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# Microporous and Mesoporous Materials



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# Molecular dynamics investigation of the self-diffusion of binary mixture diffusion in the metal-organic framework Zn(tbip) accounting for framework flexibility

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## 1. Introduction

Molecular dynamics (MD) simulation is a powerful technique widely used to obtain detailed information on structure and dynamics of the guest molecules in microporous materials such as zeolites and MOFs [\[1\].](#page-6-0) However, most of the simulations are often performed with the assumption that the framework is rigid. This assumption is a reasonable approximation for zeolites [\[2,3\].](#page-6-0) The situation with MOFs is somewhat different. Using rigid and flexible framework, the loading dependence of the self-diffusion coefficient of ethane in metal-organic framework (MOF) of type Zn(tbip) shows surprising effects arising from the lattice flexibility [\[4,5\]](#page-6-0) in comparison to the rigid model. Lattice flexibility increases the self-diffusivities and also leads to a maximum at intermediate loadings. In contrast, for IRMOF-1 it had been shown that the selfdiffusivities of several guest molecules were not much influenced by the lattice flexibility [\[6\].](#page-6-0)

In the present paper the investigations for guest molecules in  $Zn(tbip)$  have been extended to methane,  $CO<sub>2</sub>$ , and methanol, which are different in molecular sizes and charges. The surprising effect (maximum) found for ethane does not appear for methane,  $CO<sub>2</sub>$  and even methanol, but is obviously connected with the special properties of the ethane molecules. Additionally, the diffusion of mixtures of those guest molecules in Zn(tbip) have

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#### ABSTRACT

The self-diffusion of three equimolar mixtures in the metal-organic framework Zn(tbip) has been investigated by molecular dynamics simulations. The simulations take due account of lattice flexibility. The diffusional characteristics are discussed in relation to molecule properties and lattice geometry. The results show that Zn(tbip) may be a useful material for separating methane/ethane and  $CO<sub>2</sub>/ethane$  mixtures at low concentrations, and  $CO<sub>2</sub>/methanol$  mixtures at high concentrations.

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been examined as well because the curvature of the channel walls lets us expect that molecules of different sizes will show different diffusive behavior making Zn(tbip) possibly useful for separation purposes. These systems are investigated in detail in this study.

### 2. Model and simulations

In this study,  $CO<sub>2</sub>$  was modeled as a three Lennard–Jones sites model with charges centered at each atom  $(q_c = 0.6512e$  and  $q_{\rm o}$  =  $-0.3256$ e) with bonds length C–O of 1.16 A, and the interaction parameters were taken from the work of Krishna et al. [\[7,8\]](#page-6-0) as listed in [Table 1.](#page-1-0) Using this model, they performed MD simulations to study the  $CO<sub>2</sub>$  and  $CO<sub>2</sub>/$ methane mixture in CHA and DDR zeolite at 300 K, and reported the  $CO<sub>2</sub>$  self-diffusivity in the range of  $0.1 - 5.0 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup>.

Methane was modeled by the united atom model, and ethane was modeled as two united atoms with a fixed bond length of 1.53 Å which is the same model used in our previous work [\[4,5\].](#page-6-0) The intermolecular potential parameters of methane and ethane were taken from the transferable potentials for phase equilibria (TraPPE) model [\[9\]](#page-6-0), also given in [Table 1](#page-1-0). Using this model, Krishna and van Baten [\[10\]](#page-6-0) reported the self-diffusivity of methane in Zn(tbip) (rigid framework) in the range of  $10^{-11}-10^{-8}$  m<sup>2</sup> s<sup>-1</sup>. Skoulidas and Sholl [\[11\]](#page-6-0) reported the values in the range of  $2-3 \times 10^{-8}$  m<sup>2</sup> s<sup>-1</sup> for methane in IRMOF-1 at room temperature. Garberoglio and Vallauri [\[12\]](#page-6-0) reported values in the range of  $7.7 - 22.5 \times 10^{-8}$  m<sup>2</sup> s<sup>-1</sup> for methane in 2D–COFs at 289 K.

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<span id="page-1-0"></span>Table 1 LJ and Coulomb potential parameters of guest molecules used in this study.

