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In silico screening of zeolite membranes for $CO₂$ capture

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ABSTRACT

The separation of CO_2/H_2 , CO_2/CH_4 , and CO_2/N_2 mixtures is of practical importance for CO_2 capture and other applications in the processing industries. Use of membranes with microporous layers of zeolites, metal–organic frameworks (MOFs), and zeolitic imidazolate frameworks (ZIFs) offer considerable promise for use in such separations. In view of the extremely wide variety of available microporous structures, there is a need for a systematic screening of potential candidates in order to obtain the best permeation selectivities, S_{perm} . The permeation selectivity is a product of the adsorption selectivity, S_{ads} , and the diffusion selectivity, S_{diff} , i.e. $S_{\text{perm}} = S_{\text{ads}} \times S_{\text{diff}}$. For maximizing S_{perm} , we need to choose materials for which S_{ads} and S_{diff} complement each other.

For a wide variety of zeolites, we have used Configurational-Bias Monte Carlo (CBMC) simulations of mixture adsorption isotherms, along with Molecular Dynamics (MD) simulations of diffusivities for three binary mixtures, CO_2/H_2 , CO_2/CH_4 , and CO_2/N_2 , to calculate S_{ads} , S_{diff} , and S_{perm} . These simulation results provide insights into the influence of pore size, pore topology and pore connectivity that influences each of the three selectivities. In particular, we emphasize the important role of correlations in the diffusion behaviors within microporous materials. Furthermore, we have constructed Robeson plots for each of the separations in order to provide generic guidelines to the choice of materials that offer the appropriate compromise between S_{perm} and the membrane permeability.

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1. Introduction

Three $CO₂$ separation issues are considered to hold the greatest promise for reducing $CO₂$ emissions [\[1\]. F](#page-9-0)irstly, we have the problem of separating $CO₂$ and $N₂$ from power plant flue gas streams; this is also termed post-combustion processing. Secondly, in precombustion processing of syngas mixtures, $CO₂$ and $H₂$ need to be separated. Thirdly, there is the issue of sweetening of sour natural gas, involving separation of $CO₂$ and $CH₄$. D'Alessandro et al. [\[1\]](#page-9-0) present a comprehensive survey of the variety of technologies for $CO₂$ capture. On the basis of available information it appears that adsorptive and membrane separations using zeolites, metal–organic frameworks (MOFs), zeolitic imidazolate frameworks (ZIFs), and carbon nanotubes (CNTs) offer energy efficient alternatives to more conventional separation techniques such as amine absorption [\[1–5\].](#page-9-0)

[Fig. 1](#page-1-0) illustrates the wide variety of channel topologies and connectivities encountered in zeolites, MOFs, ZIFs, and CNTs. These include: one-dimensional (1D) channels (e.g. AFI, LTL, TON, MTW, CNTs, MIL-47, MIL-53(Cr)), 1D channels with side pockets (e.g. MOR), intersecting channels (e.g. MFI, BEA, ISV, GME, BOG), large cavities with large windows (e.g. FAU, NaX, NaY, IRMOF-1, CuBTC), and cages separated by narrow windows (e.g. LTA, LTA-5A, LTA-4A, CHA, DDR, TSC, ERI, ITQ-29, ZIF-8). The channel or cavity sizes of all of these structures are in the 0.3–2 nm range.

The adsorbent, or microporous membrane layer, with the highest selectivity for a given $CO₂$ separation duty can be selected on the basis of screening of available microporous structures. Palomino et al. [\[6\],](#page-9-0) for example, have presented an experimental investigation comparing the $CO₂/CH₄$ adsorption selectivity for various cation-exchanged LTA zeolites with ZIFs and MOFs. Experimental screening of potential adsorbents is very time consuming. An alternative approach, as underlined in several recent investigations, is to harness the power of molecular simulation techniques for screening purposes [\[7–17\]. M](#page-9-0)olecular simulations can be very useful in narrowing down the choices to a handful of promising structures than can be subsequently subjected tomore thorough experimental investigations.

Most, if not all, of the screening studies using molecular simulations have focused on the adsorption selectivity, S_{ads} , defined by

$$
S_{\rm ads} = \frac{c_1/c_2}{f_1/f_2} \tag{1}
$$

where the c_i represent the pore concentrations in equilibrium with a bulk fluid phase with partial fugacities f_i . We choose to use

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Fig. 1. Examples of the variety of channel topologies and connectivities in zeolites, MOFs, ZIFs, and CNT. Details of the specific structures are available in the [Supplementary](#page-9-0) [Material](#page-9-0) accompanying this article.

fugacities, f_i , in Eq. [\(1\)](#page-0-0) instead of partial pressures, p_i , because in many cases of $CO₂$ capture the pressures encountered are high, in the 1–6 MPa range, and thermodynamic non-idealities are nonnegligible. Furthermore, in molecular simulations performed in the grand canonical ensemble, the f_i are directly accessible.

