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# $CO_2/CH_4$ , $CH_4/H_2$ and $CO_2/CH_4/H_2$ separations at high pressures using $Mg_2(dobdc)$ Zoey R. Herm, Rajamani Krishna<sup>\*,1</sup>, Jeffrey R. Long<sup>\*</sup>

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# 1. Introduction

The development of efficient new methods of separating gas mixtures into their component parts is urgently needed for two distinct reasons. First, many gas separations are performed on vast scales in numerous industrial processes and so improvements will lead to global energy savings [1]. Additionally, carbon capture and storage is an exciting possibility for preventing the release of anthropogenic carbon dioxide into the atmosphere and hinges on gas separations at its core. Current gas separation processes are not sufficiently advanced to render carbon capture a viable addition to power plants [2,3]. As a result, optimizing gas separations is a pragmatic approach to solving contemporary energy-related problems.

The adsorptive separation of gases, wherein one constituent interacts more strongly with the internal surfaces of a porous material, is a leading candidate in most gas separation applications [4]. This cyclic process exposes a gas mixture to a bed filled with porous adsorbent, through which one component moves quickly to the other end. The other gas adsorbs to the internal surface of the adsorbent, and is removed by either dropping the pressure or increasing the temperature to regenerate the bed [5]. Zeolites and activated carbons are common, established porous materials that offer the advantages of being inexpensive and already optimized for many existing gas separation processes.

# ABSTRACT

High-pressure separations of binary and ternary mixtures of CO<sub>2</sub>, CH<sub>4</sub>, and H<sub>2</sub> are relevant to carbon dioxide capture as well as hydrogen and natural gas purification. Metal–organic frameworks represent a class of porous materials that could be used to accomplish these separations, and Mg<sub>2</sub>(dobdc) (dobdc<sup>4–</sup> = 1,4– dioxido-2,5-benzenedicarboxylate), also sometimes referred to as Mg–MOF-74 or CPO-27–Mg, is an especially lightweight metal–organic framework with a high concentration of coordinatively-unsaturated metal sites decorating its interior surfaces. High pressure CH<sub>4</sub> adsorption isotherms presented here, together with CO<sub>2</sub> and H<sub>2</sub> adsorption behavior, are analyzed using the Ideal Adsorbed Solution Theory to model CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub>, and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> mixture separations using Mg<sub>2</sub>(dobdc). The selectivities, working capacities and breakthrough performances for these three mixtures are reported, and Mg<sub>2</sub>(dobdc) is shown to outperform zeolite 13X in each scenario.

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The exceptional porosity and chemical tunability of metal-organic frameworks, a class of porous materials that has emerged relatively recently, render them exciting candidates to replace or augment the current suite of available adsorbents [6]. Because these materials are composed of multifunctional organic molecules linked by metal cations, a nearly limitless number of combinations are available to form new structures, resulting in an immense versatility in the possible geometries and surface properties. Ideally, a metal-organic framework could be synthesized specifically for application in any given gas separation [7].

# 1.1. High-pressure CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub>, and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> separations

Hydrogen purification is one industrial process for which optimized adsorbents are urgently needed. Over 50 million tons of H<sub>2</sub> are synthesized and purified annually [8], and the same process for generating hydrogen could potentially be a step in one method for reducing carbon dioxide emissions from power plants. In precombustion CO<sub>2</sub> capture, H<sub>2</sub> is isolated from the other gases present after its synthesis and prior to its combustion, rendering water as the only combustion product. Physisorptive separation using porous adsorbents, the strategy that is already performed in many H<sub>2</sub> purification plants [9], is attractive for both H<sub>2</sub> purification and pre-combustion CO<sub>2</sub> capture, since improvements to current processes will not require drastic engineering overhauls.

Hydrogen is commonly generated by steam-reforming of methane. This process generates CO and H<sub>2</sub>. Using this CO, the watergas shift reaction generates CO<sub>2</sub> and more H<sub>2</sub>. Some CO (ca. 1– 3%) and CH<sub>4</sub> (ca. 3–6%) impurities remain in addition to the large fraction of CO<sub>2</sub> (ca. 15–25%) [10]. Because such a large proportion

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of the resulting gas mixture is  $CO_2$ , an ideal adsorbent will have a high capacity for  $CO_2$ . However, the separation of  $CH_4$  from  $H_2$  is equally or perhaps more important than  $CO_2/H_2$  separation. This is because in a packed bed of porous adsorbent the *least* adsorbing impurity will elute first and contaminate the product stream [11]. The adsorbent must be regenerated when an impurity starts to elute, and regeneration is a critical factor in optimizing an adsorptive purification system [12]. In an  $H_2$  stream contaminated with  $CO_2$ ,  $CH_4$ , and CO,  $CH_4$  is the least adsorbing impurity, because it has no quadrupole or dipole moment [13]. Methane is also important to remove from a flue gas since it is a potent greenhouse gas [14].