Adsorbate	Site-site	$\epsilon$ (k[/mol)	$\sigma$ (Å)	Charge $(e)$	Bond $(\AA)$		
CH <sub>4</sub>	CH <sub>4</sub>	1.2305	3.730	$\Omega$			
$C_2H_6$	CH <sub>3</sub>	0.8148	3.750	$\Omega$	$1.53$ ; (C-C)		
CO <sub>2</sub>	C	0.2339	2.757	0.6512	$1.16$ ; (C=O)		
	$\Omega$	0.6694	3.033	$-0.3256$			
CH <sub>3</sub> OH	C	0.6696	3.475	$-0.0930$	1.105; $(C-H_C)$		
	$H_C$	0.1592	2.450	0.100	$1.420$ ; (C-O)		
	$\Omega$	0.9533	2.860	$-0.432$	$0.945$ ; $(H0-0)$		
	H <sub>0</sub>			0.225			

Table 2

Bonded interaction parameters for the flexible methanol molecule used in this study.

$i - i$	$k_r$ (kJ/mol· $\AA^2$ )		$r_0(\AA)$	
<b>Bond stretching</b>				
$C-H_C$	2852.11		1.105	
$C=0$	3215.86		1.420	
$H_0$ –0	3451.92		0.945	
Angle bending $i - j - k$	$k_{\theta}$ (kJ/mol·rad <sup>2</sup> )		$\theta_0$ (degree)	
$C - O - H_0$	540.318		108.32	
$Hc-C-0$	530.669		106.90	
$H_C$ –C– $H_C$	424.535		108.38	
$i-i-k-l$	$k_{\phi}$ (kJ/mol)	$\phi_0$ (degree)	α	m
<b>Torsion</b>				
$H_C - C - O - H_0$	0.7352	180.0	1.0	3

However, larger values of  $\approx 1.7 \times 10^{-7}$   $\mathrm{m}^2$  s<sup>-1</sup> have been found experimentally by Stallmach et al. [\[13\]](#page-6-0) for methane in IRMOF-1.

The flexible methanol molecule was modeled by bonding, bondbending, and torsion potentials, as given in Eq. (1). Non-bonded interactions acting between methanol molecules were described by the Coulomb and Lennard–Jones potentials, as expressed by Eq. (2). Both bonded and non-bonded potential parameters were taken from the work of Plant et al. [\[14\]](#page-6-0) for methanol diffusion in the NaY zeolite as listed in Tables 1 and 2. The validity of these force field parameters was confirmed by an agreement of the diffusion coefficient of methanol obtained in the liquid phase by simulation to be 1.365  $\times$  10<sup>-9</sup> m<sup>2</sup> s<sup>-1</sup> at an ambient temperature with the corresponding experimental results of  $1.3 \times 10^{-9}$  m<sup>2</sup> s<sup>-1</sup> [\[15\].](#page-6-0) In addition, Nanok et al. [\[16\]](#page-6-0) also used these parameters to study the methanol in NaX zelozite. Their adsorption structure results agree well with the experimental IR spectroscopic data, and the self-diffusivity values are in the range of 1.0–1.2  $\times$  10<sup>-9</sup> m<sup>2</sup> s<sup>-1</sup>

$$
U_{\text{methanol}} = \frac{1}{2}k_r(r - r_0)^2 + \frac{1}{2}k_\theta(\theta - \theta_0)^2 + k_\phi[1 + \alpha \cos(m\phi - \phi_0)].
$$
\n(1)

The force field parameters for the flexible Zn(tbip) framework were taken from our previous work [\[4,5\],](#page-6-0) and they are described in detail in the supplementary material to [\[4\].](#page-6-0) To complete them, the non-bonded interactions between the guest–guest as well as the guest-Zn(tbip) molecules were modeled by the LJ and Coulombic potential given by

$$
U(r_{ij}) = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}}, \qquad (2)
$$

where  $\epsilon_{ij}$  is the LJ well-depth,  $\sigma_{ij}$  is the LJ diameter, and  $r_{ij}$  is the distance between two interacting atoms i and j. The Lorenz–Berthelot mixing rules were used to obtain the cross potentials  $\sigma_{ij} = (\sigma_i + \sigma_j)/2$  and  $\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}$ .



Fig. 1. The self-diffusivities of  $CO<sub>2</sub>$  and  $C<sub>2</sub>H<sub>6</sub>$  both for pure components and 1:1 mixture in Zn(tbip) flexible framework.

### Table 3

Self-diffusivities of equimolar mixtures of  $CO<sub>2</sub>/eth$ ane, methane/ethane,  $CO<sub>2</sub>/meth$ anol, and their pure components in Zn(tbip) flexible framework for the range of studied concentrations.