For membrane processes, the main focus of the present communication, it is of relevance to examine the permeation selectivity, S_{perm} , defined by

$$
S_{\text{perm}} = \frac{N_1/N_2}{f_1/f_2} \tag{2}
$$

where the N_i are the permeation fluxes across the membrane for partial gas phase fugacities f_i in the upstream membrane compartment. For microporous membranes, the permeation fluxes are most conveniently described using the Maxwell–Stefan (M–S) equations [\[17–20\]](#page-10-0)

$$
-\phi \frac{c_i}{RT} \nabla \mu_i = \sum_{\substack{j=1 \ j \neq i}}^2 \frac{c_j N_i - c_i N_j}{c_t \mathbf{b}_{ij}} + \frac{N_i}{\mathbf{b}_i}, \quad i = 1, 2
$$
 (3)

where ϕ represents the fractional pore volume of the microporous crystalline material, and the concentrations c_i are defined in terms of accessible pore volume of the crystalline microporous layer.

The D_1 and D_2 are the M-S diffusivities of the pure components 1 and 2; these represent the interactions between the component species and the pore walls. For any guest species, the D_i values vary by several orders of magnitude depending on the pore size and topology; they are also dependent on the loading or concentration within the pores as is illustrated for diffusivity of $CO₂$ in a variety of microporous structures; see [Fig. 2a](#page-2-0). The channel size is an important determinant for the magnitude of the diffusivity; for the chosen structures, the highest selectivity is for MIL-53(Cr) that has 8.5 Å sized channels, while the lowest diffusivity is for DDR that has cages separated by windows that are 3.6×4.4 Å in size. Consider the three structures FAU, NaY (54 Na⁺), and NaX (86 Na⁺) that have the same pore topology with pore size of 7.4 Å, but with increasing number of cations. Increasing the number of cations increases the

adsorption strength of $CO₂$, due to increased electrostatic interactions. This is witnessed by the pure component isotherms in [Fig. 2b.](#page-2-0) The D_i values for CO_2 have the inverse hierarchy FAU > NaY > NaX; this is because the "sticking tendency" increases with adsorption strength leading to lower diffusivities [\[17\]. A](#page-10-0) higher sticking tendency, implies a lower mobility.

The D_{12} are exchange coefficients that capture correlation effects in molecular jumps from one adsorbed site to another. The ratios D_1/D_{12} and D_2/D_{12} quantify the degree of correla-tions [\[17,19,20\]. F](#page-10-0)or any guest mixture, the ratios D_1/D_2 , D_1/D_{12} , and D_2/D_{12} vary over several orders of magnitude depending on the pore size, topology, and connectivity of the host struc-ture. To illustrate this, [Fig. 2c](#page-2-0) compares the values of D_1/D_{12} for $CO₂(1)/H₂(2)$ mixture diffusion in variety of structures. Onedimensional structures such as MTW, and TON have the highest degree of correlations. This is followed by the intersecting channel structure of MFI, and the large pore FAU structure. The lowest degree of correlations are encountered in LTA, CHA, DDR, and ERI that have cages separated by narrow 0.32–0.45 nm sized windows. Another point to note is that the degree of correlations generally increases as the concentration inside the pores increases. A qualitative appreciation of the differences in the diffusion characteristics between the various structures can also be appreciated by viewing video animations of MD simulation diffusion that has been provided as [Supplementary Material.](#page-9-0) [Video animations 1–3](#page-9-0) illustrate the "single file" nature of diffusion in 1D channels of TON and MIL-47, leading to strong correlations in molecular jumps. [Video 4](#page-9-0) illustrates the jumps of $CO₂$ and CH₄ in the intersecting channels of MFI; here the intersections act as "traffic junctions" serving to increase the degree of correlations between jumps $CO₂$ and $CH₄$. [Videos 5 and 6](#page-9-0) give a feel for diffusion of $CO₂$ and $CH₄$ within the "open" structures of NaY and NaX, also showing interactions with mobile cations.[Videos 7–12](#page-9-0) given an appreciation of the hopping of guest molecules across the narrow windows of LTA, CHA, DDR, and ZIF-8. We note that only one molecule at a time can pass a window, causing the diffusion process to be practically uncorrelated.

The permeation selectivity can be expressed as

$$
S_{\text{perm}} = S_{\text{ads}} \times S_{\text{diff}} \tag{4}
$$

Fig. 2. (a) M-S diffusivity D_i , from MD simulations for pure CO₂ in a variety of microporous materials a function of c_i . (b) CBMC simulation data for isotherms of CO₂ in a variety of microporous materials. (c) The degree of correlations, B_1/B_{12} , for CO₂(1)/H₂(2) mixture diffusion a variety of zeolites. (d) Comparison of the estimations of S_{diff} using Eqs. (5) and (6) for $CO₂/CH₄$ mixture diffusion in all-silica FAU.

where S_{diff} is the diffusion selectivity. Starting with Eq. [\(3\),](#page-1-0) the following expression for S_{diff} can be derived

$$
S_{\text{diff}} = \frac{D_1}{D_2} \frac{1 + (D_2/D_{12})}{1 + (D_1/D_{12})} \tag{5}
$$

As a very good approximation, the right member of Eq.(5) can be taken equal to the ratio of the self-diffusivities $D_{i,s}$ elf in the mixture

$$
S_{\text{diff}} = \frac{D_{1,\text{self}}}{D_{2,\text{self}}} \tag{6}
$$

The detailed derivations of Eqs. (5) and (6) are provided in the [Supplementary Material](#page-9-0) accompanying this publication; see also earlier published work [\[21,22\].](#page-10-0) The use of Eq. (6) is particularly convenient because the $D_{i, self}$ are more easily accessible by use of Molecular Dynamics (MD) simulations than the D_1 , D_2 and D_{12} .

