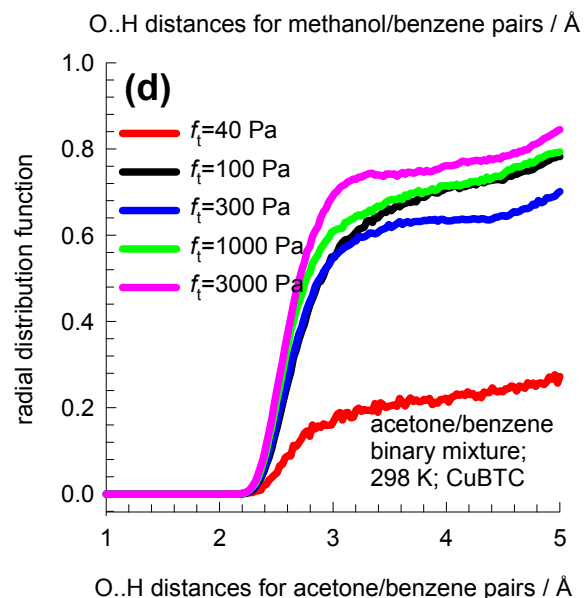
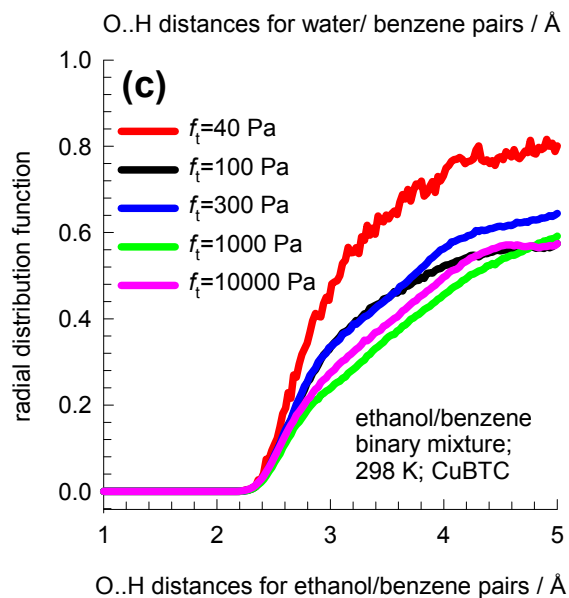
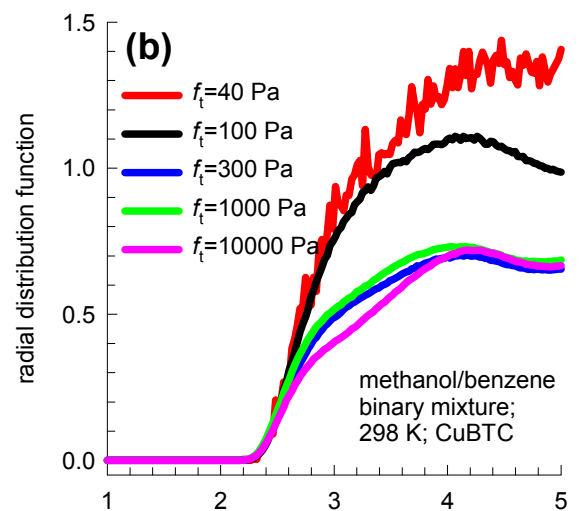
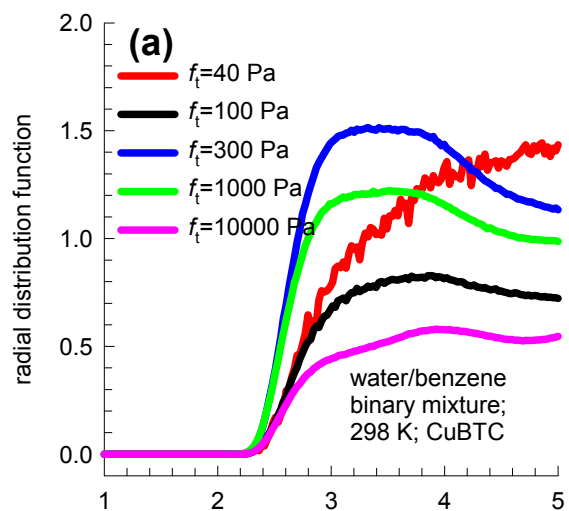
RDF

Figure ESI 27

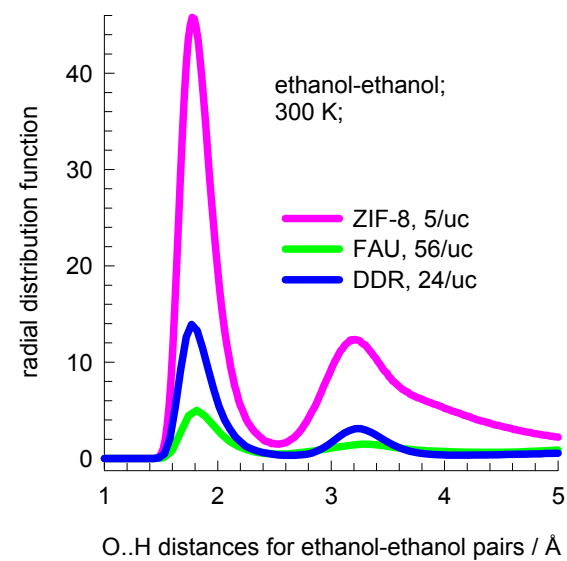
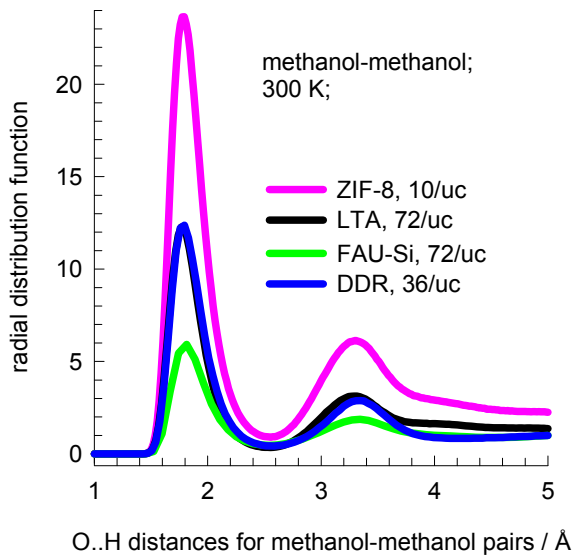
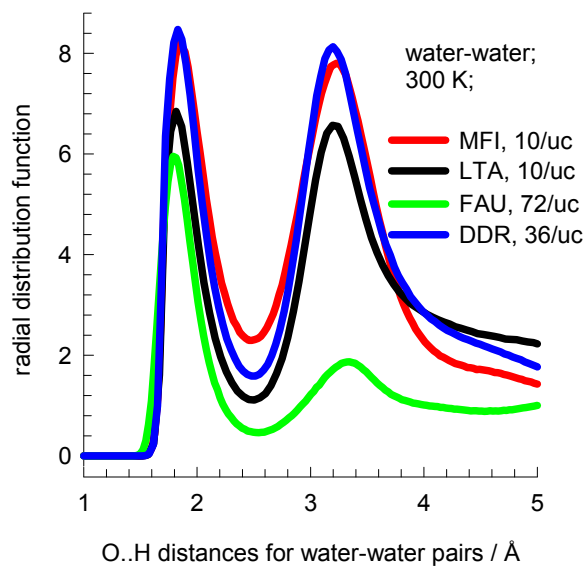


RDF

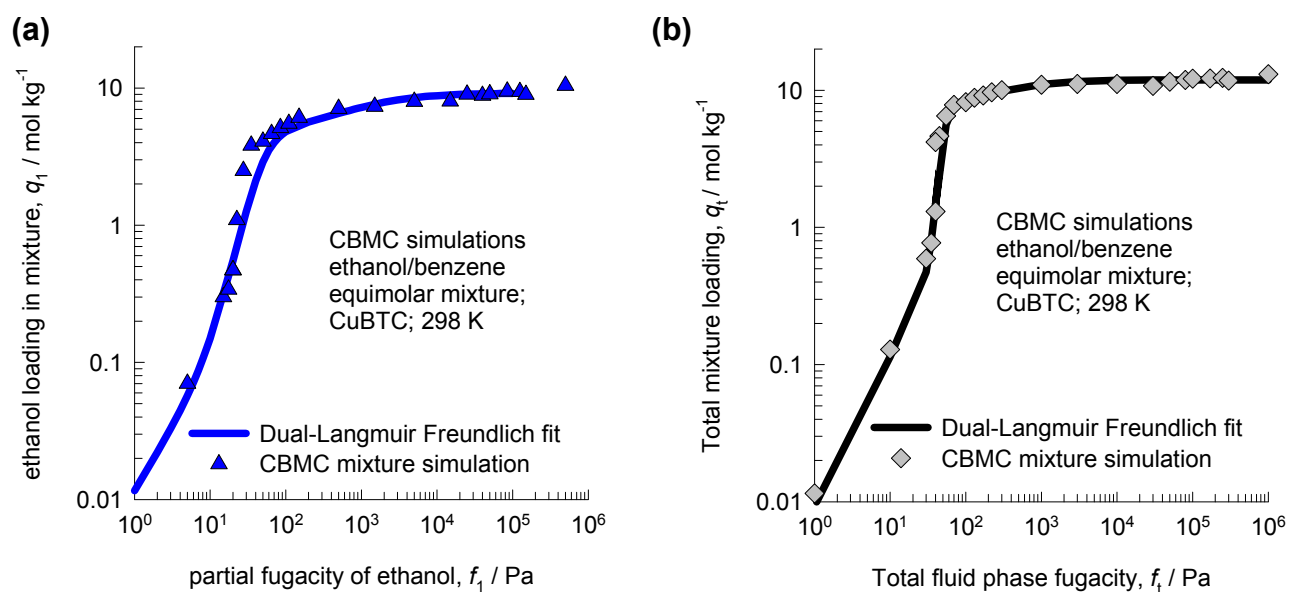
Figure ESI 28



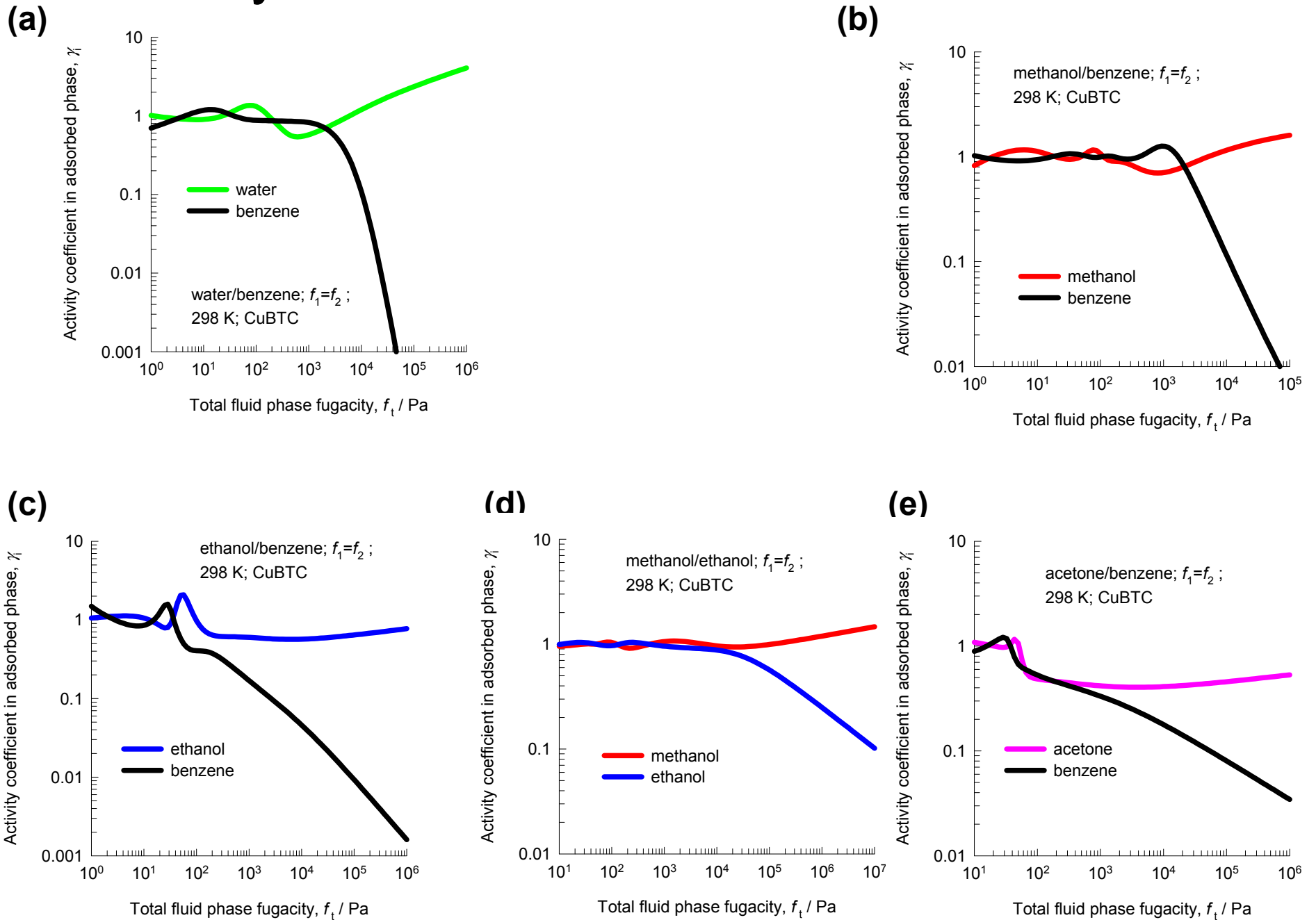
RDF



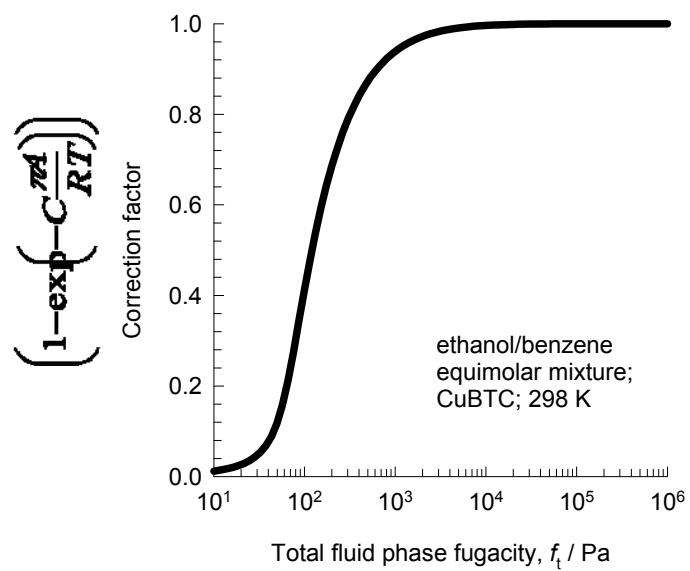
Fitting of CBMC mixture simulation data Figure ESI 30