The separation of CH<sub>4</sub> from H<sub>2</sub> is also relevant to refinery off-gas processing [13,15]. The gas mixture being separated is approximately 50% H<sub>2</sub> at 5–10 bar [16,17]. Here, the impurities are C1–C5 hydrocarbons. As in CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> separation, the most difficult separation is the most important to optimize. Methane is the smallest of the impurities, making the van der Waals forces between it and the surface of a porous material the weakest [16]. As a result, CH<sub>4</sub>/H<sub>2</sub> separation is the most difficult separation to achieve in refinery off-gas separation.

Separation of  $CO_2$  from  $CH_4$  is a distinct separation from those described above. It is relevant to the purification of natural gas, which can have up to 92%  $CO_2$  impurity at its source [18]. Removal of  $CO_2$ , which is most commonly accomplished using amines [19] to reduce  $CO_2$  levels to the required 2% maximum, is conducted between 20 and 70 bar [20]. Carbon dioxide removal is required for approximately 25% of the natural gas reserves in the United States [18].

#### 1.2. The metal–organic framework Mg<sub>2</sub>(dobdc)

Metal-organic frameworks are a class of porous materials that offer potential advantages over traditional adsorbents for all of the aforementioned gas separations. A number of these have already been studied for separations of  $CO_2/CH_4$  [21–26],  $CH_4/H_2$ [27–35], and  $CO_2/H_2$  [11,31,32,36–45]. Frameworks featuring coordinatively-unsaturated metal sites are especially promising for these gas separations. High-pressure adsorption isotherms of  $CO_2$  and  $CH_4$  have been calculated [46,47] and measured [48] together in metal-organic frameworks of this type. High-pressure  $CO_2$ ,  $H_2$  and  $CH_4$  adsorption behavior have been studied in isolation in even more metal-organic frameworks with open metal sites.

We recently reported that metal-organic frameworks are promising candidates for effecting H<sub>2</sub> separation from CO<sub>2</sub> and, as a result, are possible alternatives to current adsorbents (zeolites and activated carbons) for H<sub>2</sub> purification or pre-combustion CO<sub>2</sub> capture [42]. In particular, Mg<sub>2</sub>(dobdc), a metal-organic framework with a high concentration of exposed Mg<sup>2+</sup> sites decorating its surface, displayed a much higher CO<sub>2</sub>/H<sub>2</sub> selectivity than other frameworks, as well as zeolites and activated carbons. Additionally, its working capacity (the difference in the amount adsorbed at the high adsorption pressure and the lower purge pressure) is much higher than activated carbons, zeolites, and most other metal-organic frameworks. Computationally, Mg<sub>2</sub>(dobdc) was shown to be outstanding in both selectivity and CO<sub>2</sub> capacity among an even larger group of zeolites, activated carbons and metal-organic frameworks when compared for both CO<sub>2</sub>/H<sub>2</sub> and CH<sub>4</sub>/H<sub>2</sub> separations [45]. Experimentally, the material was investigated for the ambient-pressure separation of  $CO_2$  and  $CH_4$  in  $Mg_2(dobdc)$  [26] and high-pressure adsorption isotherms of CO<sub>2</sub> and CH<sub>4</sub> were also measured [49]. Both of these studies reported breakthrough curves for CO<sub>2</sub>/CH<sub>4</sub> mixtures, but neither discussed the equilibrium mixture behavior.

In order to rigorously examine the applicability of  $Mg_2(dobdc)$  for  $CO_2/CH_4$ ,  $CH_4/H_2$ , and  $CO_2/CH_4/H_2$  separations, we now report

pure-component CH<sub>4</sub> adsorption behavior onto Mg<sub>2</sub>(dobdc). These data are analyzed together with the previously reported high-pressure CO<sub>2</sub> and H<sub>2</sub> isotherms [42]. Low pressure (0–1 bar) CO<sub>2</sub> and CH<sub>4</sub> adsorption isotherms are also reported in order to improve the quality of the data set. The Ideal Adsorbed Solution Theory (IAST) [50] is applied to pure component isotherms of CH<sub>4</sub>, H<sub>2</sub> and CO<sub>2</sub> in order to demonstrate the selectivity and working capacity for binary CO<sub>2</sub>/CH<sub>4</sub> and CH<sub>4</sub>/H<sub>2</sub>, as well as ternary CH<sub>4</sub>/H<sub>2</sub>/CO<sub>2</sub>, mixtures. Breakthrough behavior for CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub> and CO<sub>2</sub>/H<sub>2</sub>/CH<sub>4</sub> mixtures are simulated. All of the isotherms were measured on samples of Mg<sub>2</sub>(dobdc) generated in the same laboratory and confirmed to be of high quality via cryogenic N<sub>2</sub> adsorption measurements, a technique that is very sensitive to the purity of the sample.