As illustration, Fig. 2d compares the estimations of S_{diff} using Eqs. (5) and (6) for $CO₂/CH₄$ diffusion in all-silica FAU. The agreement between the two sets of results is extremely good.

From the point of view of selecting optimum microporous structures, it is useful to identify two limiting scenarios for the correlations. When correlations are negligibly small, $(D_1/D_{12}) \rightarrow 0$; $(D_2/D_{12}) \rightarrow 0$ either Eq. (5) or (6) degenerates to yield

$$
S_{\text{diff}} = \frac{D_1}{D_2}; \text{ correlations negligible} \tag{7}
$$

This scenario implies that S_{diff} can be estimated on the basis of experimental pure component permeance data. Eq. (7) holds as a good approximation for structures such as CHA, DDR, LTA, TSC, ERI, and ZIF-8 that have cages separated by narrow windows. The molecules hop one-at-a-time across the windows, and the hopping rates are practically uncorrelated.

The other extreme scenario is one in which correlation effects are dominant, i.e. $(b_1/b_{12}) \gg 0$; $(b_2/b_{12}) \gg 0$ yielding

$$
S_{\text{diff}} = 1; \text{ correlations dominant} \tag{8}
$$

When Eq. (8) holds, $S_{\text{perm}} = S_{\text{ads}}$. Eq. (8) holds as a good approximation for 1D channel structures such as CNTs [\[19\].](#page-10-0)

The main objective of the present communication is to highlight the possibilities of enhancing the permeation selectivities by proper choice of the microporous structure that offers the best diffusion selectivities. We shall underline the importance of choosing the structure that has the right degree of correlations for a specified separation application. We shall demonstrate that, for any given separation, we aim to satisfy either Eq. (7) or (8). For illustrating a variety of concepts we consider the separation of three different binary mixtures CO_2/H_2 , CO_2/CH_4 , and CO_2/N_2 that are relevant for $CO₂$ capture. Additionally, a few simulations were also carried out with CH_4/H_2 and CH_4/N_2 mixtures in order to underline the generic applicability of the presented concepts. In all cases, we determined $S_{\rm ads}$ by use of Configurational-Bias Monte Carlo (CBMC) simulations of mixture adsorption. Additionally, S_{diff} was determined from MD simulations of the $D_{i, self}$. The entire data base of simulation results is available in the [Supplementary Material](#page-9-0) accompanying this publication; this material includes details of the CBMC and MD simulation methodologies, details of the microporous structures investigated (unit cell dimensions, accessible pore volume, characteristic pore dimensions), pore landscapes, specification of the force fields used, simulation data on mixture isotherms, S_{ads} , and S_{diff} . Most of the investigated structures are zeolites, chosen carefully to reflect the different classes of pore topologies and connectivities portrayed in [Fig. 1. F](#page-1-0)or comparison purposes we also investigated a few typical MOFs (CuBTC, IRMOF-1, MIL-53), ZIFs (ZIF-68, ZIF-8), and CNTs.

In performing molecular simulations, we assume perfect, defect-free, crystals, and rigid crystalline frameworks. These assumptions are considered to be reasonable for purposes of screening, the focus of the current study. However, for more accurate design purposes, it may be necessary to take other factors into consideration, such as surface resistance or inter-crystalline resistance of crystals [\[23,24\], a](#page-10-0)nd framework flexibility influences [\[25–27\]. F](#page-10-0)ramework flexibility issues are of particular importance when the guest molecules are tightly constrained as for example in inter-cage hopping across the narrow windows of CHA, DDR, LTA, and ZIF-8 [\[28\]. I](#page-10-0)n MOFs such as MIL-53, guest-induced structural transformations may occur, and this needs special analysis [\[29,30\].](#page-10-0)

We begin our discussions by considering the adsorption selectivities.