Activity coefficients: Numerical calculations

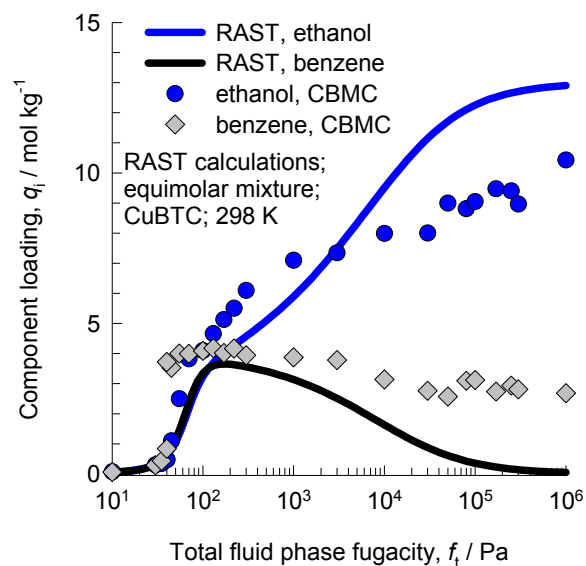


Correction factor

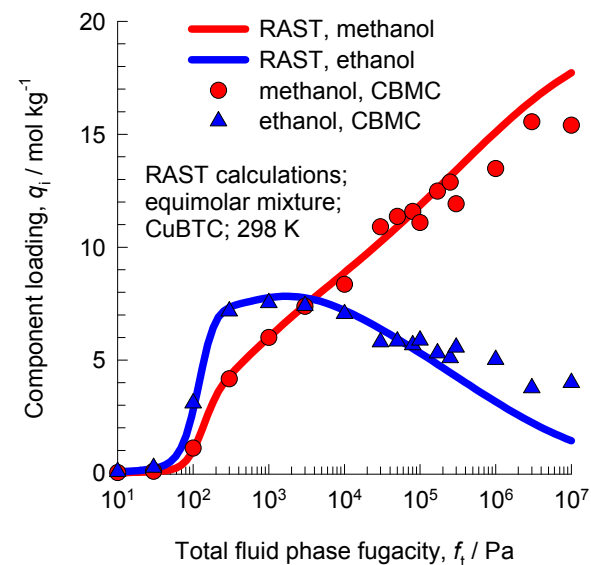


RAST vs CBMC mixture

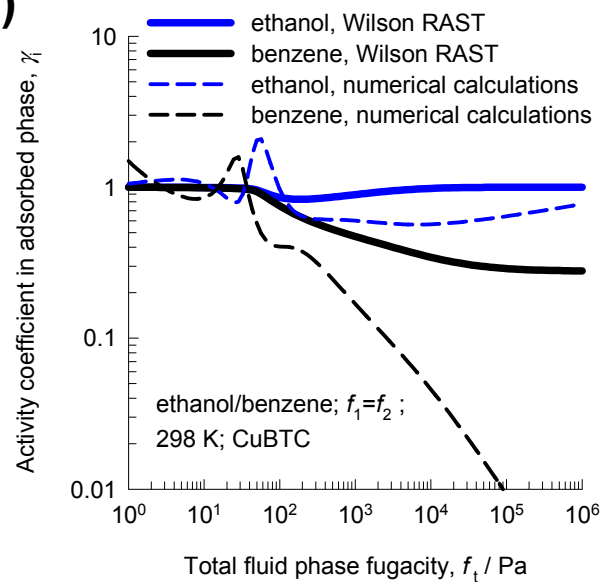
(a)



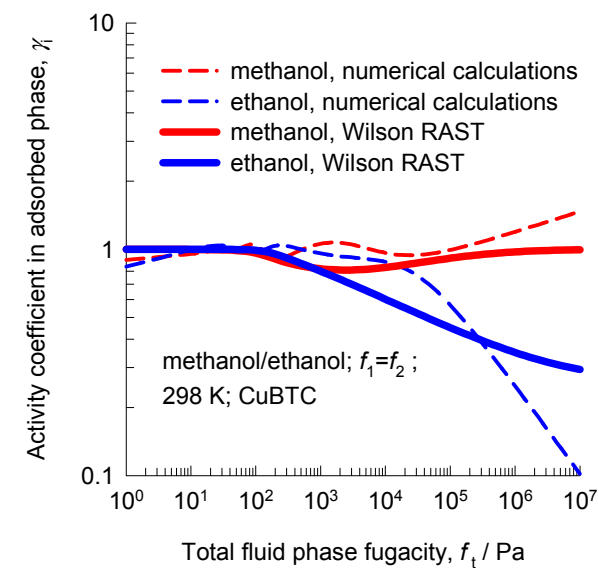
(b)



(c)

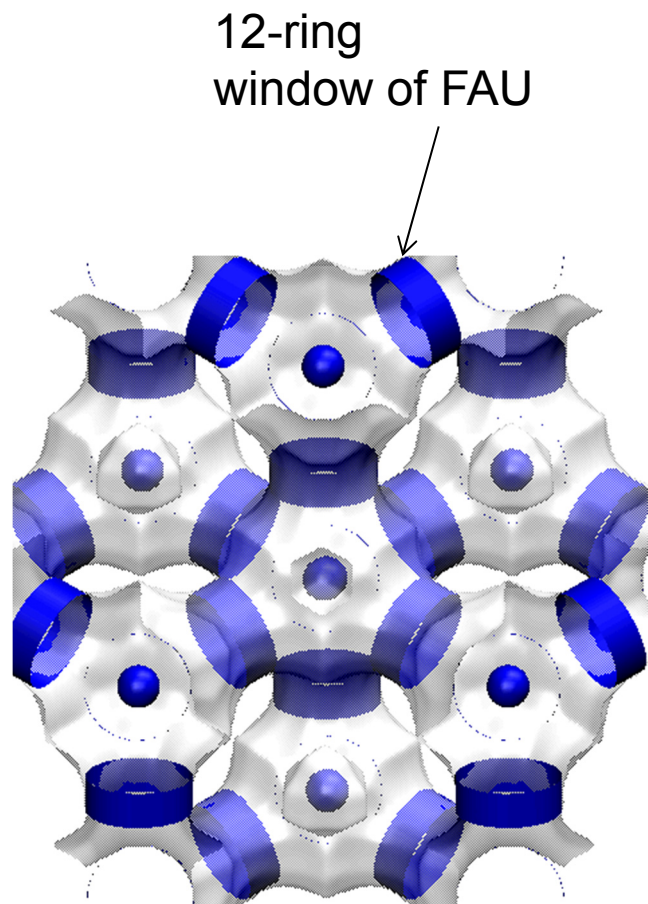


(d)

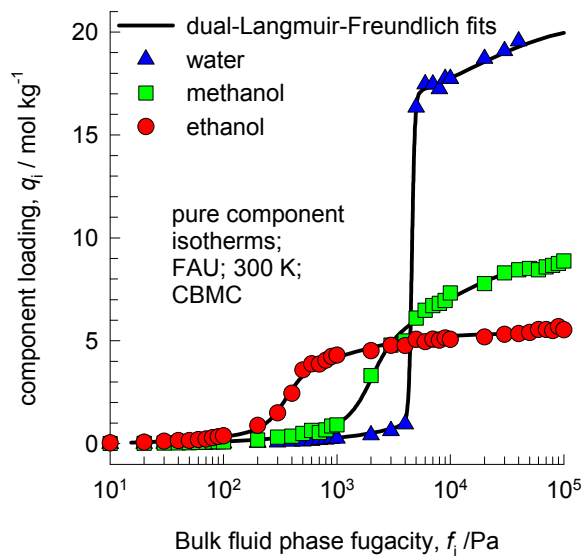


Water, methanol, ethanol unary isotherms in FAU

Figure ESI 34

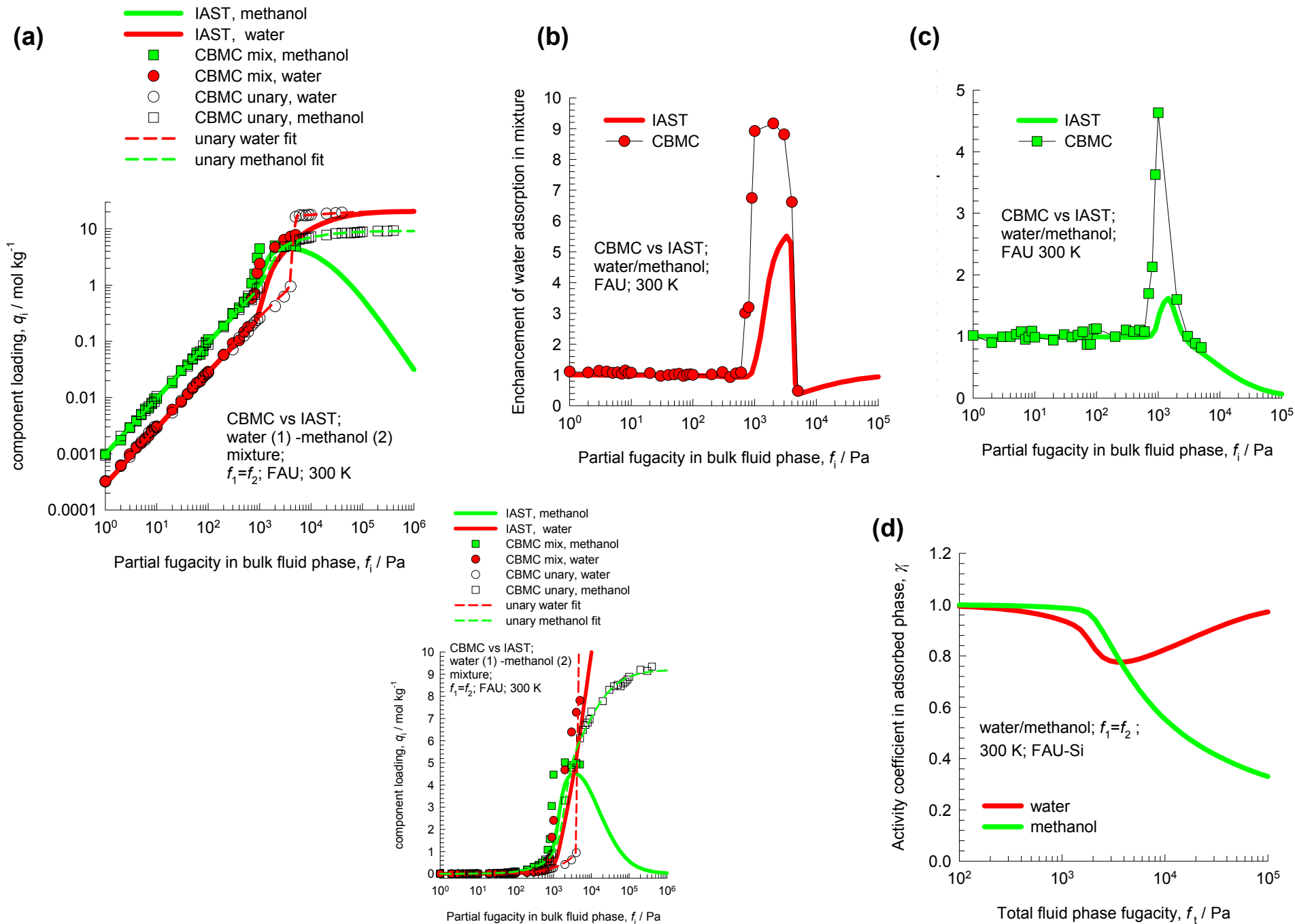


There are 8 cages per unit cell.
The volume of one FAU cage is 786 \AA^3 , larger in size than that of CHA (316.4 \AA^3) and DDR (278 \AA^3).