#### 2. Experimental

#### 2.1. Synthesis and characterization of Mg<sub>2</sub>(dobdc)

The compound Mg<sub>2</sub>(dobdc) was synthesized as reported previously [42]. All reagents were obtained from commercial vendors and used without further purification. The material was activated using a strategy adapted from the literature procedure. The yellow microcrystalline solids were combined and washed five times with DMF and soaked in DMF for 24 h. The DMF was decanted, and freshly distilled methanol was added. The solid was then transferred to a nitrogen-filled glovebox. The methanol was decanted and the solid was soaked in anhydrous DMF on a hotplate set at 100 °C for 18 h. The DMF was decanted and replaced, and the solid was soaked at 100 °C for 4 h. The DMF was decanted and replaced by methanol, which was decanted and replenished 12 times with a minimum of 6 h between washes. Infrared spectroscopy was used to confirm the removal of all DMF by monitoring the C=O stretch at ca. 1650  $\text{cm}^{-1}$  (see Fig. S1). Infrared spectra were obtained on a Perkin-Elmer Spectrum 100 Optica FTIR spectrometer furnished with an attenuated total reflectance accessory (ATR).

# 2.2. Low-pressure gas adsorption measurements

Gas adsorption isotherms for pressures in the range 0-1.1 bar were measured by a volumetric method using a Micromeritics ASAP2020 instrument. A sample was transferred in an N<sub>2</sub>-filled glovebox to a pre-weighed analysis tube, which was capped with a transeal and evacuated by heating to 180 °C at 0.1 °C per minute under dynamic vacuum for until the outgas rate was determined to be 4 µTorr/min. The evacuated analysis tube containing the degassed sample was then carefully transferred to an electronic balance and weighed again to determine the mass of sample. The tube was then transferred back to the analysis port of the gas adsorption instrument. For all isotherms, warm and cold free space correction measurements were performed using ultra-high purity He gas (UHP grade 5.0, 99.999% purity); N2 isotherms at 77 K were measured in liquid nitrogen using UHP-grade gas sources. Adsorption of CO<sub>2</sub> and CH<sub>4</sub> at 323 K was measured using a Julabo isothermal bath with UHP-grade gases. Oil-free vacuum pumps and oil-free pressure regulators were used for all measurements to prevent contamination of the samples during the evacuation process or of the feed gases during the isotherm measurements.

#### 2.3. High-pressure gas adsorption measurements

A sample of  $Mg_2(dobdc)$  (289.0 mg) was loaded in an air-free sample holder in a glove box under a nitrogen atmosphere. The stainless steel sample holder was weighed five times before adding the sample and three times afterwards in order to determine the precise mass of Mg<sub>2</sub>(dobdc). Methane excess adsorption measurements were performed on an automated Sieverts' apparatus (PCT-Pro-E&E from Setaram Instrumentation) over a pressure range of 1–50 bar. UHP grade 5.0 methane and helium (99.999% purity) were used. Total adsorption was calculated using NIST Thermochemical Properties of Fluid Systems [51]: CH<sub>4</sub> densities between 0 and 50 bar were fit using a sixth-order polynomial, then multiplied by the previously reported pore volume of 0.57 cm<sup>3</sup>/g. The Langmuir region of the 77 K N<sub>2</sub> adsorption isotherm was measured again after the high-pressure adsorption measurement to ensure sample contamination had not occurred (see Fig. S2).

#### 2.4. Ideal Adsorbed Solution Theory calculations

The Ideal Adsorbed Solution Theory (IAST) of Prausnitz and Myers was used to estimate the composition of the adsorbed phase from pure component isotherm data [50,52]. A detailed explanation of the IAST calculations has been previously reported [42]. The pure component isotherm data for  $CO_2$ ,  $CH_4$ , and  $H_2$  in Mg<sub>2</sub>(dobdc), after conversion to absolute loadings, were fitted with Langmuir–Freundlich isotherm models. For the cases of  $CO_2$  and  $CH_4$  dual-site isotherm models of the type shown in Eq. (1) were employed.

$$q_{i} = q_{i,A,sat} \frac{b_{i,A} p_{i}^{v_{i,A}}}{1 + b_{i,A} p_{i}^{v_{i,A}}} + q_{i,B,sat} \frac{b_{i,B} p_{i}^{v_{i,B}}}{1 + b_{i,B} p_{i}^{v_{i,B}}}$$
(1)

Here,  $q_i$  is the component molar loading of species *i* (in mol/kg),  $q_{i,sat}$  is the saturation loading of species *i* and  $p_i$  is the bulk gas pressure of species *i* (in Pa). Subscripts *A* and *B* refer to the two different types of adsorption sites on the surface. The parameters  $v_i$  are the dimensionless exponent in the Langmuir–Freundlich isotherms. These parameters are provided for all three gases in Table 1. For the case of H<sub>2</sub>, the data were fit using a single-site isotherm model in which the second term in Eq. (1) is dropped. Fig. S3 compares the experimental data with the Langmuir–Freundlich fits.