2. Adsorption selectivities

CO₂ has a larger quadrupole moment (14.3 × 10⁻⁴⁰ Cm²), and a higher polarizability (26.3 × 10⁻²⁵ cm³) than any of the partner molecules H_2 , CH₄, and N₂. Consequently, CO₂ has the higher adsorption strength in all three mixtures. As illustration, Fig. 3 shows the CBMC simulations of the component loadings in NaX zeolite for $CO_2(1)/N_2(2)$ mixtures in equilibrium with a bulk fluid phase, with partial fugacities f_1/f_2 = 15/85. For a fair comparison of the loadings in various structures, it is necessary to express the loadings, c_i , in terms of moles per $m³$ of accessible pore volume [\[17,20,31\]. I](#page-10-0)n this context, it is worth pointing out that many microporous structures contain pockets or cages that are not accessible in experiments. In CBMC simulations, it is important to block such regions in order to obtain a fair representation of experimental reality [\[32\].](#page-10-0) For example, the sodalite cages in LTA, ITQ-29, FAU, TSC need to be blocked as these are inaccessible to guest molecules. Also, DDR zeolite contains pockets that need blocking [\[32,33\]. T](#page-10-0)he molecular simulation screening study of Liu and Smit [\[11\]](#page-10-0) must be treated with caution because the inaccessible pockets of LTA and DDR were not blocked [\[32\]. F](#page-10-0)or every structure, the accessible pore volume was determined with the aid of molecular simulations

Fig. 3. CBMC simulations for the component loadings c_i in equilibrium with binary fluid phase mixtures $CO_2(1)/N_2(2)$ in NaX (106 Si, 86 Al, 86 Na⁺, Si/Al = 1.23) at 300 K. The partial fugacities in the bulk fluid phase are such that $f_1/f_2 = 15/85$. The complete set of CBMC data for all mixtures in all microporous hosts available in the [Supplementary Material](#page-9-0) accompanying this publication.

using the helium probe insertion technique suggested by Talu and Myers [\[34,35\]. T](#page-10-0)he details of the technique used and the pore volume data are provided in the [Supplementary Material, w](#page-9-0)hich also contains data such as that shown in Fig. 3 for all guest mixtures in all the chosen host materials.

From the CBMC simulated component loadings, the adsorption selectivities, S_{ads} , can be calculated by use of Eq. [\(1\).](#page-0-0) Let us first consider S_{ads} for CO_2/H_2 mixtures; this problem is encountered in pre-combustion applications. Fig. 4a summarizes the adsorption

Fig. 4. Adsorption selecivities, S_{ads} , for (a) $CO_2(1)/H_2(2)$, (b) $CO_2(1)/CH_4(2)$, and (c) $CO₂(1)/N₂(2)$ mixtures in a variety of microporous materials, plotted as a function of the total bulk fluid phase fugacity, $f_t = f_1 + f_2$. For clarity of presentation, only a selection of the simulation data are presented here; the complete set of data are available in the [Supplementary Material](#page-9-0) accompanying this publication.

selectivities, S_{ads} , for $CO_2(1)/H_2(2)$ mixtures as a function of the total gas phase fugacity, $f_t = f_1 + f_2$. In all structures $S_{ads} \gg 1$. The highest S_{ads} is obtained with NaX (86 Na⁺). Comparing the S_{ads} values for the same FAU topology we find the following hierarchy NaX (86 Na⁺) \gg NaY (54 Na⁺) \gg FAU (all-silica). A similar hierarchy

Fig. 5. Adsorption selecivities, S_{ads} , for (a) $CO₂(1)/H₂(2)$, (b) $CO₂(1)/CH₄(2)$, and (c) $CO₂(1)/N₂(2)$ at a total bulk fluid phase fugacity $f_t = 1$ MPa, plotted as a function of the pore volume of the microporous material.

holds for $CO_2(1)/CH_4(2)$ and $CO_2(1)/N_2(2)$ mixtures; see [Fig. 4b](#page-3-0) and c. These data underline the strong increase in S_{ads} with increasing number of cations present. This increase is to be attributed to enhanced electrostatic interactions of the cations with $CO₂$. The significant role of electrostatic interactions for $CO₂$ adsorption has been underlined in the literature [\[11,16\]. T](#page-10-0)he adsorption selectivities are also enhanced by incorporation of special functional groups within a framework. For example, the work of Couck et al. [\[36\]](#page-10-0) demonstrates that functionalizing the MIL-53(Al) metal–organic framework with amino groups increases its selectivity in $CO₂/CH₄$ separations by orders of magnitude while maintaining a very high capacity for $CO₂$ capture. An and Rosi [\[37\]](#page-10-0) demonstrate the possibility of enhancing the $CO₂$ adsorption selectivity in MOFs by introduction of cations.

In a recent simulation study of RHO-zeolite-like metal–organic framework, Babarao and Jiang [\[38\]](#page-10-0) found extremely high selectivities, significantly higher than 50, for $CO₂/H₂$, $CO₂/CH₄$, and $CO₂/N₂$ adsorption due to electrostatic interactions of $CO₂$ with the charges of the anionic framework atoms and charge-balancing extra-framework Na⁺ ions. Their selectivity values for rho-ZMOF are also plotted in [Fig. 4a–](#page-3-0)c. It is interesting to note that for total gas phase fugacities, f_t , exceeding 0.2 MPa, NaX and NaY exhibit values of S_{ads} that are higher than that for rho-ZMOF. The statement of Babarao and Jiang [\[38\]](#page-10-0) in their paper "The predicted selectivities in rho-ZMOF are the highest reported to date among various MOFs and unprecedentedly higher than those for other porous materials" needs to be revised in light of the data presented in this work.