Water/methanol mixture adsorption in FAU

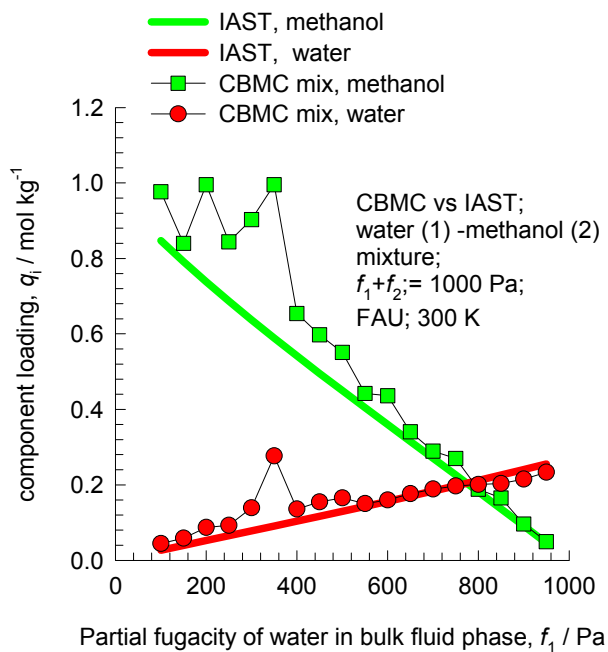
Figure ESI 35



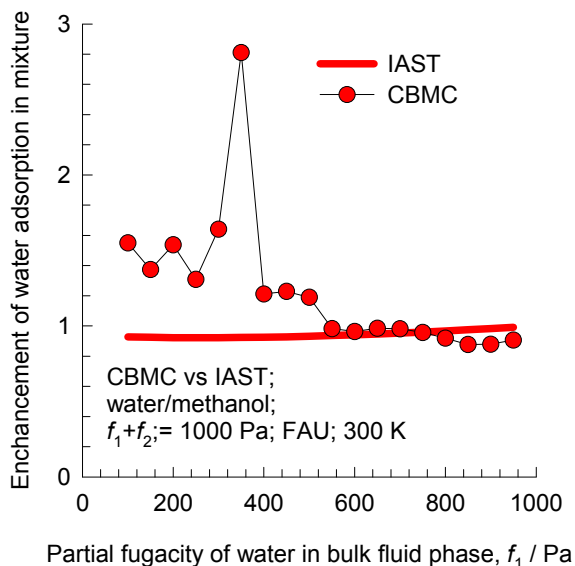
Water/methanol mixture adsorption in FAU

Figure ESI 36

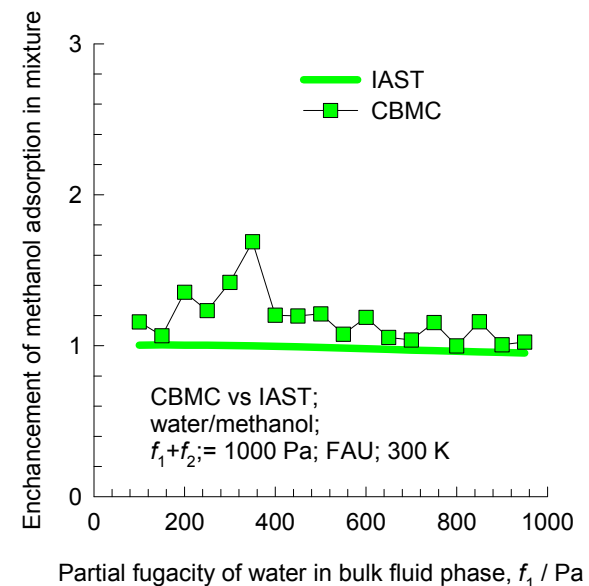
(a)



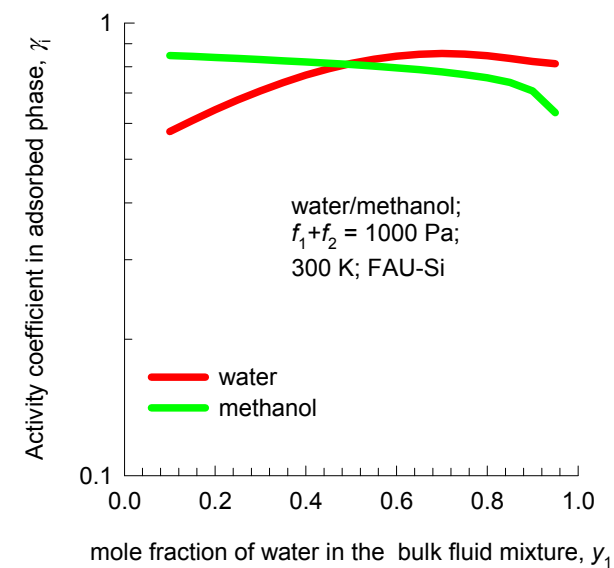
(b)



(c)

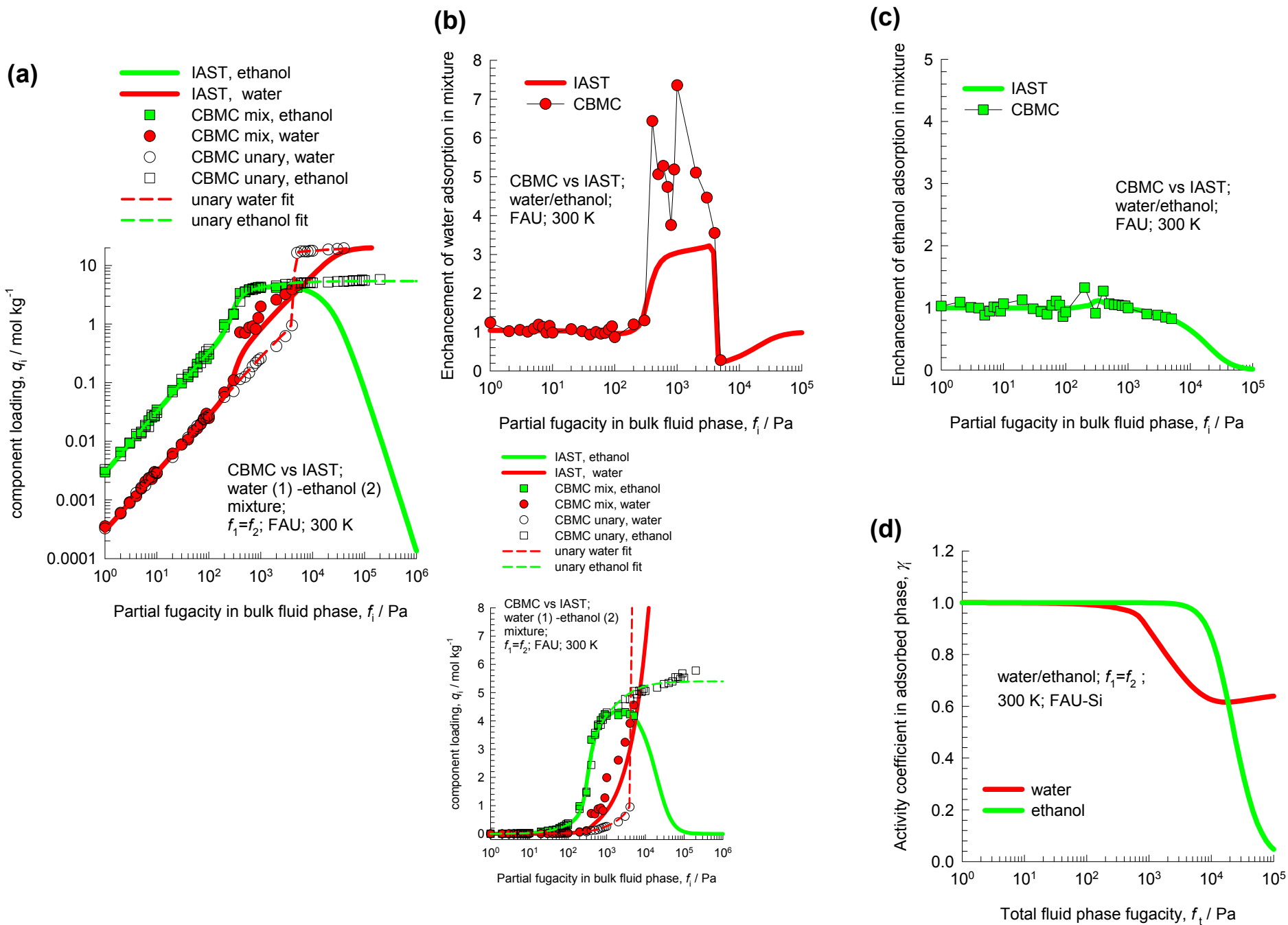


(d)



Water/ethanol mixture adsorption in FAU

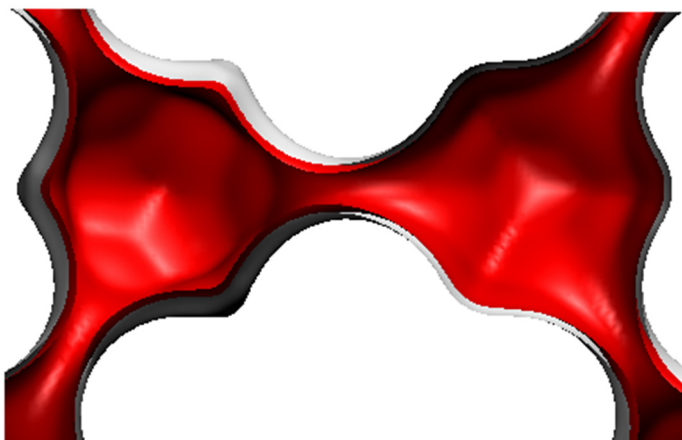
Figure ESI 37



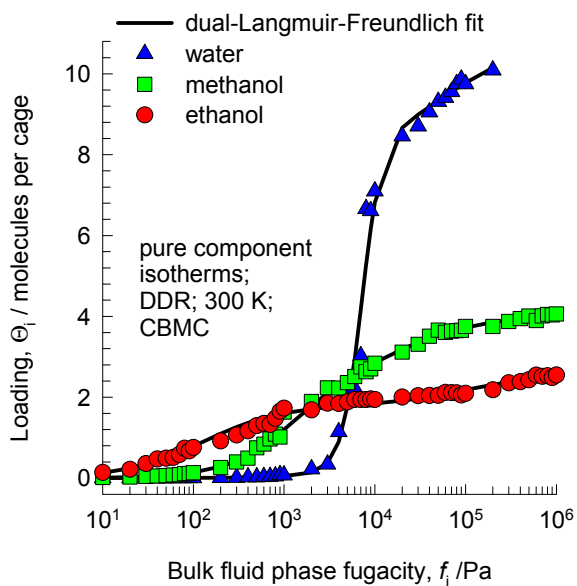
Water, methanol, ethanol unary isotherms in DDR

Figure ESI 38

There are 12 cages per unit cell.
The volume of one DDR cage is 278 \AA^3 , significantly smaller than that of a single cage of FAU (786 \AA^3), or ZIF-8 (1168 \AA^3).

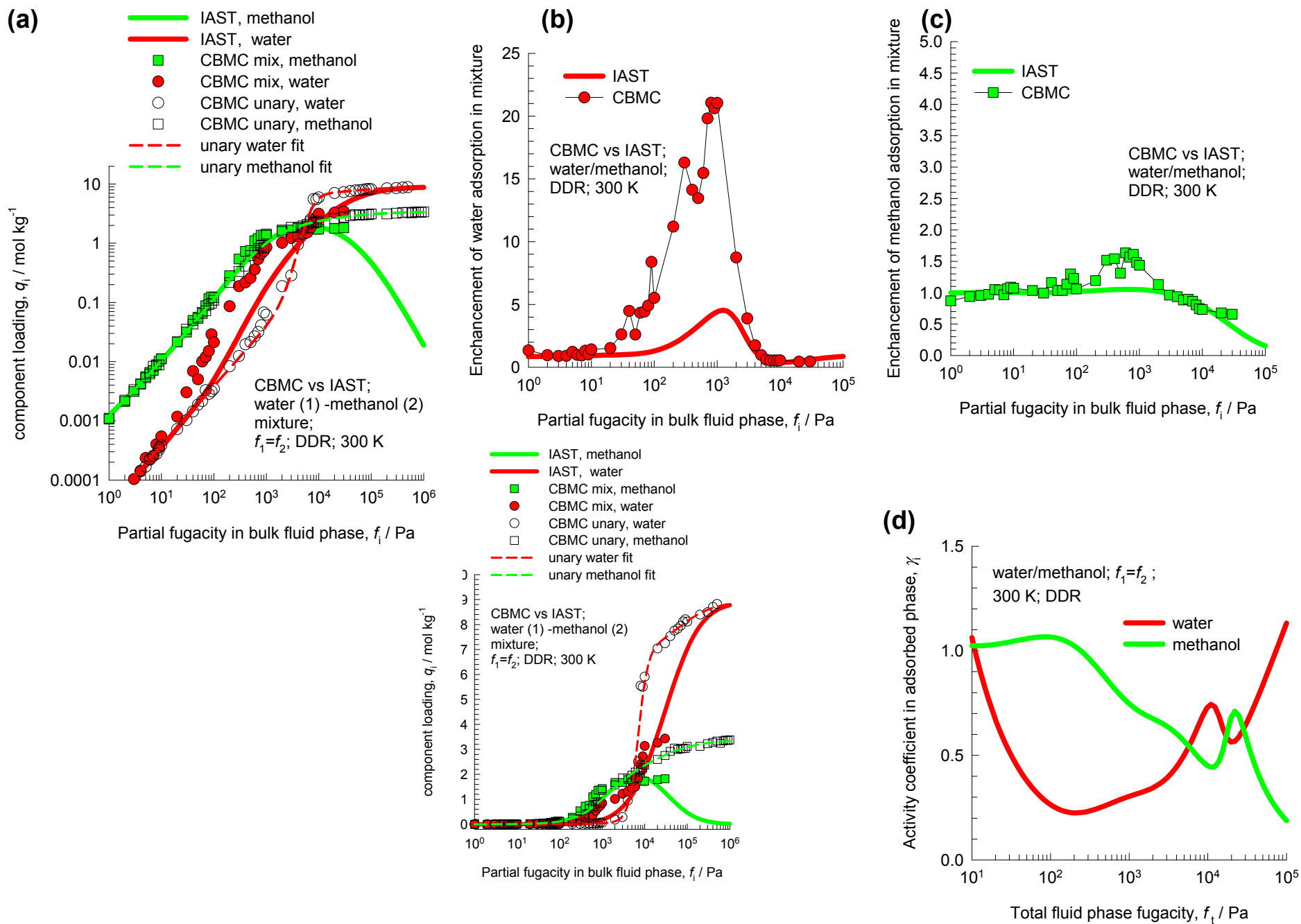


The volume of one DDR cage is 278 \AA^3 , significantly smaller than that of a single cage of FAU (786 \AA^3), or ZIF-8 (1168 \AA^3).