#### 2.5. Zeolite 13X data treatment

The pure component isotherm data for  $CO_2$ ,  $CH_4$ , and  $H_2$  in zeolite 13X were obtained from previous reports [53,54]. In cases where the excess loadings were reported, these were converted to absolute loadings using the reported pore volume data along with the Peng–Robinson equation of state for estimation of fluid densities in the pores. The reported data are for a variety of temperatures that unfortunately do not include 313 K. In these cases the Langmuir constants were fitted using Eq. (2).

$$\begin{aligned} b_{i,A} &= b_{i,A0} \exp\left(\frac{k}{kT}\right) \\ b_{i,B} &= b_{i,A0} \exp\left(\frac{k}{kT}\right) \end{aligned}$$

$$(2)$$

Here, *b* is the dual-site Langmuir–Freundlich constant for species *i* and *A* and *B* represent the two adsorption sites on the surface. The heats of adsorption, *E*, for CO<sub>2</sub>, CH<sub>4</sub>, and H<sub>2</sub> were taken to be 35, 14, and 6 kJ/mol respectively. The reported values of the dual-site

Langmuir–Freundlich parameters are listed in Table 1 and are for T = 313 K. Figs. S4 and S5 compare the experimental data with the dual-site Langmuir–Freundlich fits for 313 K.

# 2.6. Breakthrough simulations

The methods employed for performing breakthrough simulations have been described in detail elsewhere [11].

# 3. Results and discussion

# 3.1. Pure-component CO<sub>2</sub>, CH<sub>4</sub>, and H<sub>2</sub> adsorption in $Mg_2(dobdc)$

Fig. 1 shows the pure-component absolute adsorption isotherms for  $CH_4$ ,  $H_2$ , and  $CO_2$  in  $Mg_2(dobdc)$  at 313 K and pressures in the range 0–40 bar. These isotherms are in agreement with previously published data [3,42,49]. At 35 bar,  $CO_2$  has reached saturation at 15 mmol/g, while  $CH_4$  and  $H_2$  have not, reaching ca. 10 and 3 mmol/g, respectively. The  $H_2$  adsorption isotherm is linear in this pressure window, while  $CH_4$  begins to approach saturation behavior.

These isotherms were fit with Langmuir–Freundlich models using a dual-site model for  $CO_2$  and  $CH_4$  and a single-site model for  $H_2$  (see Table 1). The open-metal sites in Mg<sub>2</sub>(dobdc) create heterogeneity in the surface that requires this type of modeling; however, the small size and low adsorption enthalpy of  $H_2$  led to a sufficiently good fit of the data using a single-site model.

# 3.2. CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> separations calculated with IAST

The remainder of this article discusses the mixed-gas adsorption behavior of  $CO_2$ ,  $CH_4$ , and  $H_2$  in Mg<sub>2</sub>(dobdc). Using the Ideal Adsorbed Solution Theory (IAST) [50], mixed-gas adsorption behavior was extracted from the pure-component isotherms. Such estimations are essential in practice because collecting experimental data on mixture adsorption is time consuming and extremely rare [55]. IAST was used to calculate selectivity, working capacity and breakthrough performance.

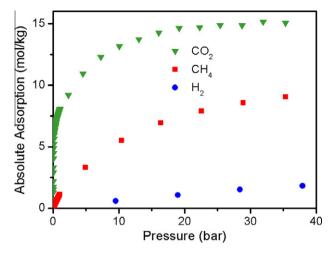
The binary mixtures are calculated as a 50/50 composition. This composition was chosen because most reports of these mixtures employ a 50/50 mixture. Further, this ratio should mitigate some of the artifacts of IAST that can be observed when the less-ad-sorbed species is a large fraction of the gas mixture [44]. The ternary mixture is 1:4:20 CH<sub>4</sub>:CO<sub>2</sub>:H<sub>2</sub> in an effort to model a realistic hydrogen purification composition.