Fig. 5 presents a comparison of S_{ads} for the three mixtures at total bulk fluid phase fugacity $f_t = 1$ MPa, typical of several CO₂ capture technologies, using the pore volume V_p of the various microporous materials on the x-axis. Such a comparison is useful from a practical point of view, because V_p is a reflection of the capacity of material for adsorption. The upper right corner of these plots are the desirable regions, with both high selectivities and high capacities for adsorbing guest molecules. NaX, NaY, and rho-ZMOF are three structures that emerge as the best ones using this criterion. It is of particular practical interest to note that the best adsorption selectivities are obtained with a widely used commercial adsorbent such as NaX.

3. Diffusion and permeation selectivities

The diffusion selectivity S_{diff} is dictated by a variety of factors that include molecular dimensions, pore size, connectivity, and adsorption strength. Fig. 6 presents cartoons showing approximate molecular dimensions of the gases investigated in this work;

Fig. 6. Cartoon showing the approximate molecular dimensions of CO_2 , H_2 , N_2 , and CH4. The molecular diameters are estimated on the basis of the Lennard–Jones size parameters σ for molecule–molecule interactions. The molecular lengths are estimated on the basis of the bond lengths.

Fig. 7. (a) Comparison of diffusion selectivities, S_{diff} , for equimolar ($c_1 = c_2$) CO₂/H₂ mixtures at 300 K, plotted as a function of the total pore concentration $c_t = c_1 + c_2$. (b) Permeation selectivities, S_{perm} , for CO_2/H_2 mixtures, plotted against the total bulk gas phase fugacity, f_t .

these dimensions were estimated using published force fields for molecule–molecule interactions [\[39–43\]. T](#page-10-0)he cartoons will be helpful in appreciating the trends in the S_{diff} that invariably do not go hand-in-hand with S_{ads} .

3.1. $CO₂/H₂$ mixtures

Due to the much smaller molecular size of H_2 molecules, the S_{diff} in all microporous structures is lower than unity, as witnessed by MD simulation results for equimolar (i.e. $c_1 = c_2$) CO₂(1)/H₄(2) mixtures in Fig. 7a. For the same FAU topology we find the S_{diff} values for FAU, NaY, and NaX to be 0.24, 0.055, and 0.018 for a pore concentration of 10 kmol m⁻³, a hierarchy that is opposite to that for S_{ads} . Increasing adsorption strength by enhancing the electrostatic interactions of $CO₂$ with Na⁺ has the effect of reducing the mobility of $CO₂$ due to increased "sticking" tendency [\[17\]. T](#page-10-0)his is true in most cases, and for membrane permeation this essentially means that S_{diff} counteracts the gain in S_{ads} . Also shown in Fig. 7a are the S_{diff} values for a fluid mixture at the same molar concentration as within the pores. The value of S_{diff} for a fluid mixture is an "upper bound" and provides a target of $CO₂$ -selective operations. If we aim for a membrane separation process that is selective to $CO₂$, we should choose micropore topologies that yield S_{diff} values as close to the fluid mixture value as possible. This is achievable by choosing structures in which the degree of correlations are very strong, and for which the differences in the mobilities of $CO₂$ and $H₂$ get washed out. One-dimensional channel structures such as CNT, TON and MTW allow this possibility. Indeed we find that for TON, S_{diff} is very close to that of the fluid mixture. [Video 1](#page-9-0) gives a visual appreciation of the high degree of correlations in TON; the more mobile H_2 cannot bypass the tardier CO_2 , and "single file" diffusion prevails.

We can combine the information presented in [Figs. 4a and 7a](#page-3-0) to obtain the S_{perm} , using Eq. [\(4\). F](#page-1-0)or this purpose, the S_{diff} values are determined at the total fluid concentration $c_t = c_1 + c_2$, with the component loadings c_i from data such as shown in [Fig. 3. T](#page-3-0)he S_{perm} , plotted in Fig. 7b, reflect a balance between the S_{ads} and S_{diff} . For an upstream membrane fugacity $f_t = 1$ MPa, typical for pre-combustion separations $[1]$, the zeolites with the highest S_{perm} are obtained with NaY, NaX, TON, MTW, and MFI.

From a membrane process development viewpoint, a more appropriate approach is not to select membranes based just on S_{perm} , but to also consider the $CO₂$ permeability of the membrane, Π_i , defined by

$$
\Pi_i = \frac{N_i}{\Delta f_i / \ell} \tag{9}
$$

where ℓ is the thickness of the crystalline layer on the membrane. If the downstream conditions are such that the loadings are negligibly small, the $CO₂$ permeability can be determined from MD simulations by using the following expression