Asorbates	Components	$D_s$ (10 <sup>-8</sup> m <sup>2</sup> s <sup>-1</sup> )
CH <sub>4</sub>	Pure	$0.58 - 1.60$
	$CH_4/C_2H_6$	$0.09 - 0.95$
CO <sub>2</sub>	Pure	$0.30 - 0.56$
	CO <sub>2</sub> /CH <sub>3</sub> OH	$0.11 - 0.39$
	$CO_2/C_2H_6$	$0.09 - 0.36$
CH <sub>3</sub> OH	Pure	$0.09 - 0.24$
	CO <sub>2</sub> /CH <sub>3</sub> OH	$0.03 - 0.30$
C <sub>2</sub> H <sub>6</sub>	Pure	$0.09 - 0.15$
	$CH_4/C_2H_6$	$0.04 - 0.15$
	$CO_2/C_2H_6$	$0.04 - 0.14$



Fig. 2. The cross section area of the window as a function of concentration for pure component of methane, CO<sub>2</sub>, methanol and ethane in Zn(tbip) flexible framework. The cross section areas are calculated in the NVT ensemble.

Our molecular dynamics simulations of methane/ethane,  $CO<sub>2</sub>/$ ethane and  $CO<sub>2</sub>/method$  mixture in Zn(tbip) have been carried out, like the earlier simulations of single component ethane diffusion in Zn(tbip) [\[4,5\]](#page-6-0) using the DL\_POLY simulation package [\[17\]](#page-6-0) on a Linux workstation cluster. The simulation box has the dimensions of 28.863  $\times$  49.992  $\times$  39.855 Å. This contains five unit cells of Zn(tbip) and comprises of 5220 framework atoms. Periodic

<span id="page-2-0"></span>

Fig. 3. The center-of-mass distribution of a CO<sub>2</sub> and ethane molecule projected into the xy plane tracked every 0.5 ps during a simulation period of 10 ns for CO<sub>2</sub>: ethane = 1:1 mixture in Zn(tbip) flexible framework.

boundary conditions have been applied to all three directions. The long-range electrostatic interactions between the Zn(tbip) framework atoms have been computed using the Ewald summation technique, and the short-range van der Waals interactions between framework atoms and between framework and guest molecules have been computed up to a cutoff radius of 12 Å. The MD simulations were performed in the NVE ensemble at the temperature of 298 K. The equations of motion were integrated by using the velocity Verlet algorithm with a time step of 1 fs. In each loading, every channel of Zn(tbip) is loaded with an equal number of guest molecules. The starting configuration was used as input for 500 ps equilibration period at 298 K. After that, velocity rescaling was switched off and an equilibration of 500 ps was performed to ensure that there were no further drifts. Then, the production runs have been conducted for 10 ns. During the production runs, the coordinates have been stored every 100 fs for further analysis.

By using Einstein's relation [\[18\],](#page-6-0) Eq. (3), we calculated onedimensional self-diffusion coefficients for each kind of molecule pure and in mixture from the slope of the mean-squared displacement (MSD) as function of time

$$
D_{s,i} = \frac{1}{2N_i} \lim_{\Delta t \to \infty} \frac{1}{\Delta t} \left\langle \sum_{l=1}^{N_i} \left[ z_{l,i}(t + \Delta t) - z_{l,i}(t) \right]^2 \right\rangle
$$
 (3)

where  $D_{s,i}$  is the center of mass self-diffusivity of molecules of species *i*,  $N_i$  is the number of molecules of species *i*, and  $z_{Li}(t)$  is the position of molecule  $l$  of species  $i$  at any time  $t$ .



Fig. 4. The self-diffusivities of methane and ethane both for pure components and 1:1 mixture in Zn(tbip) flexible framework.

<span id="page-3-0"></span>

Fig. 5. The center-of-mass distribution of a methane and ethane molecule projected into the xy plane tracked every 0.5 ps during a simulation period of 10 ns for methane:ethane = 1:1 mixture in Zn(tbip) flexible framework.

From the self-diffusivities the diffusion selectivities have been further examined. The diffusion selectivity [\[8\]](#page-6-0);  $\alpha^{\text{diff}}_{\text{A,B}}$ , is defined as the ratio of the self-diffusivities of molecules of species A and of species B in a binary mixture, so that  $\alpha^{\text{diff}}_{\text{A,B}}$  is given by

$$
\alpha_{\rm A,B}^{\rm diff} = \frac{D_{\rm s,A}}{D_{\rm s,B}}\tag{4}
$$

where  $D_{s,A}$  is the self-diffusivity of molecules of species A, and  $D_{s,B}$  is the self-diffusivity of molecules of species B. Values of  $\alpha_{\rm A,B}^{\rm diff}$  greater than unity imply that A is diffusing faster than B.