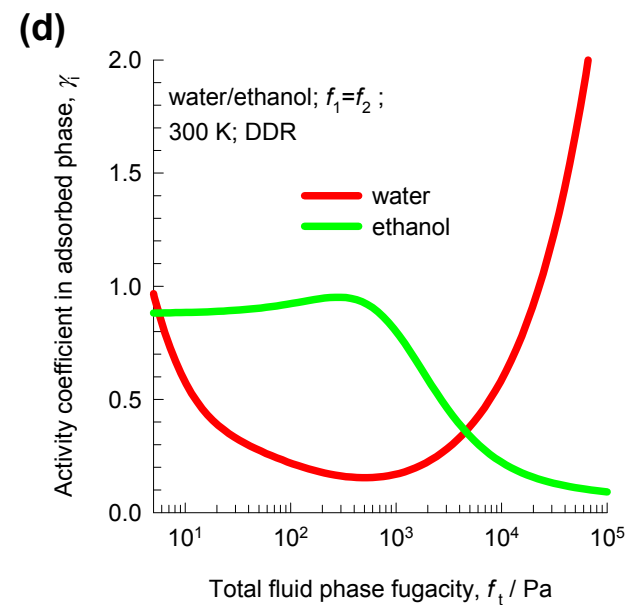
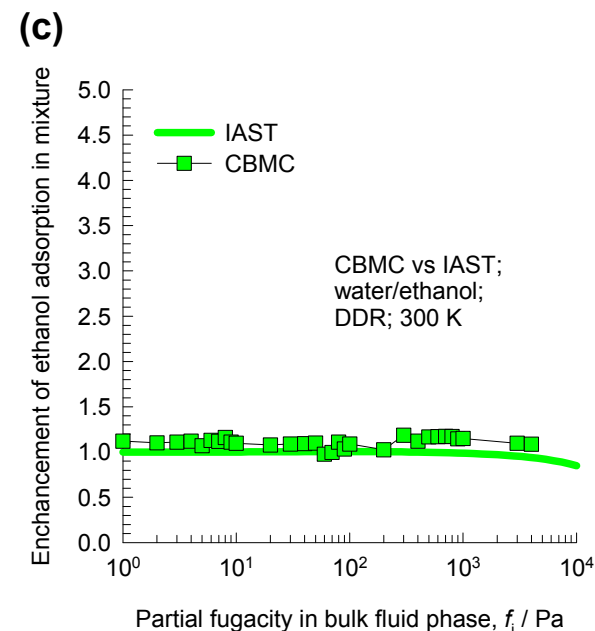
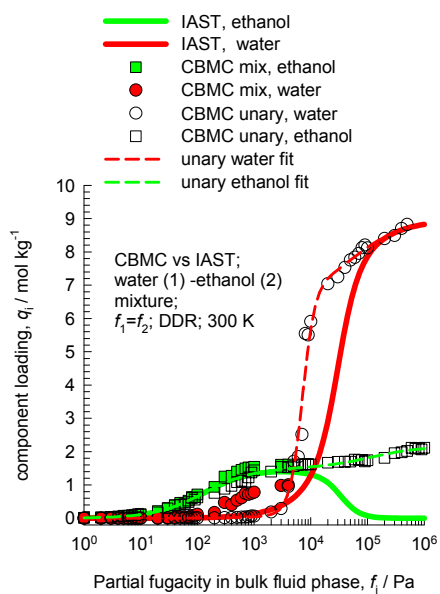
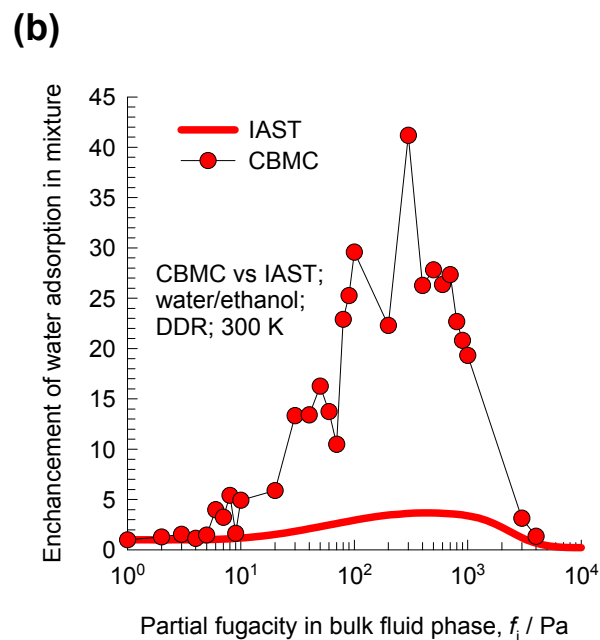
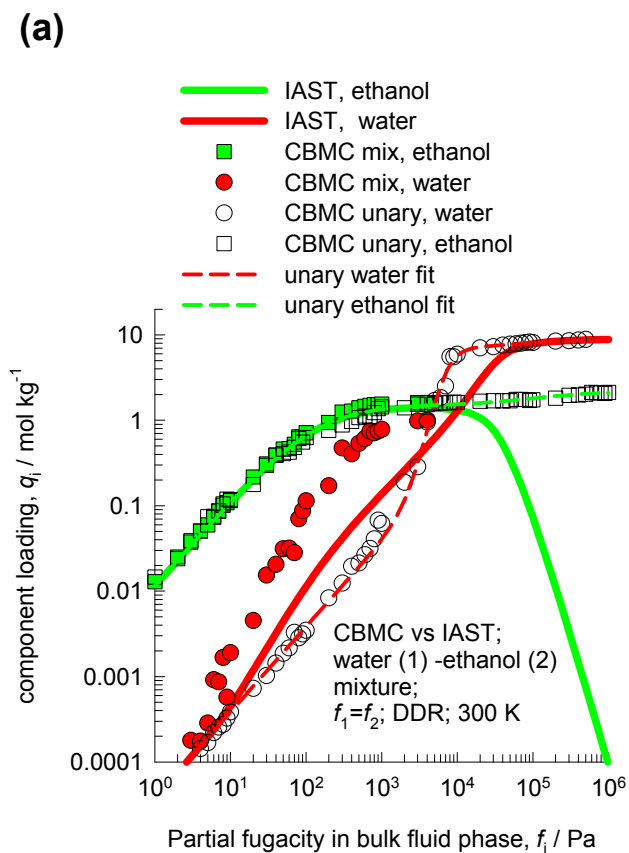
Water/methanol mixture adsorption in DDR

Figure ESI 39



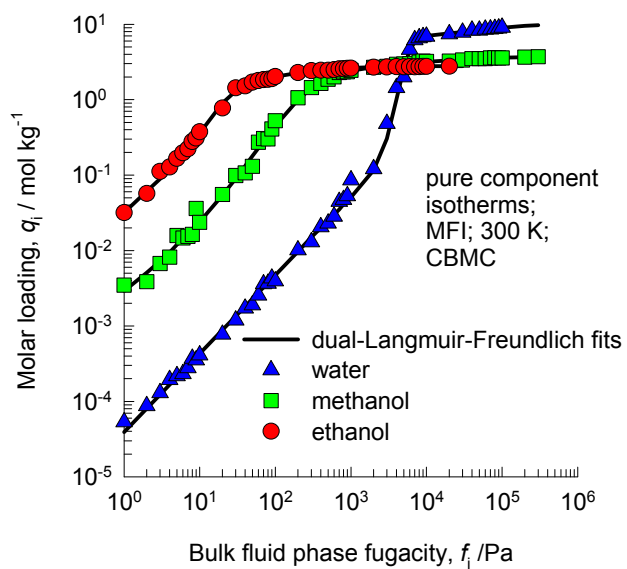
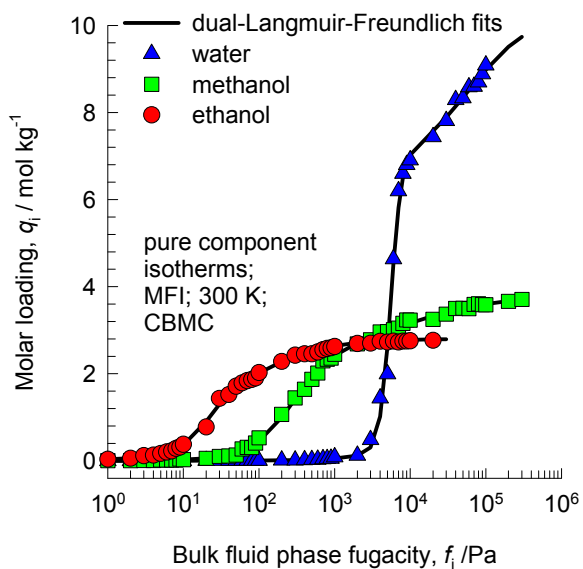
Water/ethanol mixture adsorption in DDR

Figure ESI 40



Water, methanol, ethanol isotherms in MFI

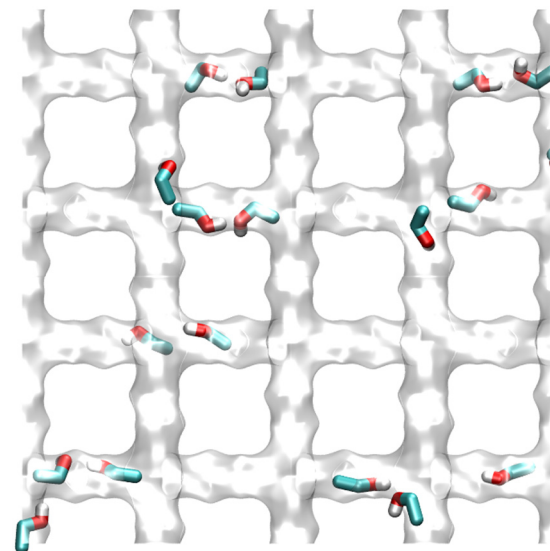
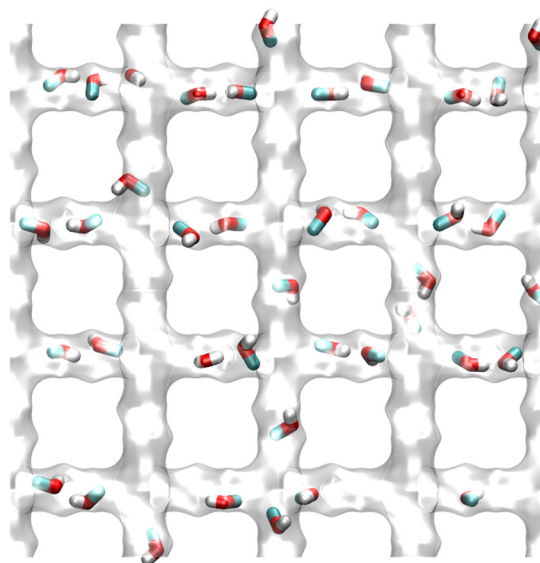
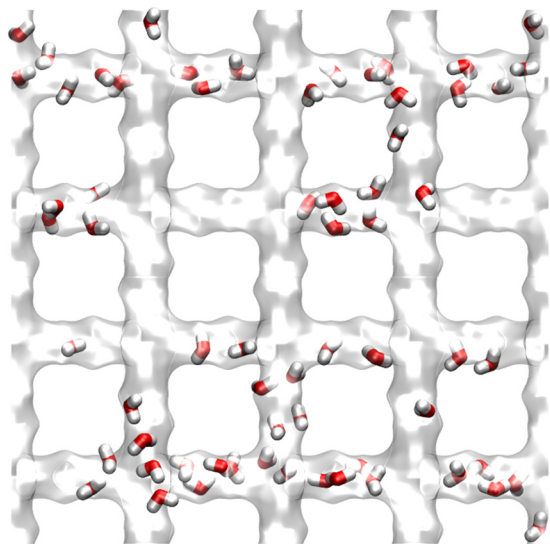
Figure ESI 41



water

methanol

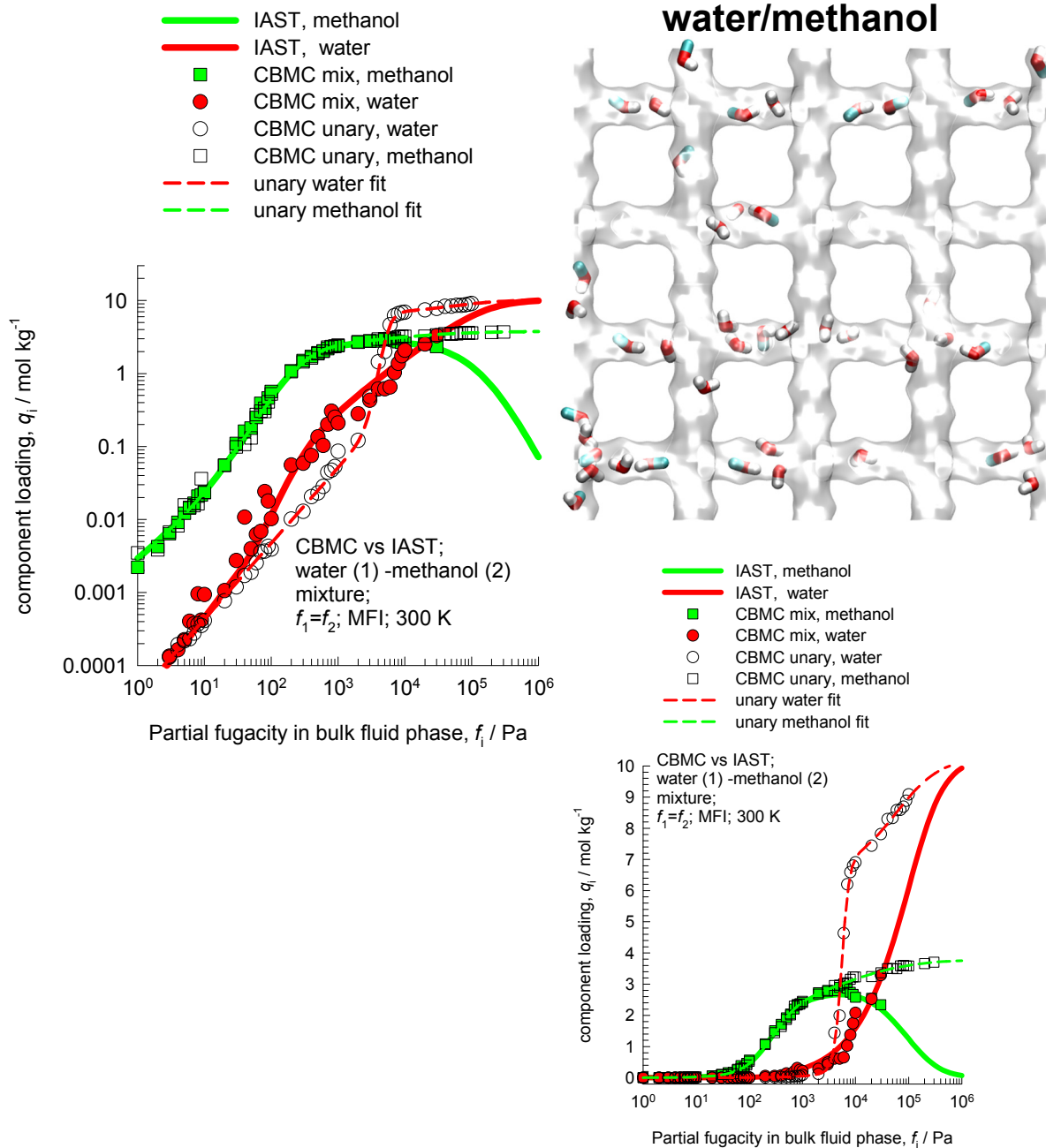
ethanol



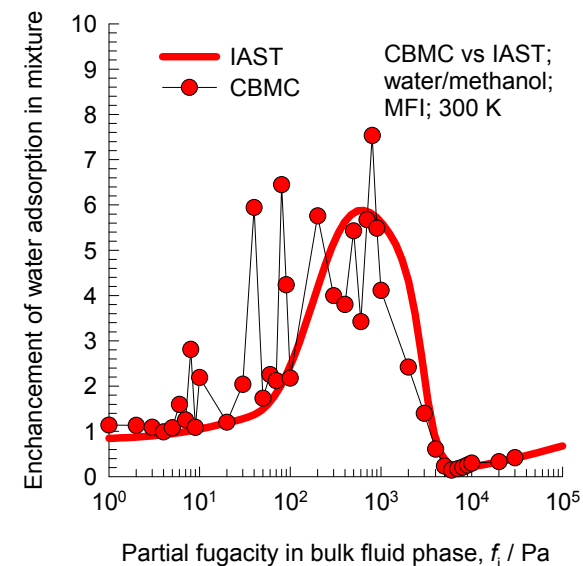
Water/methanol mixture adsorption in MFI