$$
\Pi_i = \frac{\phi D_{i,\text{self}} c_i}{f_i} \tag{10}
$$

where c_i is the pore concentration of CO_2 at the upstream face of the membrane. Detailed derivations of Eq. (10) are provided in the [Supplementary Material. F](#page-9-0)or a chosen upstream total fugacity f_t = 1 MPa, the conventionally used Robeson plot [\[44\]](#page-10-0) can be constructed in which the permeation selectivities are plotted against the CO₂ permeability, Π_i , expressed in Barrers; see Fig. 8. NaY offers the best combination of S_{perm} and Π_i . The good performance of NaY can be attributed to three different reasons: (1) high S_{ads} due to electrostatic interactions of $CO₂$ with cations, (2) high permeability due to the large and "open" pore structure, and (3) high degree of correlations in such open structures. For the same set of reasons, we should also expect a material such as amine functionalized MIL-53 to offer comparable performance in terms of S_{perm} and Π_i . The 1D channels of MIL-53 offer a high degree of correlations that are desirable [\[17\]. F](#page-10-0)or use of 1D channel structures in membrane permeation devices, there is however a practical issue relating to the orientation, and alignment of all 1D channels.

Fig. 8. Robeson plot for separation of $CO₂/H₂$ mixtures, with total upstream fugacity f_t = 1 MPa, and T = 300 K. The permeation selectivities, S_{perm} , for different microporous structures are plotted against the $CO₂$ permeability, Π_i . Note that the x-axis is expressed in 104 Barrers.

A different approach is to aim for a $H₂$ -selective membrane separation. This is possible if we allow S_{diff} to overpower S_{ads} by choosing microporous structures that act as H_2 -sieves. One candidate structure is ZIF-8 that is a structural analog of SOD zeolite. The windows separating the cages are about 0.34 nm in size [\[45,46\],](#page-10-0) allowing

Fig. 9. (a) Snapshot showing the location of CO₂ and H₂ within a ZIF-8 cage. (b) Comparison of S_{ads} for separation of $CO₂/H₂$ mixture at 300 K, 373 K, and 500 K in ZIF-8. (c) Comparison of S_{ads} , S_{diff} , and S_{perm} , for separation of CO_2/H_2 mixture at 500 K in ZIF-8.

 $H₂$ to diffuse through much more easily than $CO₂$; see snapshot in Fig. 9a. For this strategy to be more effective, it is advantageous to operate at higher temperatures, where the adsorption selectivity in favor of $CO₂$ is reduced; see Fig. 9b. At a temperature of 500 K, the comparison of S_{ads} , S_{diff} , and S_{perm} , is shown in Fig. 9c. We note that H_2/CO_2 permeation selectivities of the order of 50 are anticipated by a combination of CBMC and MD simulations. There is recent experimental evidence in the literature to confirm that such a $H₂$ -selective separation is possible with ZIF-7, that has a structure similar to that of ZIF-8 [\[47\].](#page-10-0) [Video 11](#page-9-0) illustrates the rapid inter-cage hopping of $H₂$ across the windows of ZIF-8, while CO₂ can be seen to be predominantly engaged in intra-cage hops.

3.2. CH4/H2 mixtures

The foregoing concepts and considerations for $CO₂/H₂$ mixtures also apply to CH_4/H_2 separations, relevant for H_2 recovery from fuel gas or natural gas streams. For CH4-selective separation, we should aim for 1D structures with a high degree of diffusional correlations. Carbon nanotubes are excellent choices in this regard, and this is evidenced by molecular simulation results for CH_4/H_2 permeation selectivities that are summarized in Fig. 10a. The earlier studies of Chen and Sholl [\[48\]](#page-10-0) also confirm the efficacy of CNTs for this task. Structures such as ZIF-8, LTA, and CHA, that have narrow windows separating cages, allow $H₂$ -selective permeation and there is

Fig. 10. Comparison of S_{perm} for separation of (a) CH_4/H_2 , and (b) CH_4/N_2 mixtures at 300 K in a variety of microporous structures.

experimental evidence of such separations in the published literature [\[45,46,49\].](#page-10-0) [Video 12](#page-9-0) illustrates the rapid inter-cage hopping of H_2 across the windows of ZIF-8, while CH₄ can be seen to be predominantly engaged in intra-cage hops.

3.3. $CH₄/N₂$ mixtures

Nitrogen is a common contaminant in natural gas, and requires removal because it reduces the calorific value of the fuel and makes it unsaleable. For CH_4/N_2 separations, the permeation selectivity is in favor of $CH₄$ in microporous structures such as TON, MTW, and MFI in which diffusional correlation effects are significantly high; see [Fig. 10b](#page-6-0). Conversely, for structures such as LTA and CHA, for which correlation effects are negligibly small, the permeation selectivities are in favor of N_2 . Experimental data [\[49\]](#page-10-0) for CH_4/N_2 permeation across a SAPO-34 membrane, an iso-type of CHA, confirm the predictions of [Fig. 10b](#page-6-0).