The use of IAST with any adsorbent/adsorbate mixture system must be carefully considered due to the limitations of the theory [56]. We have determined IAST to be appropriate for the gas mixtures evaluated here. The theory has been used to evaluate  $CH_4/H_2$ [30],  $CO_2/CH_4$  [25,57–63], and  $CO_2/H_2$  [42] gas mixtures in metalorganic frameworks. More valuable in evaluating the validity of IAST in these gas mixtures are comparisons of IAST and Grand Canonical Monte Carlo (GCMC) simulations. It has been show that IAST compares well with GCMC simulations of  $CH_4/H_2$  selectivity

Table 1

Dual-site Langmuir–Freundlich parameters for pure  $CH_4$ ,  $H_2$  and  $CO_2$  data for  $Mg_2$ (dobdc) and zeolite 13X at 313 K.

		Site A			Site B		
		$q_{i,A,sat}$ (mol/kg)	$b_{i,A_i} P a^{-v_i}$	n <sub>i,A</sub> Dimensionless	$q_{i,B,sat}$ (mol/kg)	$b_{i,B}$ , $Pa^{-v_i}$	n <sub>i,A</sub> Dimensionless
CO <sub>2</sub>	$Mg_2(dobdc)$	6.8	$\textbf{2.48}\times \textbf{10}^{-4}$	1	9.9	$1.4\times10^{-6}$	1
	13X	3.5	$2.51  imes 10^{-7}$	1	5.2	$4.16  imes 10^{-5}$	1
CH <sub>4</sub>	Mg <sub>2</sub> (dobdc)	11	$7.91  imes 10^{-7}$	1	5	$1.9  imes 10^{-8}$	1
	13X	4	$7.92  imes 10^{-8}$	1	5	$8.12  imes 10^{-7}$	1
$H_2$	$Mg_2(dobdc)$	40	$1.62  imes 10^{-7}$	0.832			
	13X	18	$2.43 imes10^{-8}$	1			



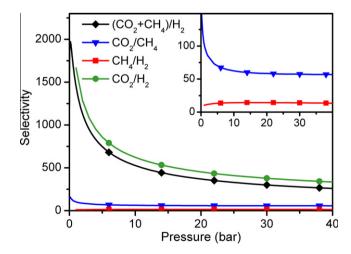
**Fig. 1.** Absolute adsorption isotherms for  $CO_2$ ,  $CH_4$  and  $H_2$  in  $Mg_2(dobdc)$  at 313 K. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

in MOF-5 and HKUST-1 [32]. The effectiveness of IAST has also been validated by this method for  $CH_4/H_2$  separations in non-interpenetrated [29,31,33,34] and interpenetrated [35,64] metal-organic frameworks. GCMC simulations have further validated the use of IAST for the modeling of  $CO_2/CH_4$  mixtures in metal-organic frameworks [64–66]. Finally, the use of IAST for  $CO_2/H_2$  separations has been validated in Mg<sub>2</sub>(dobdc) specifically using configurational bias Monte Carlo simulations [67].

#### 3.3. CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> selectivity

Selectivity is an important metric for evaluating adsorbents and can be calculated using IAST [68,69]. Selectivity for a binary gas mixture is defined as in Eq. (3), where  $q_i$  is the mole fraction of component *i* in the adsorbed phase and  $p_i$  is the mole fraction of component *i* in the bulk gas phase.

$$Selectivity = \frac{q_1/q_2}{p_1/p_2}$$
(3)



**Fig. 2.** IAST selectivities obtained for  $Mg_2(dobdc)$  at 313 K for  $CO_2$  and  $CH_4$  in a 1:4:20  $CH_4:CO_2:H_2$  mixture,  $CO_2$  in a 1:1  $CO_2:CH_4$  mixture,  $CH_4$  in a 1:1  $CH_4:H_2$  mixture and  $CO_2$  in an 80:20  $H_2:CO_2$  mixture. Selectivities are calculated throughout the entire line trace, and symbols are only shown to distinguish the lines visually. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

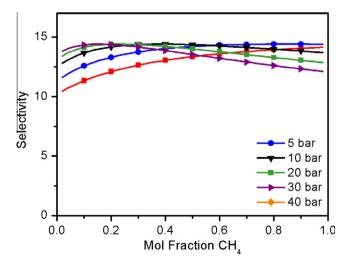
Fig. 2 shows  $CO_2/CH_4$ ,  $CH_4/H_2$  and  $(CO_2 + CH_4)/H_2$  selectivities for  $Mg_2(dobdc)$ .  $CO_2/H_2$  selectivity is also shown for comparison for an 80:20 mixture. As expected, the  $CO_2/CH_4$  selectivity is higher than the  $CH_4/H_2$  selectivity, and both are lower than the  $CO_2/H_2$ selectivity, which ranges from 900–400 at these pressures [42]. This can be rationalized using the quadrupole moments and polarizabilities of the three gases [13] and are discussed individually below.