Figure ESI 42

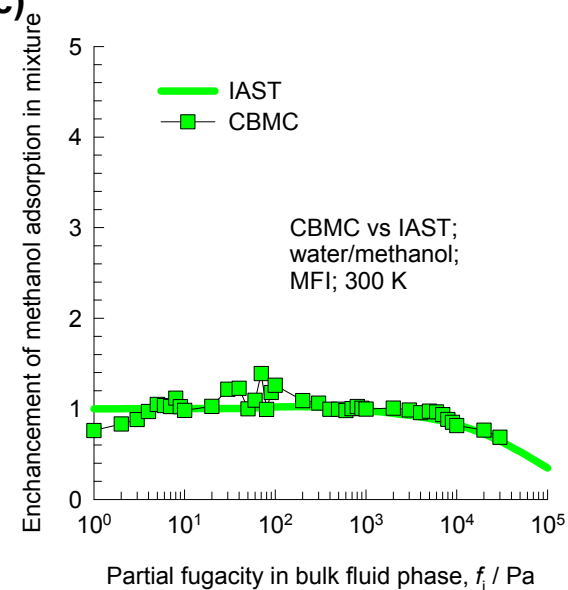
(a)



(b)



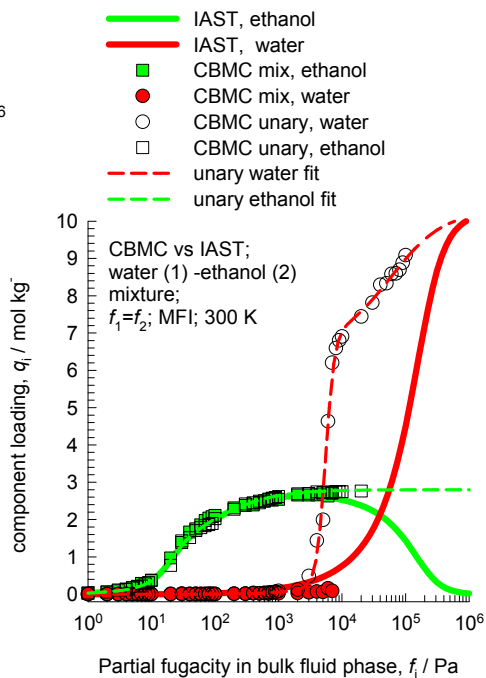
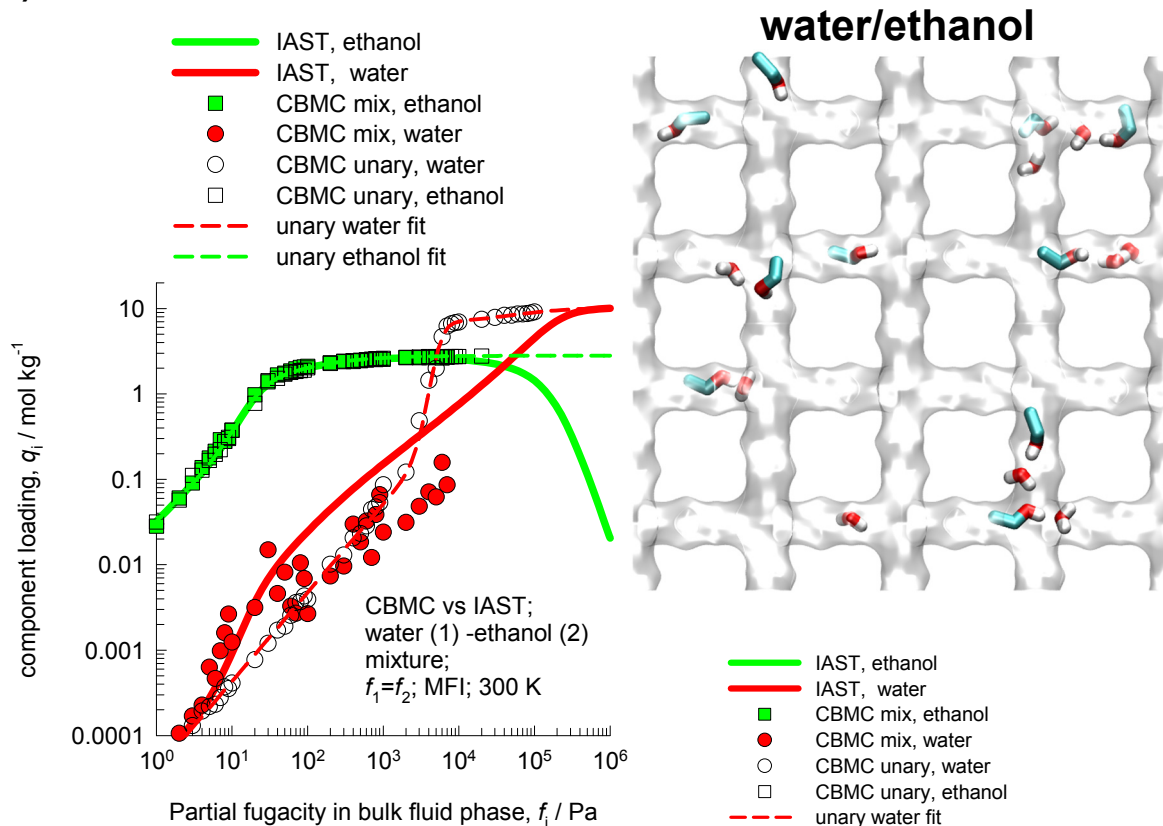
(c)



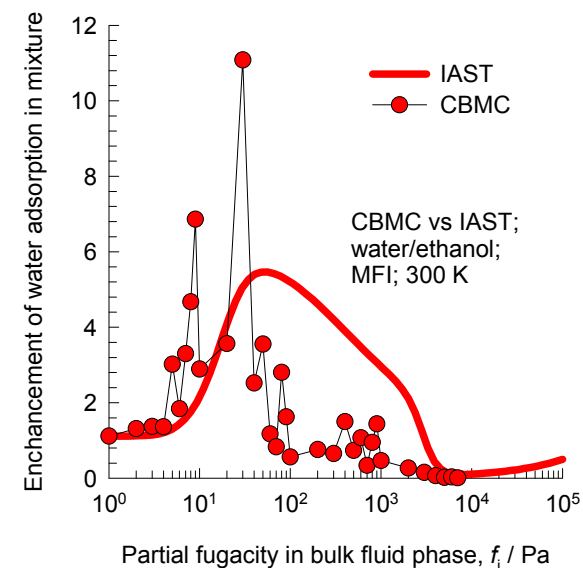
Water/ethanol mixture adsorption in MFI

Figure ESI 43

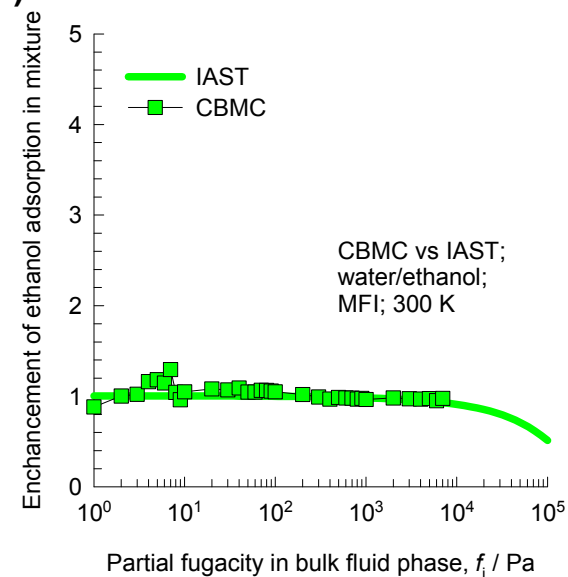
(a)

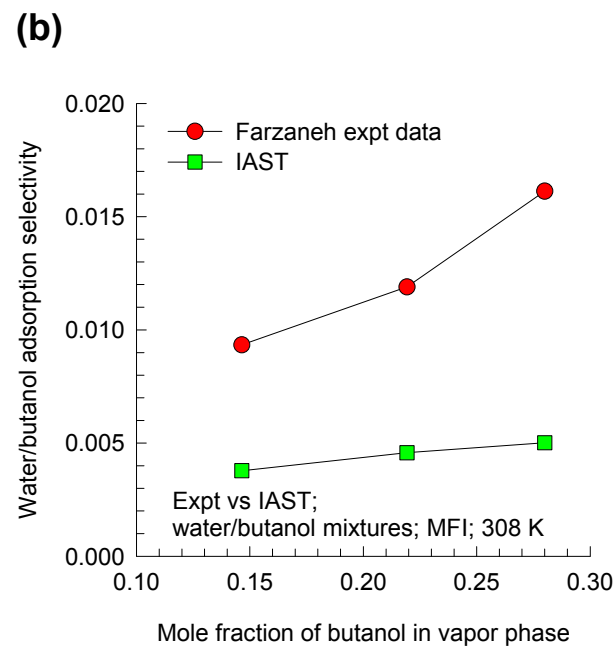
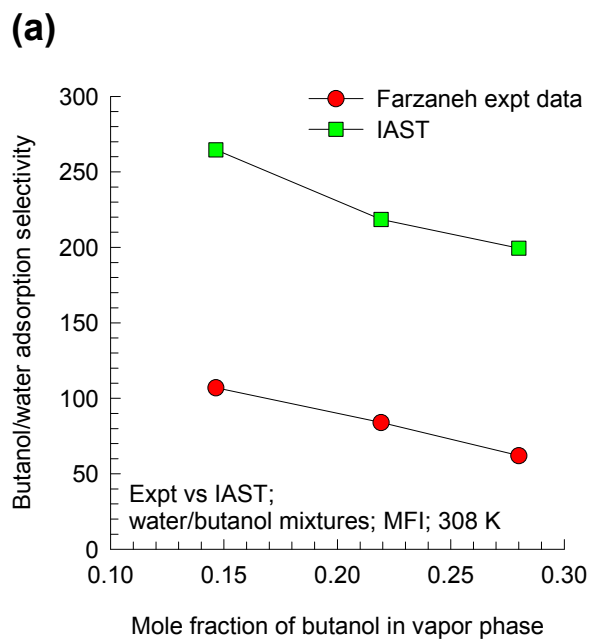


(b)



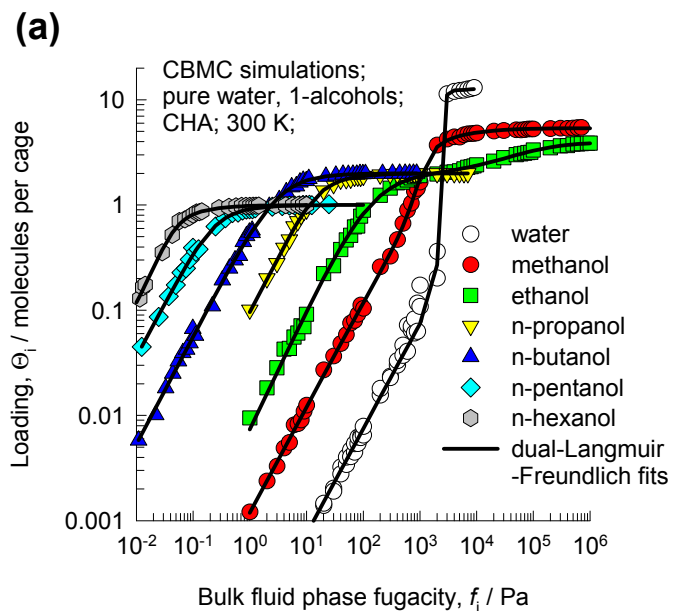
(c)