3.4. $CO₂/N₂$ mixtures

The molecular sizes of $CO₂$ and N₂ are comparable (cf. [Fig. 6\),](#page-4-0) and consequently the diffusion selectivities in a given material are higher than for $CO₂/H₂$ mixtures. The hierarchy of S_{diff} is however the same as for CO_2/H_2 mixtures. The S_{perm} values, along with the Robeson plot, are summarized in Fig. 11a and b. Our S_{perm} estimate for MFI of 8.2 is in reasonable agreement with the experiments

Fig. 11. (a) Permeation selectivities, S_{perm}, for CO₂/N₂ mixtures, plotted against the total bulk gas phase fugacity, f_t . (b) Robeson plot for separation of CO_2/N_2 mixtures, with total upstream fugacity f_t = 1 MPa, and T = 300 K. The permeation selectivities, S_{perm} , for different microporous structures are plotted against the $CO₂$ permeability, Π_i . Note that the x-axis is expressed in 10⁴ Barrers. Also plotted is the "upper bound" calculated using the parameters specified in Table 12 of Robeson [\[44\].](#page-10-0)

of Bernal et al. [\[50\].](#page-10-0) The best combination of S_{perm} and Π_i . values are obtained with NaX and NaY zeolites, a conclusion that is essentially the same as for CO_2 -selective CO_2/H_2 separation. There is evidence that the predicted permeation selectivities for NaY can indeed be realized in experiments [\[51–54\]. T](#page-10-0)his is useful from practical view point because for $CO₂$ -selective separation of pre- and post-combustion processes the same material (i.e. NaY) works the best, and therefore process development can be focused on just one material. However, N_2 -selective separation of CO_2/N_2 does not appear to be feasible.

3.5. $CO₂/CH₄$ mixtures

Let us now analyze the diffusional selectivities for $CO₂/CH₄$ mixtures. In 1D channels, intersecting channels, and open structures for which the pore sizes are larger than about 0.55 nm, the diffusion selectivities S_{diff} < 1; see Fig. 12a. This is mainly due to the fact that the higher adsorption strength of $CO₂$, lowers its mobility within the micropores.

 $CO₂$ is a more slender molecule than CH₄ (cf. [Fig. 6\) a](#page-4-0)nd a different scenario holds for ERI, CHA, ITQ-29, DDR, TSC, and LTA. For these structures, the S_{diff} is significantly higher than unity; see Fig. 12b. This is because the linear $CO₂$ molecule hops length-wise across the narrow 0.35–0.45 nm sized windows. This is best evidenced by viewing the animations in [Videos 7–11](#page-9-0) for LTA, DDR, and CHA zeolite. Furthermore, the preferential location of $CO₂$ at the window regions of LTA, and DDR serves to hinder the inter-cage hopping of CH₄; this explains why $S_{\text{diff}} \gg 1$ [\[55,56\]. T](#page-10-0)he hierarchy of S_{diff} in Fig. 12b is dictated, broadly speaking, by the hierarchy of window

Fig. 12. (a and b) Comparison of diffusion selectivities, S_{diff} , for equimolar ($c_1 = c_2$) $CO₂/CH₄$ mixtures at 300 K plotted as a function of the total pore concentration $c_t = c_1 + c_2$. For clarity of presentation only a selection of the simulation data are presented here; the complete set of data are available in the [Supplementary Material](#page-9-0) accompanying this publication.

Fig. 13. (a) Permeation selectivities, S_{perm} , for CO_2/CH_4 mixtures, plotted against the total bulk gas phase fugacity, f_t . (b) Robeson plot for separation of CO_2/CH_4 mixtures, with total upstream fugacity f_t = 1 MPa, and T = 300 K. The permeation selectivities, S_{perm} , for different microporous structures are plotted against the $CO₂$ permeability, $\overline{\Pi}_i$. Note that the x-axis is expressed in 10⁴ Barrers. Also plotted is the "upper bound" calculated using the parameters specified in Table 12 of Robeson [\[44\].](#page-10-0)

sizes; the smaller the window size, the higher is the value of S_{diff} . Unlike for the four foregoing mixtures discussed above, there is a possibility of enhancing S_{perm} by choosing topologies such as ERI, CHA, ITQ-29, DDR, TSC, and LTA in which correlation effects are negligible.

The permeation selectivities S_{perm} , plotted in Fig. 13a, reflect the combined influences of adsorption and diffusion. For an upstream membrane fugacity $f_t = 1$ MPa, typical of natural gas sweetening applications, the S_{perm} > 100 are obtained with ERI, DDR, and CHA. For DDR and CHA, there is experimental evidence that such high permeation selectivities can be realized in practice [\[49,56–61\]. F](#page-10-0)or MFI, the S_{perm} value of 2.3 is in agreement with experiment [\[60\].](#page-10-0) Fig. 13b presents the Robeson plot for $CO₂/CH₄$ mixture separation in all the microporous structures that we have investigated. Open, large pore, structures such as FAU, MIL-53, IRMOF-1, and CuBTC have high Π_i but low S_{perm}. On the other hand, ERI, DDR, and CHA have significantly higher S_{perm} values but with lower Π_i . For technological applications, a compromise has to be struck. The compromise structure could perhaps be NaY with a relatively high permeability, or CHA, with a high S_{perm} . There is considerable scope for development of novel materials that would lead to a performance at the top right corner. The strategy should be to aim to develop frameworks such as MIL-53, with 1D channels in which strong functional groups are attached to ensure strong $CO₂$ adsorption.