 $CO_2/CH_4$  selectivity is high because  $CH_4$  has no quadrupole moment, while  $CO_2$  does. In contrast,  $CO_2/H_2$  selectivity is higher than  $CO_2/CH_4$  because  $CO_2$  is has a higher quadrupole moment and higher polarizability than  $H_2$ , while  $CO_2$  and  $CH_4$  have similar polarizabilities. The selectivity decreases drastically for the  $CO_2/$  $CH_4$  mixture up to 5 bar, which can be attributed to the strong  $CO_2$  binding at low loadings evidenced by the steep rise in the pure-component isotherm at low pressures [38].

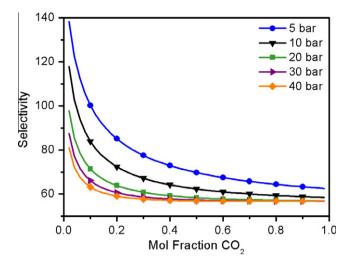
 $CH_4/H_2$  selectivity is the lowest selectivity examined here because while  $CH_4$  is more polarizable than  $H_2$  the quadrupole moment of  $H_2$  is *larger* than that of  $CH_4$ . However, the difference in quadrupole moment between  $CH_4$  and  $H_2$  is larger  $(6.62\times 10^{25}\,esu\,cm^2)$  than the difference in polarizability  $(17.888\times 10^{25}\,cm^3).$ 

The selectivity for three-component  $CH_4/CO_2/H_2$  mixtures relevant to hydrogen purification and pre-combustion  $CO_2$  capture is also shown in Fig. 2. In a 1:4:20  $CH_4:CO_2:H_2$  mixture, the selectivity for both  $CO_2$  and  $CH_4$  decreases from 1400 at 1 bar to 260 at 40 bar. This selectivity is slightly lower than the 20:80  $CO_2:H_2$  selectivity reported in an earlier work [42]. This is expected, as compared to a 20:80 mixture a 4:16:80  $CH_4:CO_2:H_2$  mixture essentially replaces a fraction of strongly-selective  $CO_2$  with less-selective  $CH_4$ .

Because of the variability in gas mixture compositions in the shifted products of steam-methane reforming, refinery off-gas, and natural gas, investigating the performance under different compositions is an important indicator of a broadly useful material. Fig. 3 shows the selectivity for  $CH_4$  in a  $CH_4/H_2$  mixture and mixture as a function of mole fraction of  $CH_4$ . Selectivity for  $CH_4$  in a  $CH_4/H_2$  mixture varies only slightly with composition at all pressures. This is expected because the selectivity shown in Fig. 2 is not strongly pressure-dependent and therefore should not be dependent on the partial pressure of  $CH_4$ .



**Fig. 3.** IAST selectivities obtained for  $Mg_2(dobdc)$  at 313 K for  $CH_4$  in a 1:1  $CH_4:H_2$  mixture at 5, 10, 20, 30 and 40 bar. Selectivities are calculated throughout the entire line trace, and symbols are only shown to distinguish the lines visually. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 4.** IAST selectivities obtained for  $Mg_2(dobdc)$  at 313 K for  $CO_2$  in a 1:1  $CO_2:CH_4$  mixture at 5, 10, 20, 30 and 40 bar. Selectivities are calculated throughout the entire line trace, and symbols are only shown to distinguish the lines visually. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

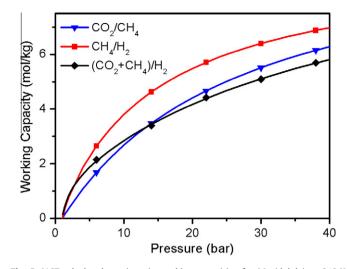
Fig. 4 shows the selectivity for  $CO_2$  in a  $CO_2/CH_4$  as a function of mole fraction of  $CO_2$ . In contrast to  $CH_4/H_2$  selectivity, which is nearly pressure-independent,  $CO_2/CH_4$  selectivity decreases by half from 2% to 98%  $CO_2$  in the case of a 5 bar mixture. This is expected because selectivity decreases with higher partial pressures of  $CO_2$  due to the saturation of the strongly adsorbing sites on the surface of Mg<sub>2</sub>(dobdc). At high mole fractions of  $CO_2$ , the selectivity asymptotically approaches ca. 57.