1-alcohols unary isotherms in CHA zeolite

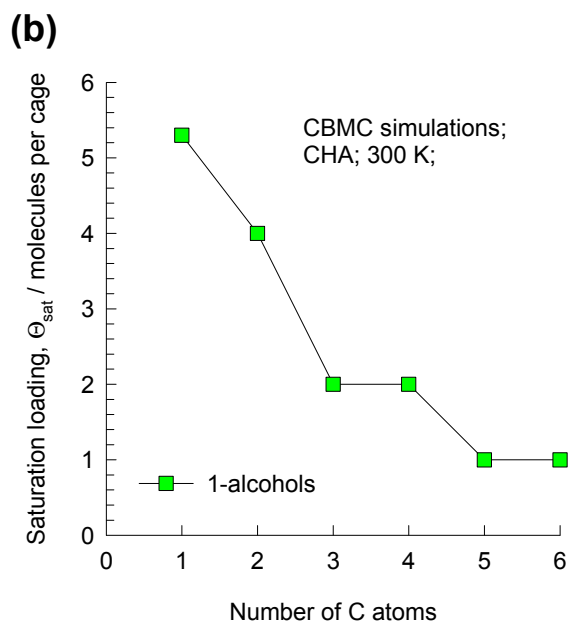
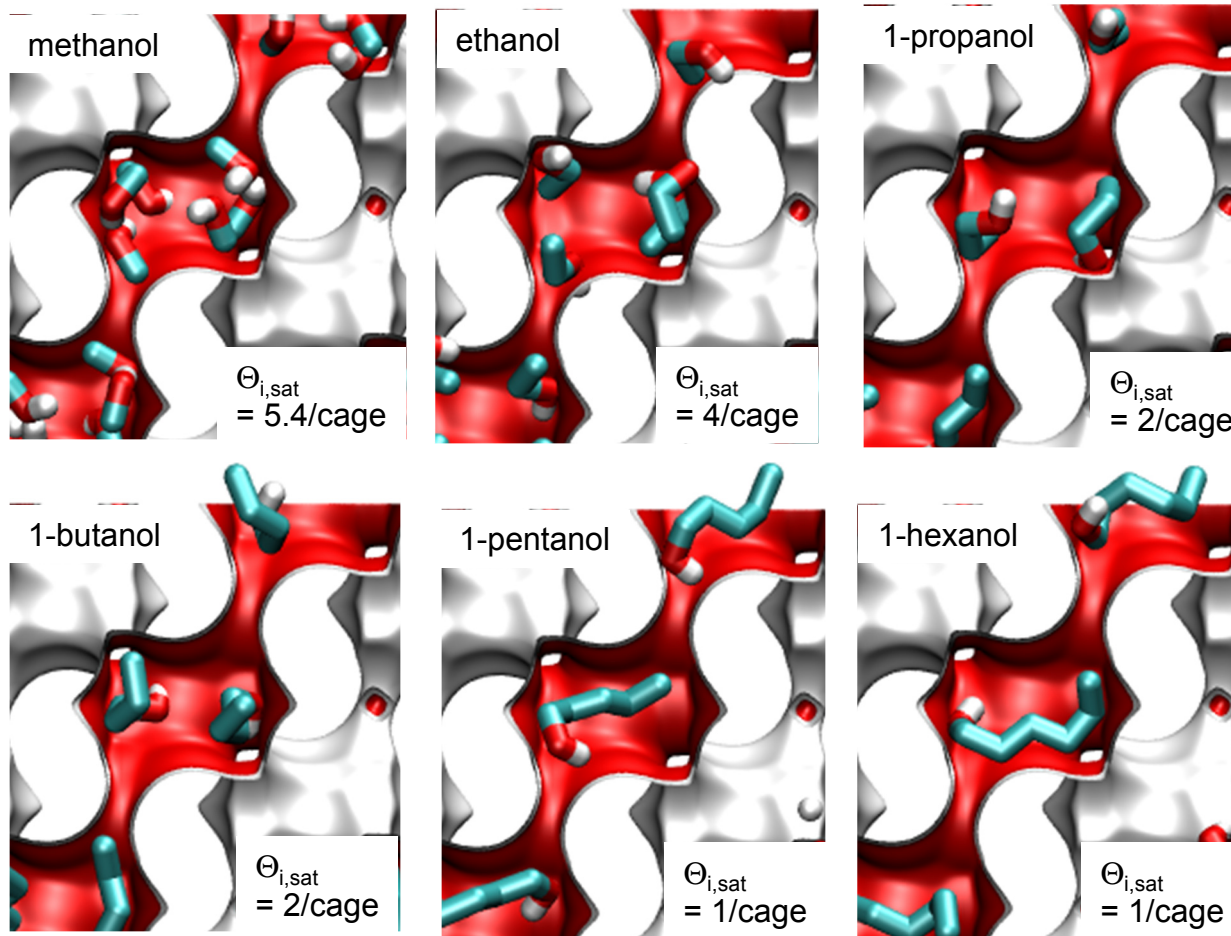
Figure ESI 45



There are 6 cages per unit cell.

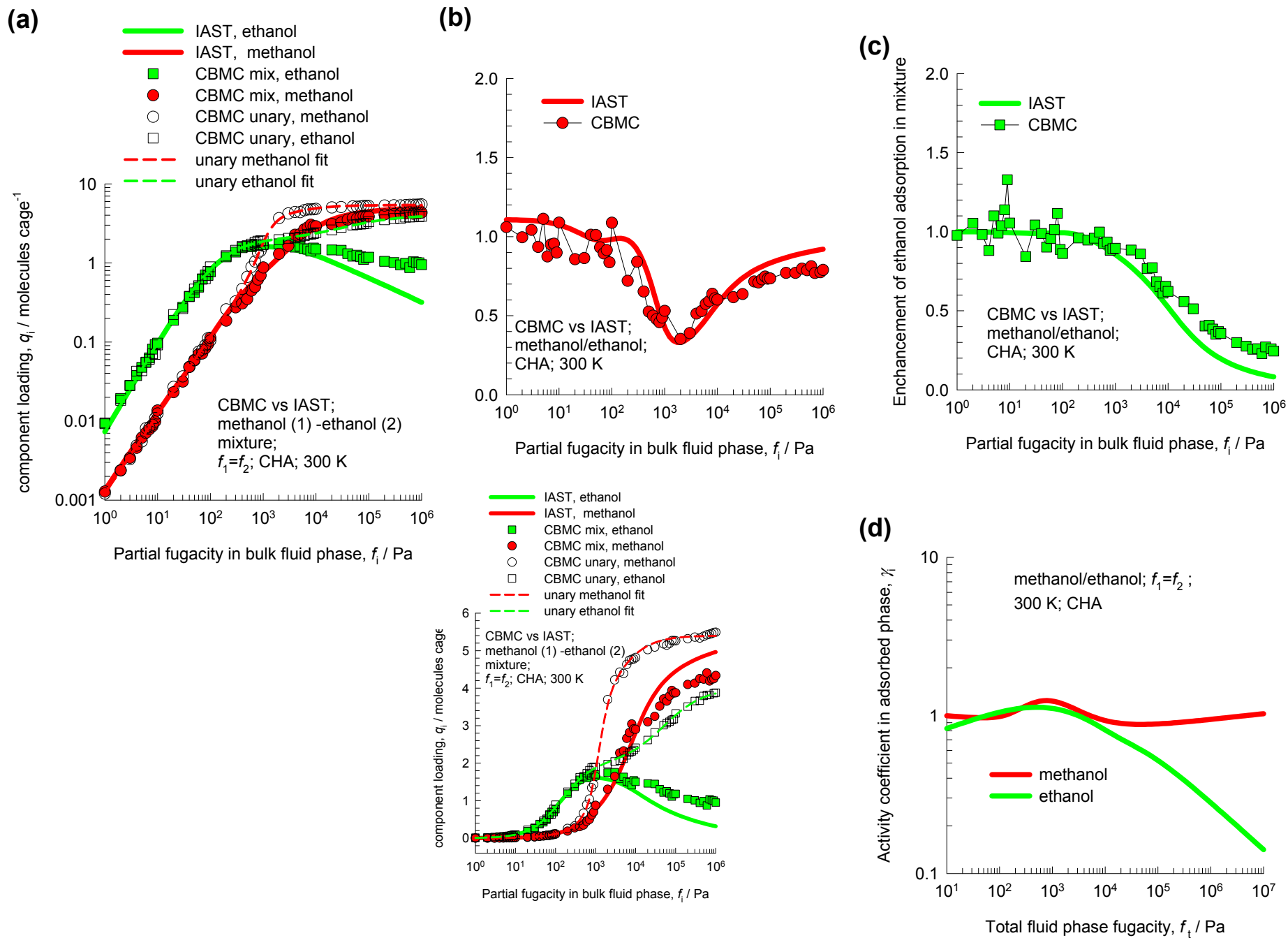
The volume of one CHA cage is 316.4 \AA^3 , slightly larger than that of a single cage of DDR (278 \AA^3), but significantly lower than FAU (786 \AA^3).

(c)



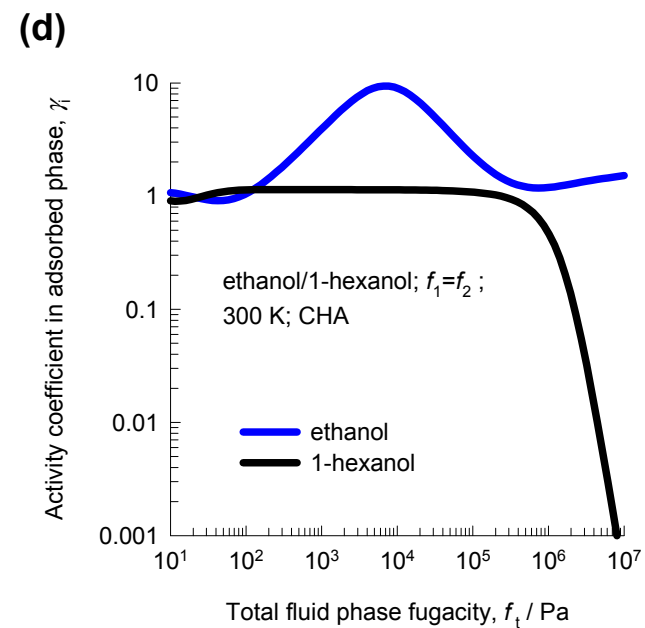
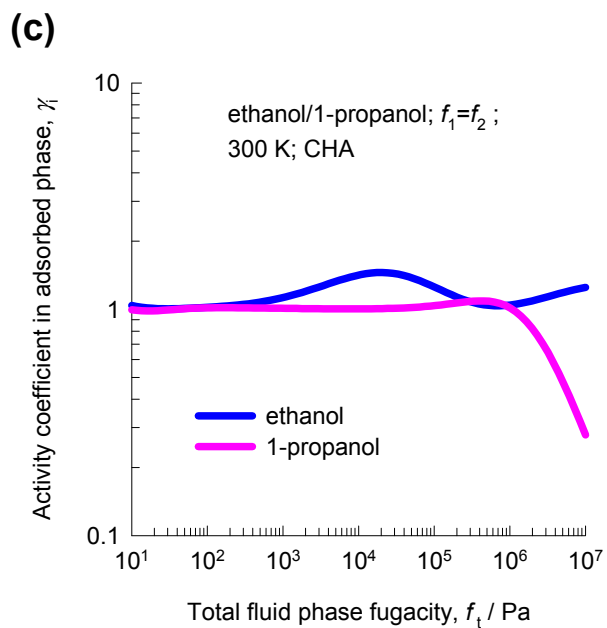
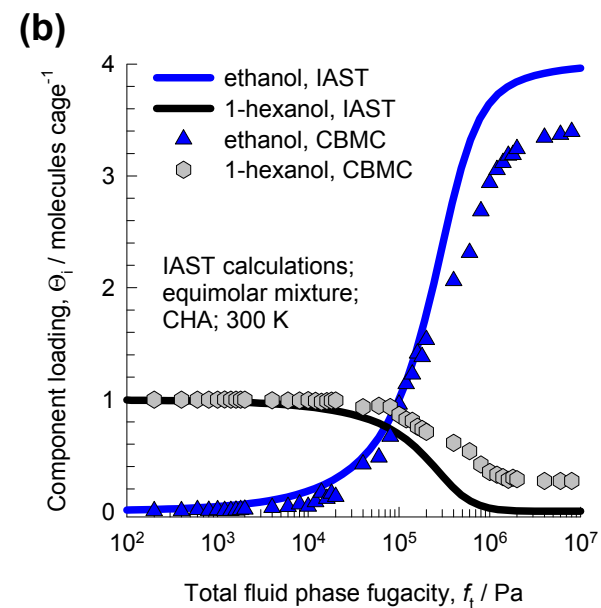
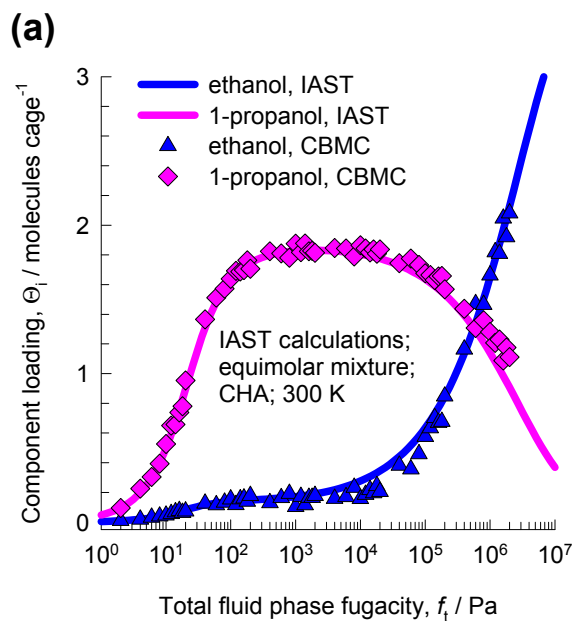
1-alcohols mixture adsorption in CHA zeolite