## 3. Results

The results showed that the maximum in the self-diffusivity of ethane as a function of loading that was shown to be present only in the flexible lattice appears also in the mixture. The reasons for this maximum have been explained in [\[5\].](#page-6-0) For the other diffusants examined in this paper pure and in mixture the loading dependence of the self diffusivity is a monotonic one. This is the common form of loading-dependence of self-diffusivities which arises from the mutual steric hindrance of diffusing molecules and was observed for many other adsorbate molecules in many MOFs [\[10,19–21\].](#page-6-0)

In the mixtures the slower molecule always slowed down the mobility of the faster one and the faster one somewhat drags the slowly diffusing one.

### 3.1.  $CO_2$ /ethane mixture in Zn(tbip)

Self-diffusivities of equimolar mixtures of  $CO<sub>2</sub>/eth$  and of pure components in Zn(tbip) flexible framework as function of the total concentration are shown in [Fig. 1.](#page-1-0) The data are also given in [Table 3](#page-1-0) for completenes. Both, pure and in mixture,  $CO<sub>2</sub>$ 

self-diffusivity is found to be higher than that of  $C_2H_6$  over the entire range of total concentration,  $c_t$ .

[Fig. 3](#page-2-0) shows the center-of-mass density distribution of the  $CO<sub>2</sub>/$ ethane mixture in Zn(tbip) at different total loading. At low loading ethane molecules preferably adsorb near the center of the channel and the middle of the segment.  $CO<sub>2</sub>$  on the one hand has a dipole moment and on the other hand is more slender can diffuse around the whole segment and can also diffuse through the window into the adjacent segments. Because of this the self-diffusivity of  $CO<sub>2</sub>$ is higher than that of ethane. At high total concentrations, the mutual repulsion between molecules in the same segment causes the ethane molecule to be significantly adsorbed within the leaf



Fig. 6. The self-diffusivities of  $CO<sub>2</sub>$  and methanol for pure components in rigid and flexible Zn(tbip) framework.

positions. By contrast, however,  $CO<sub>2</sub>$  is still fastly diffusing in the same segment and hopping to the adjacent segments. In consequence, the self-diffusivity of  $CO<sub>2</sub>$  is still higher than that of ethane.

#### 3.2. Methane/ethane mixture in Zn(tbip)

In [Fig. 4](#page-2-0) the self-diffusivities of equimolar mixtures of methane/ ethane and pure components in Zn(tbip) with flexible framework as a function of the total concentration are shown. Methane selfdiffusivities in both pure and mixture are found to be larger than that of ethane. This is because methane is smaller than ethane.

[Fig. 5](#page-3-0) shows the center-of-mass distribution of the methane/ ethane mixture in Zn(tbip) at different total concentration. It can



Fig. 7. The self-diffusivities of  $CO<sub>2</sub>$  and methanol both for pure components and 1:1 mixture in Zn(tbip) flexible framework.

be seen that at both, low and high concentrations the smaller and faster diffusing methane molecule, does not only easily diffuse from one leaf site to another leaf site in the same segment but also fastly diffuses through the ethane molecules and performs hops between the segments. Consequently, the self-diffusivity of methane is higher than that of ethane. The diffusion of ethane again shows a maximum at intermediate loadings. At highest loadings the steric hindrance effects cause a decrease for both methane and ethane diffusivity. In [Fig. 5,](#page-3-0) we also observe that ethane molecules still prefer to locate in the center region of the channel and to adsorb closer to the windows more than in the case of CO2/ethane mixtures.

### 3.3.  $CO<sub>2</sub>/method$  mixture in Zn(tbip)

As we have mentioned above,  $CO<sub>2</sub>$  is a polar and more slender molecule than ethane, so that the surprising effect of the flexible lattice (maximum in the loading dependence) found for ethane is not to be expected and does not appear for  $CO<sub>2</sub>$ . This behavior caused us to extend the investigation of Zn(tbip) with flexible lattice to methanol as guest molecule, which is also a polar molecule but has stronger confinement than  $CO<sub>2</sub>$ , and mixtures of  $CO<sub>2</sub>$  and methanol. In [Fig. 6](#page-3-0) it can be seen that the lattice flexibility affects the self-diffusivity of methanol while that of  $CO<sub>2</sub>$  is nearly unaffected by the flexibility.