#### 3.4. CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> working capacity

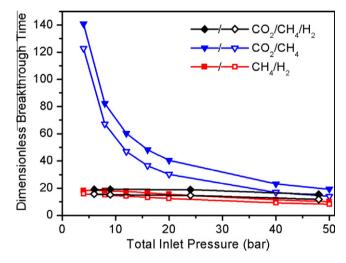
The working capacity of  $Mg_2(dobdc)$  for these same three mixtures can be seen in Fig. 5. The working capacity is the difference between the amount adsorbed at high pressures and the amount adsorbed at the lower purge pressure, which is assumed here to be 1 bar. It has been previously reported [68,69] that the working capacity is equally as important as selectivity in optimizing an adsorbent for pressure-swing adsorption. The working capacity of  $CO_2$  is higher than for CH<sub>4</sub>, but the difference is smaller than the difference in the pure-component isotherms. This is a result of the shallow rise in adsorption of CH<sub>4</sub> at lower pressures. The three-component mixture working capacity falls close to the binary mixture capacities but is lower at high pressures. This can be attributed to the difference in compositions of the three mixtures studied, as 80% of the mixture is comprised of H<sub>2</sub> in the three-component mixture.

# 3.5. CO<sub>2</sub>/CH<sub>4</sub>, CH<sub>4</sub>/H<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> breakthrough performance

The performance of a pressure swing adsorber, an industrial gas separation unit that relies on physisorption at high pressure and regeneration at low pressure, is dictated by both selectivity and capacity considerations. In a recent publication, we developed a procedure for screening MOFs using transient breakthrough of gas mixtures in a fixed bed adsorber [11]. In this approach, a dimensionless breakthrough time is defined and calculated assuming isothermal conditions. The breakthrough time, for a specified purity of the outlet gas mixtures, represents an appropriate combination of selectivity and capacity that is relevant in practice. In the current work, we use the same approach to evaluate the performance of  $Mg_2(dobdc)$ .



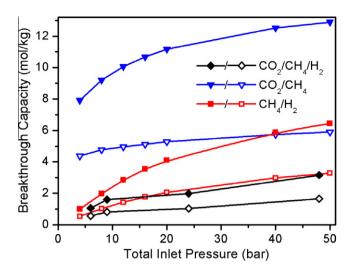
**Fig. 5.** IAST-calculated gravimetric working capacities for  $Mg_2(dobdc)$  at 313 K assuming a purge pressure of 1 bar for  $CO_2$  and  $CH_4$  in a 1:4:20  $CH_4:CO_2:H_2$  mixture,  $CO_2$  in a 1:1  $CO_2:CH_4$  mixture, and  $CH_4$  in a 1:1  $CH_4:H_2$  mixture. Working capacities are calculated throughout the entire line trace, and symbols are only shown to distinguish the lines visually. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 6.** Dimensionless breakthrough times at 313 K for a 1:1:1  $CH_4:CO_2:H_2$  mixture, 1:1  $CO_2:CH_4$ , and a 1:1  $CH_4:H_2$  mixture as a function of the inlet pressure of a packed bed adsorber where the breakthrough is defined as 0.05 mol percent impurity in outlet gas. Closed symbols represent Mg<sub>2</sub>(dobdc) and open symbols represent zeolite 13X. Lines are for visualization purposes only. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 6 displays the time at which 0.05 mol percent of the gas leaving the column is impurity gas for equimolar mixtures of  $CO_2/CH_4$ ,  $CH_4/H_2$ , and  $CO_2/CH_4/H_2$  in both  $Mg_2(dobdc)$  and zeolite 13X. Interestingly,  $CH_4/CO_2/H_2$  and  $CH_4/H_2$  mixture breakthrough times are very similar and  $CO_2/CH_4$  breakthrough times are much higher. This difference can theoretically be attributed to the significantly lower adsorption strength of  $H_2$ .

Fig. 7 displays the amount of  $CO_2$  or  $CH_4$  that is adsorbed by the time this breakthrough threshold is reached. The relative ordering of the three separations is dependent on the ratios of less-adsorbing to more-adsorbing compounds.  $CO_2/CH_4$  mixtures display a high breakthrough capacity due to the high breakthrough time paired with the high working capacity for  $CO_2$  in  $Mg_2(dobdc)$ .  $CH_4/H_2$  is lower due to the lower breakthrough time, despite the similar work-



**Fig. 7.** Adsorption capacity for CO<sub>2</sub> at 313 K in a 1:1:1 CH<sub>4</sub>:CO<sub>2</sub>:H<sub>2</sub> mixture and 1:1 CO<sub>2</sub>:CH<sub>4</sub> and CH<sub>4</sub> in a 1:1 CH<sub>4</sub>:H<sub>2</sub> mixture as a function of the inlet pressure of a packed bed adsorber where the breakthrough is defined as 0.05 mol percent impurity in outlet gas. Closed symbols represent Mg<sub>2</sub>(dobdc) and open symbols represent zeolite 13X. Lines are for visualization purposes only. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

ing capacity. The  $CO_2/CH_4/H_2$  breakthrough capacity shows only the amount of  $CO_2$  adsorbed rather than both  $CO_2$  and  $CH_4$ , illustrating the reduction in  $CO_2$  adsorption in the presence of other gases.