It is also interesting to note that for both $CO₂/N₂$ and $CO₂/CH₄$ separations, the separation performance of a few zeolites exceeds the upper bound of Robeson [\[44\]; s](#page-10-0)ee [Figs. 11b and 13b.](#page-7-0)

3.6. Comparison with experimental data

It remains to provide experimental proof that the predictions of the permeation selectivity trends using molecular simulations are a fair reflection of actual experimental data. Fig. 14a presents a collection of the experimental data of Li et al. [\[49,60\]](#page-10-0) on permeation selectivities, S_{perm} , for CO₂/CH₄, CO₂/N₂, CO₂/H₂, CH₄/N₂,

Fig. 14. (a) Permeation selectivities, S_{perm} , for CO_2/CH_4 , CO_2/N_2 , CO_2/H_2 , CH_4/N_2 , and CH4/H2 mixtures obtained from experimental data of Li et al. [\[49,60\]](#page-10-0) for SAPO-34 membrane at 295 K. (b) Permeation selectivities, S_{perm}, from molecular simulations (CBMC, and MD) for CHA at 300 K. (c) Estimations of S_{perm} using the pure component SAPO-34 membrane permeation data, along with the negligible correlations scenario, Eq. [\(7\). F](#page-2-0)urther information on the SAPO-34 modeling is provided in the [Supplementary Material.](#page-9-0)

and $CH₄/H₂$ mixtures across a SAPO-34 membrane at 295 K. SAPO-34 is an iso-type of CHA zeolite, and therefore these data can be compared with molecular simulations of S_{perm} for CHA for the corresponding mixtures; see [Fig. 14b.](#page-8-0) We note that molecular simulations predict the right order of magnitudes for the separation selectivities, along with the correct hierarchy of values for the various mixtures. These results lend confidence in the use of molecular simulations for screening purposes.

For membrane design and development purposes, better estimates of the permeation fluxes and selectivities are obtained by using M–S diffusivities D_i that are backed out from unary permeation data, along with experimental pure component isotherms. Using this procedure, described in detail in our earlier work [\[49,59–61\],](#page-10-0) the calculations of the permeation selectivities for SAPO-34 are presented in [Fig. 14c.](#page-8-0) The agreement of these calculations with the experimental data is better, as is to be expected. In this context, we also draw attention to the recent model of van den Bergh et al. [\[62\].](#page-10-0)

For more accurate modeling of membrane permeation, there may be a need to also account for inter-crystalline and grain boundary resistances in the polycrystalline membrane layers.

4. Conclusions

With the aid of CBMC and MD simulations we have examined the adsorption, diffusion, and permeation selectivities for separation of $CO₂/H₂$, $CO₂/CH₄$, $CO₂/N₂$, $CH₄/N₂$ and $CH₄/H₂$ mixtures using a wide variety of microporous structures, mainly consisting of zeolites. Our investigations provide guidelines to the optimum choice of microporous layers to be used in membrane separations that represent the optimum compromise between S_{perm} and the permeability Π_i . Specifically, the following major conclusions can be drawn.

- (1) For CO_2 -selective separation of CO_2/H_2 mixtures we should aim for microporous structures that have a high degree of correlations, washing out differences in the mobilities of $CO₂$ and $H₂$ molecules. The optimum structure with the best balance between permeation selectivity and permeability is determined to be NaY.
- (2) For CO₂-selective separation of CO₂/N₂ mixtures, NaY zeolite again offers the best balance between S_{perm} and permeability.
- (3) For H₂-selective separation of $CO₂/H₂$ mixtures, a different strategy needs to be adopted by choosing structures such as ZIF-8 with narrow windows separating cages. The diffusional correlations are negligibly small, and the narrow 0.34 nm result in high S_{diff} values, that overpower the adsorption selectivity in favor of CO₂.
- (4) For CO₂ removal from CO₂/CH₄ mixtures the highest S_{perm} are obtained with structures such as ERI, CHA, ITQ-29, and DDR that have narrow 0.35–0.45 nm sized windows separating cages. In such zeolites, the correlation effects are negligibly small. Due to the slenderness of the $CO₂$ molecules, its diffusivities are higher than for partner molecules. For these frameworks, S_{diff} serves to significantly enhance permeation selectivities above the S_{ads} values. The disadvantage of the aforementioned structures is the low permeability, and if the latter is the more desirable property a NaY membrane is a reasonable compromise.
- (5) For both CO_2/N_2 and CO_2/CH_4 separations, the separation performance of a few zeolites exceeds the upper bound of Robeson [\[44\].](#page-10-0)

We believe that the results presented in this article will help in the development of the appropriate microporous membrane technology for $CO₂$ capture, by appropriate choice of the pore topology with the right degree of diffusional correlations.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at [doi:10.1016/j.memsci.2010.05.032.](http://dx.doi.org/10.1016/j.memsci.2010.05.032)

Nomenclature

- μ_i molar chemical potential (J mol⁻¹)
- Π_i , permeability of species *i* across membrane (Barrer)

Subscripts

i referring to component i

t referring to total mixture

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