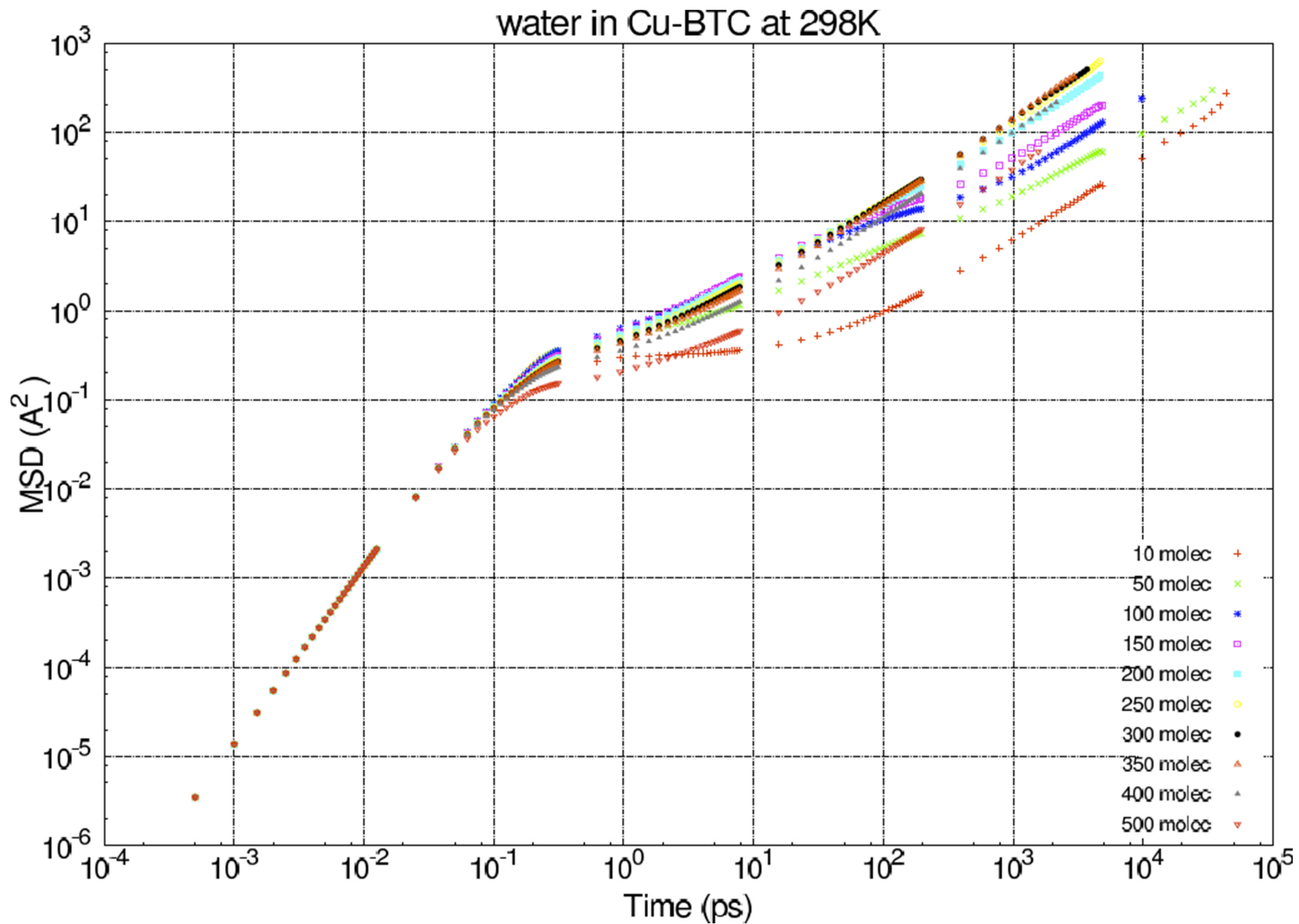
Figure ESI 46



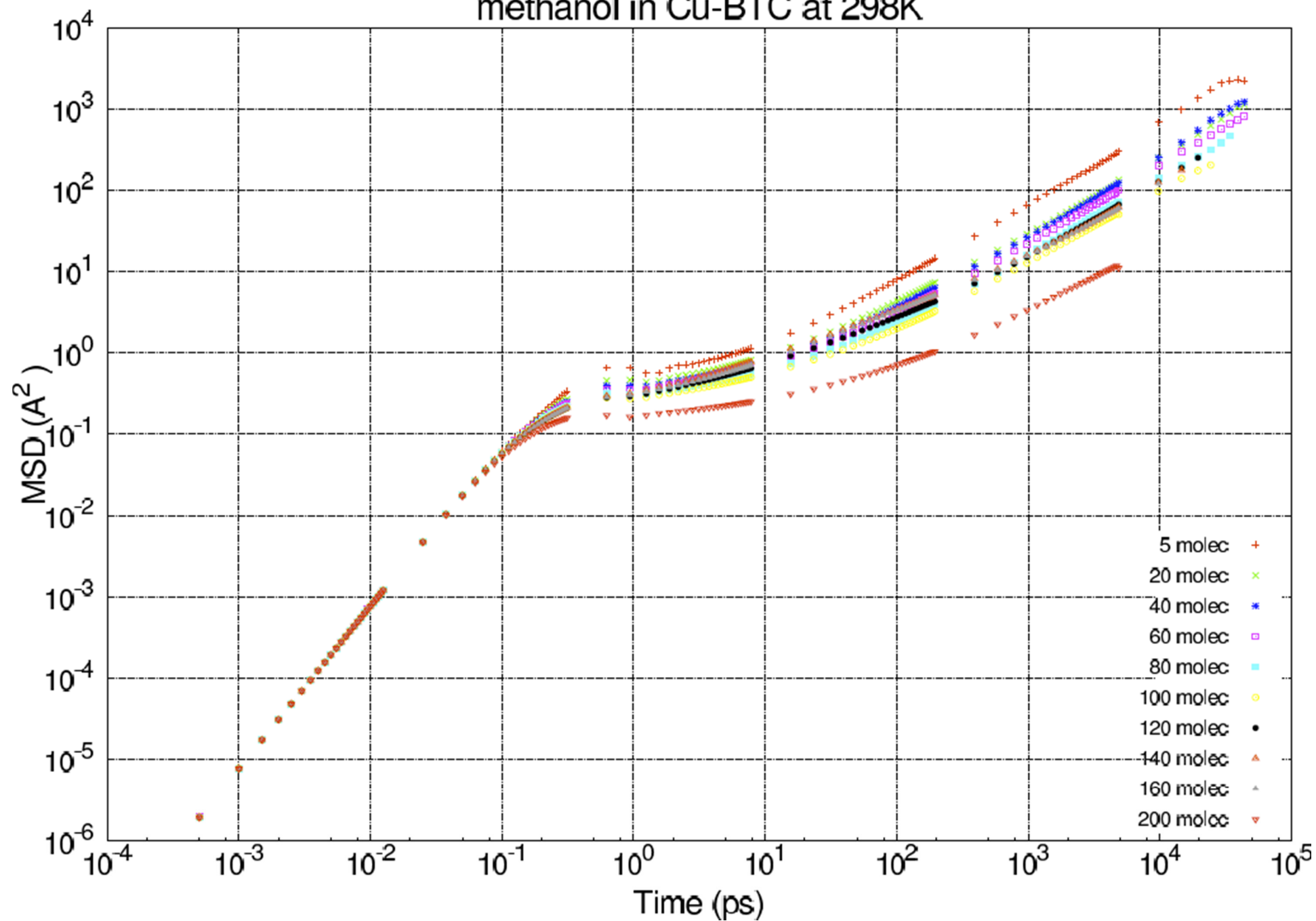
1-alcohols mixture adsorption in CHA zeolite

Figure ESI 47

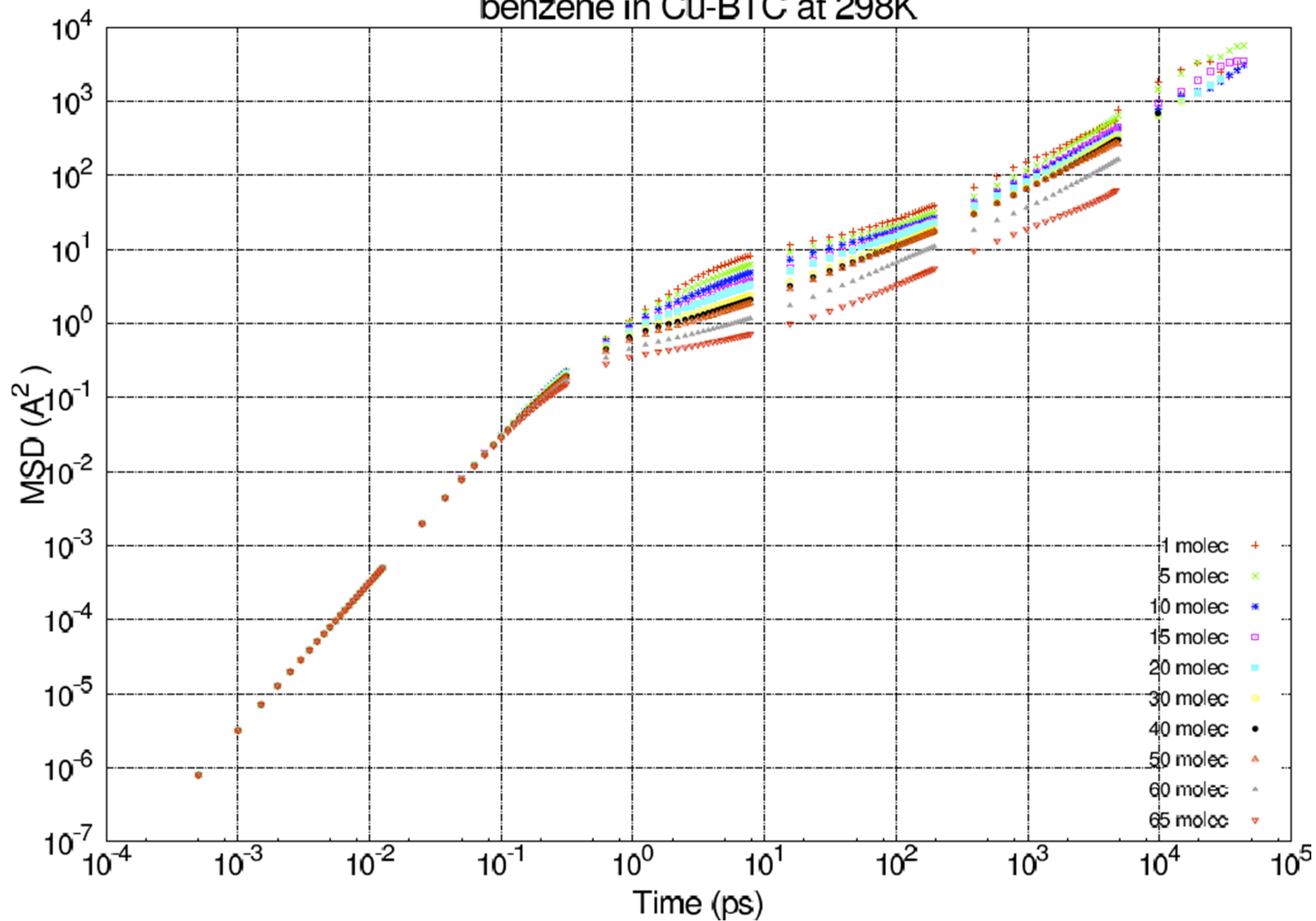


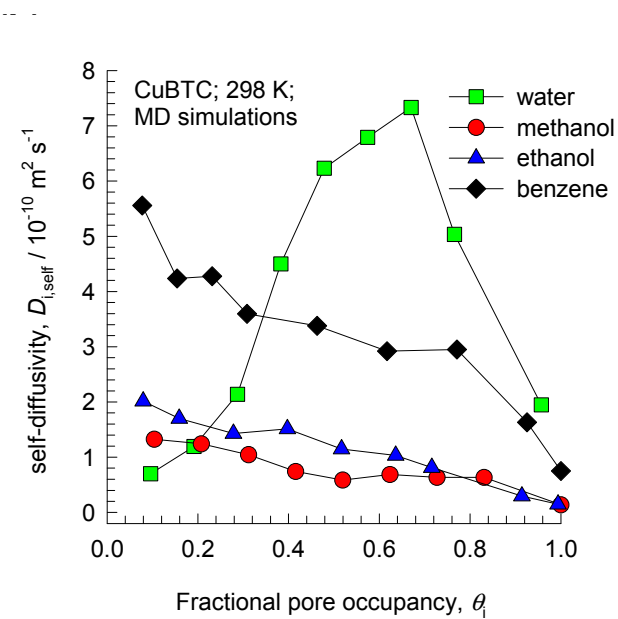
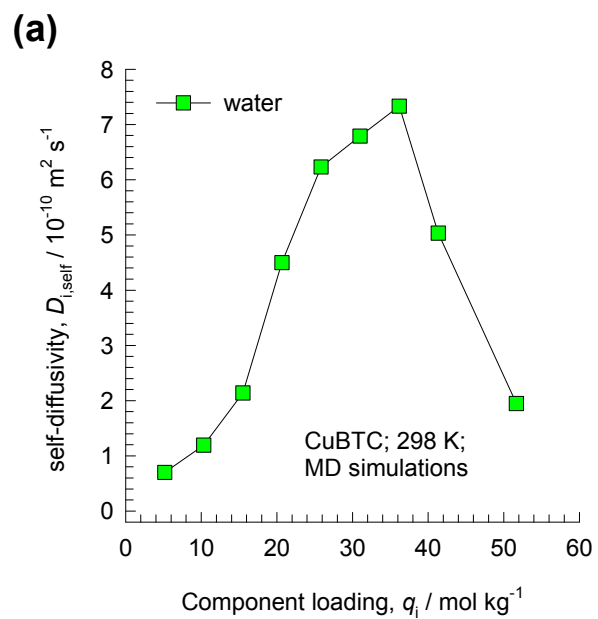


methanol in Cu-BTC at 298K

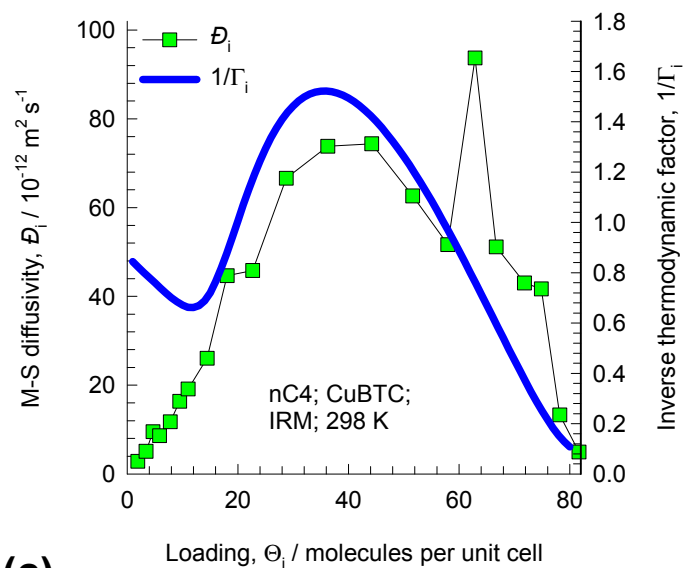


benzene in Cu-BTC at 298K

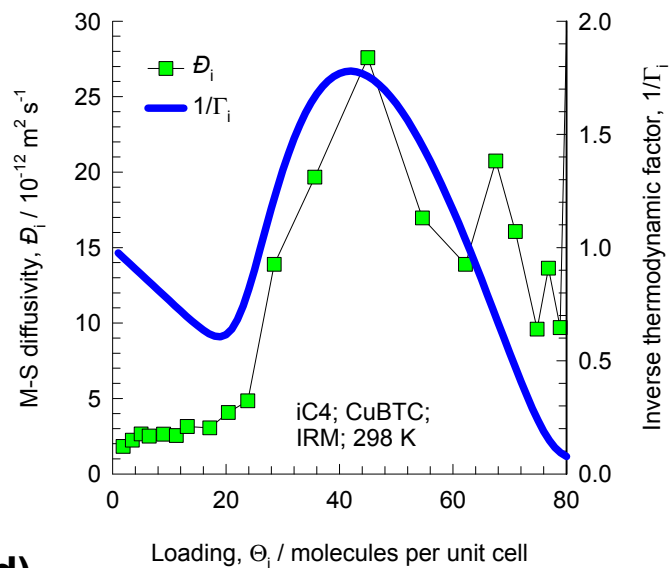


$D_{i,\text{self}} \text{ vs } q_i ; D_{i,\text{self}} \text{ vs } \theta_i$ 

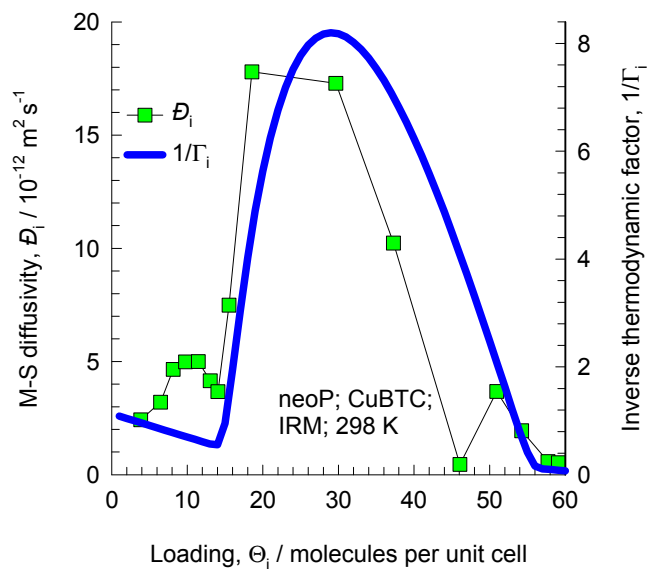
(a)