# 3.6. $CO_2/CH_4$ , $CH_4/H_2$ and $CO_2/CH_4/H_2$ selectivity, working capacity and breakthrough performance in zeolite 13X compared to $Mg_2(dobdc)$

Figs. S6–S9 display the selectivity and working capacity of zeolite 13X using the same analysis scenarios described above for Mg<sub>2</sub>(dobdc) and shown in Figs. 2–5. This zeolite was chosen for comparison because it has an exceptionally high CO<sub>2</sub> capacity [70] and breakthrough performance [71] compared to other zeolites. High-pressure adsorption isotherms for CO<sub>2</sub>, CH<sub>4</sub>, and H<sub>2</sub> in zeolite 13X have been reported previously [53].

In every case, Mg<sub>2</sub>(dobdc) outperforms zeolite 13X. The three selectivities shown in Fig. S6 resemble those in Fig. 2, but are 75–50% lower. The three working capacity traces are approximately half of those of Mg<sub>2</sub>(dobdc). Fig. S7 shows the CH<sub>4</sub>/H<sub>2</sub> selectivity displays a clear trend of decreasing selectivity between 10 and 6 from 2% to 98% CH<sub>4</sub>. This can preliminarily be ascribed to a modestly higher pressure dependence in CH<sub>4</sub>/H<sub>2</sub> selectivity for zeolite 13X compared to Mg<sub>2</sub>(dobdc). Fig. S8 displays the CO<sub>2</sub>/ CH<sub>4</sub> selectivity decreases with increasing CO<sub>2</sub> partial pressure, here approaching a value of 20 rather than 57.

The working capacity of zeolite 13X is approximately half that of  $Mg_2(dobdc)$  for all separations evaluated. In all three cases of breakthrough adsorption,  $Mg_2(dobdc)$  adsorbs approximately double the amount of gas as zeolite 13X with slightly higher breakthrough times. The difference in working capacity can explain this behavior. The supporting information includes video animations of the breakthrough behavior of 1:1 CO<sub>2</sub>:CH<sub>4</sub> and CH<sub>4</sub>:H<sub>2</sub> mixtures and a 1:1:1 CH<sub>4</sub>:CO<sub>2</sub>:H<sub>2</sub> mixture for both  $Mg_2(dobdc)$ and zeolite 13X. In all of these high pressure breakthrough cases,  $Mg_2(dobdc)$  outperforms zeolite 13X significantly.

# 4. Conclusions

Here, we have presented the experimental single-component  $CH_4$  adsorption behavior of  $Mg_2$ (dobdc). Together with previously

reported CO<sub>2</sub> and H<sub>2</sub> isotherms, we experimentally evaluated this material for high-pressure gas separations performance. Binary CO<sub>2</sub>/CH<sub>4</sub> and CH<sub>4</sub>/H<sub>2</sub> as well as ternary CO<sub>2</sub>/CH<sub>4</sub>/H<sub>2</sub> mixtures were examined by applying the Ideal Adsorbed Solution Theory to these pure component isotherms. The selectivity and working capacity of Mg<sub>2</sub>(dobdc) render this material promising for all of these high pressure separations, where it offers significant improvements over the competing material zeolite 13X. Further work on the industrial applicability of Mg<sub>2</sub>(dobdc) could involve substantiating prior calculations wherein the use of Mg<sub>2</sub>(dobdc) as a membrane for high pressure gas separations was investigated [67].

Additionally, experimentally evaluating Mg<sub>2</sub>(dobdc) for its performance under regeneration conditions is pertinent. We expect Mg<sub>2</sub>(dobdc) to perform as well or better than zeolite 13X due to the isosteric heat of adsorption of CO<sub>2</sub> onto the two materials. Between 0 and 6 mmol/g, zeolite 13X decreases from approximately 50 to 37 kJ/mol [72], where Mg<sub>2</sub>(dobdc) decreases from approximately 42 to 38 kJ/mol [3]. More specifically, the strengths of the interaction at the assumed purge pressure of 1 bar are 46 and 41 kJ/mol for zeolite 13X and Mg<sub>2</sub>(dobdc), respectively. At higher loadings, the heat of adsorption on Mg<sub>2</sub>(dobdc) decreases even further after a steep drop in heat at 8 mmol/g where 1 CO<sub>2</sub> per Mg<sup>2+</sup> site is achieved. Despite the promising regeneration capability these data suggest, laboratory regeneration experiments are necessary to determine the usefulness of this material in an industrial setting.

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#### Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.micromeso.2011.09.004.

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