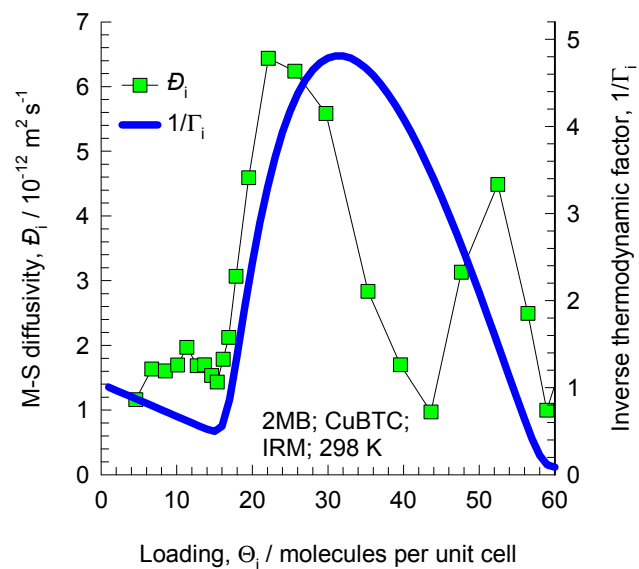
(b)



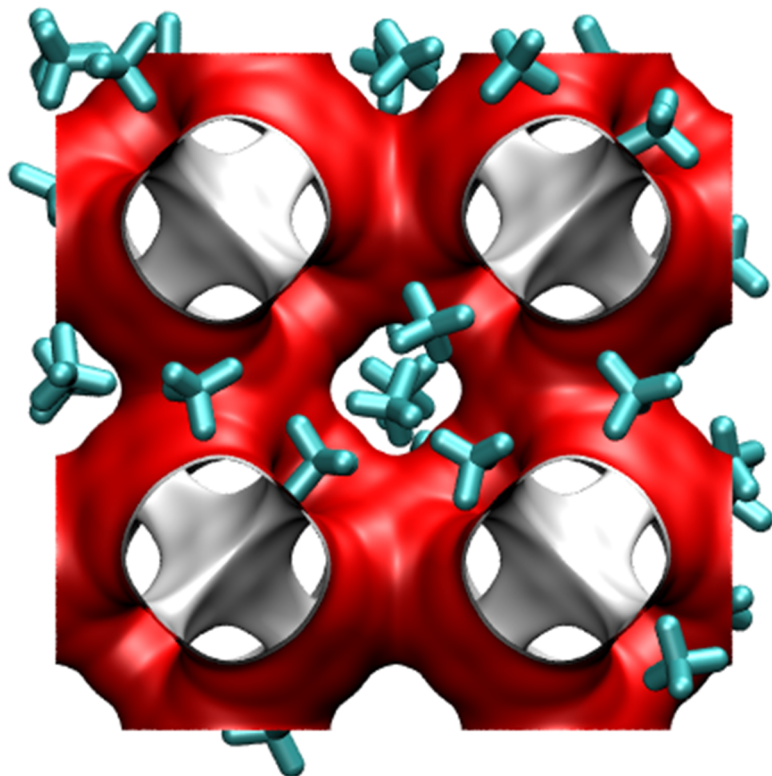
(c)



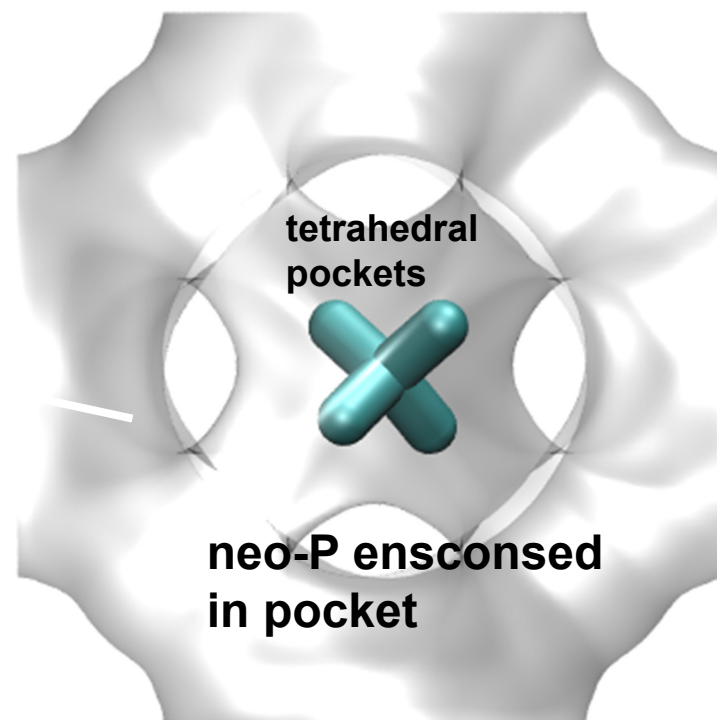
(d)



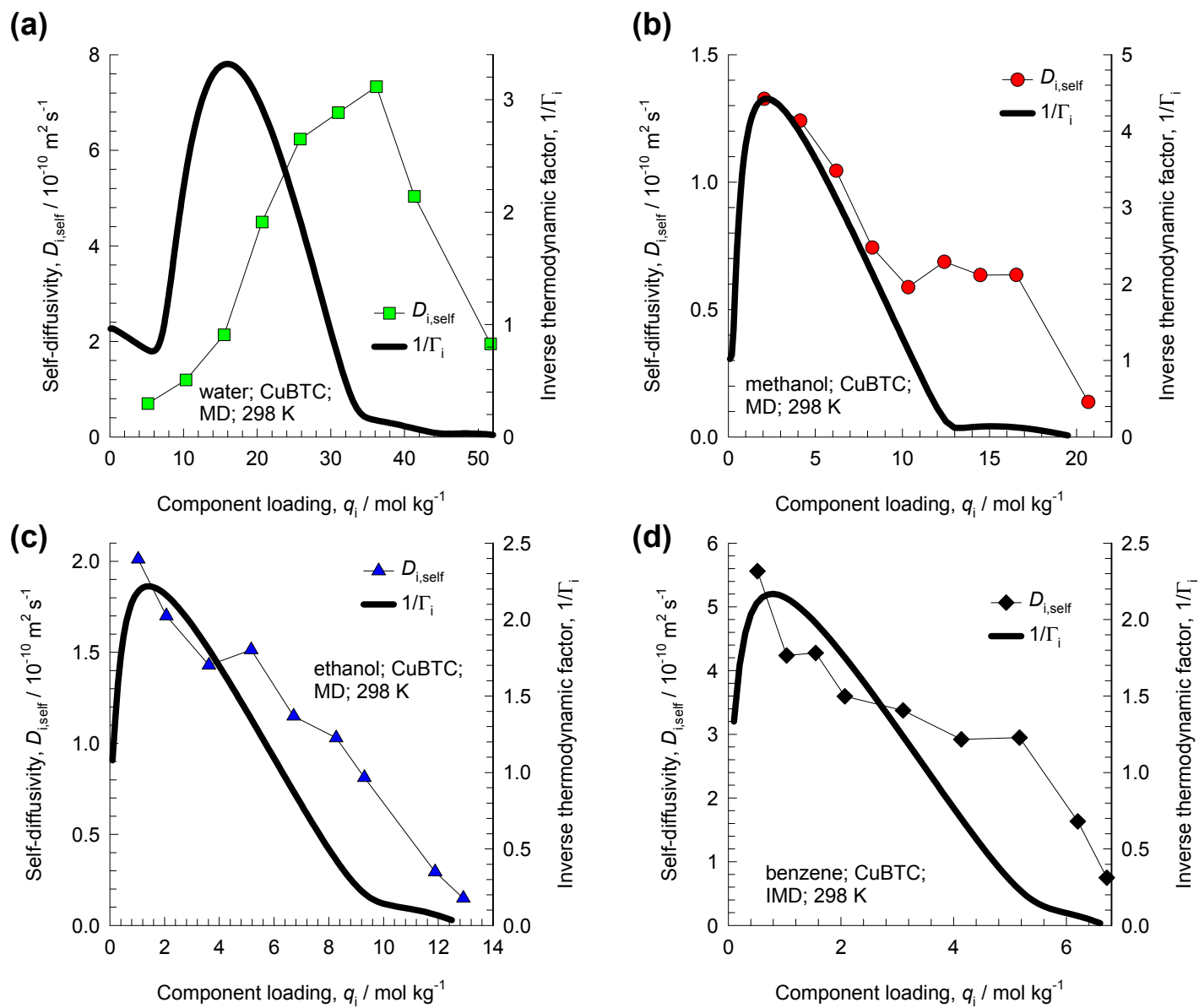
(a)

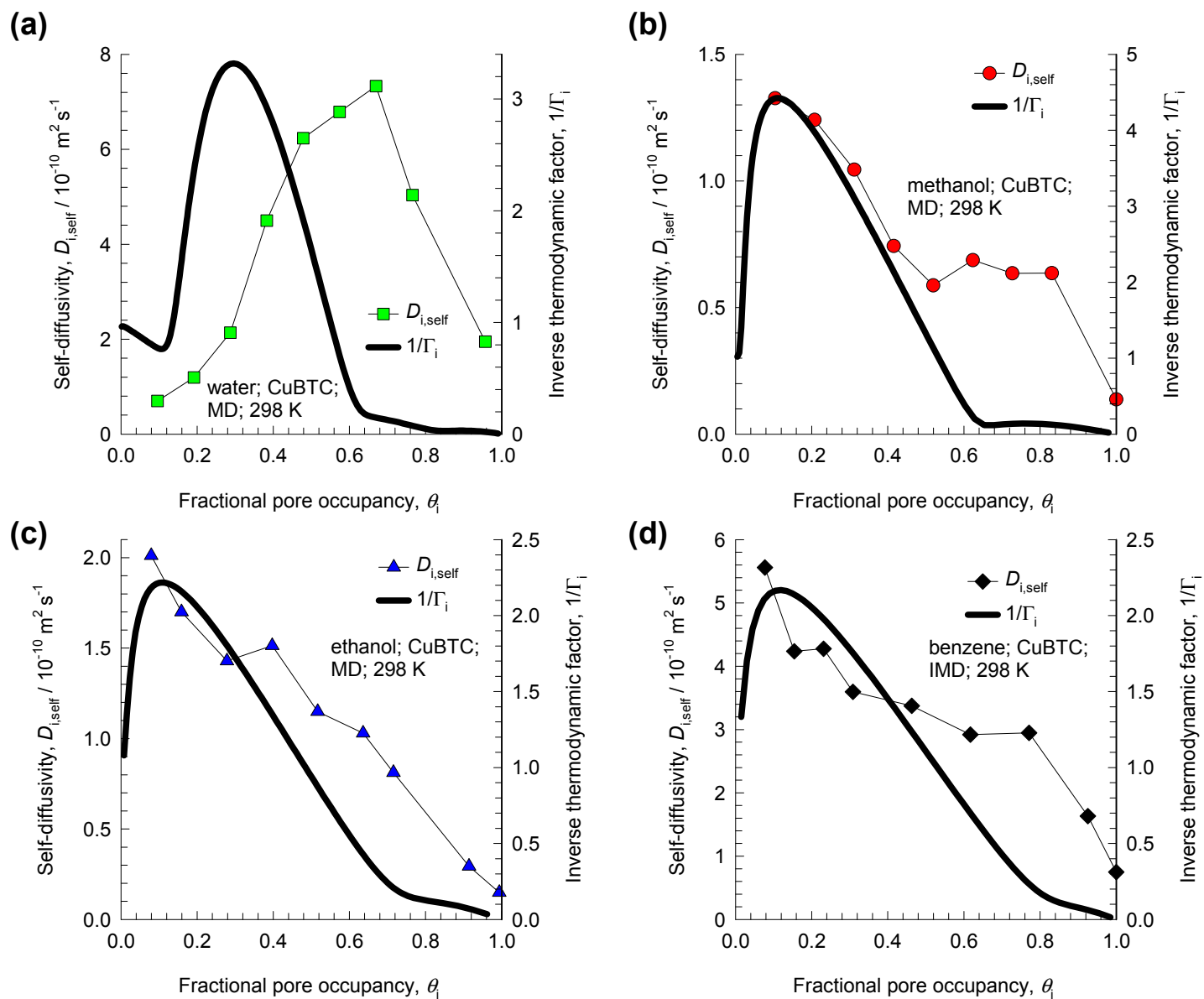


(b)



$D_{i,\text{self}}$ vs q_i versus $1/\Gamma_i$ vs q_i



$D_{i,\text{self}}$ vs θ_i versus $1/\Gamma_i$ vs θ_i 

Transient Desorption of Methanol