Fig. 7 shows the self-diffusivity of  $CO<sub>2</sub>$  and methanol, in both the pure and the mixture studies, as a function of total concentration. The  $CO<sub>2</sub>$  self-diffusivity is higher than that of methanol for the entire range of total concentrations. The density dependence shows the expected behavior discussed above for all mixtures.

Fig. 8 shows the center-of-mass distribution of  $CO<sub>2</sub>$  and methanol mixtures in Zn(tbip) at low and high total concentrations. It can be seen that methanol molecules prefer to be located at the leaf positions, and then preferably are adsorbed and sticking together



Fig. 8. The center-of-mass distribution of a CO<sub>2</sub> and methanol molecule projected into the xy plane tracked every 0.5 ps during a simulation period of 10 ns for  $CO<sub>2</sub>$ :methanol = 1:1 mixture in Zn(tbip) flexible framework.

<span id="page-5-0"></span>

Fig. 9. The typical arrangement of CO<sub>2</sub> and methanol in a channel of Zn(tbip) at total concentration of 24 molecules per unit cell, also the typical C2–C<sub>m</sub> and C6–C<sub>m</sub> distance are presented in angstrom, giving values consistent with those observed the RDfs as shown in Fig. 10.

more and more when the loading increases. This behavior is also found in case of its pure components (not shown). This is a consequence of the electrostatic interactions between methanol molecules, as well as between methanol molecules and the framework. Because methanol prefers to be located at the leaf positions, the strong change of the framework at window regions found in the case of ethane, cannot be found in the case of methanol, as



Fig. 10. The radial distribution function;  $g(r)$ , for C2–C<sub>m</sub> and C6–C<sub>m</sub>, where C2, C6 are carbon atoms of Zn(tbip), see Fig. 9 for its coordinates,  $C_m$  is carbon atoms of methanol. The data are shown for different total concentrations of equimolar  $CO<sub>2</sub>/$ methanol mixture in Zn(tbip) flexible framework.

shown in [Fig. 2](#page-1-0). Hence, the methanol self-diffusivity does not show a maximum when the concentration is increased.

Because the  $CO<sub>2</sub>$  molecule is more slender than methanol the  $CO<sub>2</sub>$  self-diffusivity is larger than that of methanol for the full loading range studied. With increasing concentration both  $CO<sub>2</sub>$  and methanol self-diffusivities decrease monotonically.

# 3.4. Radial distribution functions

In addition, to gain insight into the typical locations and arrangements of methanol inside the segment of Zn(tbip) the RDFs of C2– $C_m$  and C6– $C_m$  have been evaluated. C2 represents the carbon atoms in the organic linker, or benzene groups, of Zn(tbip), C6 is the carbon atom that connects the methyl groups at the window, and  $C_m$  is the carbon atom of methanol, for each total concentration of the  $CO<sub>2</sub>/methanol$  mixture in  $Zn(tbip)$  that has been evaluated. The results are given in Fig. 10. The  $C2 - C<sub>m</sub>$  RDF shows the typical first peak at about 4.00 Å, and about 4.75 Å for the  $C_0-C_m$ . For both  $C_0-C_m$  and  $C_0-C_m$  the intensity of the first peak of  $g(r)$  gradually increases with increasing mixture loading. These positions are consistent with the typical snapshots of the  $CO<sub>2</sub>/$ ethanol mixture in Zn(tbip) that are shown in Fig. 9. These snapshots show that in the  $CO<sub>2</sub>/methanol$  mixture in Zn(tbip), methanol molecules are preferentially adsorbed in the leaf positions of the framework. Simultaneously, the methanol



Fig. 11. The diffusion selectivities of methane/ethane,  $CO<sub>2</sub>/$ ethane and  $CO<sub>2</sub>/$ methanol mixtures in Zn(tbip) flexible framework.

<span id="page-6-0"></span>molecules try to turn their axis perpendicular to the benzene ring of the framework, and to put the methyl group close to this ring.

#### 3.5. Self-diffusion selectivity

The diffusion selectivities for the  $CO<sub>2</sub>/eth$  and, the methane/ethane and the  $CO<sub>2</sub>/methanol$  mixtures within  $Zn(tbip)$  with flexible framework were calculated using Eq. (4), as shown in [Fig. 11](#page-5-0). The  $\alpha^{\text{diff}}_{\text{CO}_2,\text{C}_2\text{H}_6}$  values are in the range of 2–6 for the total concentrations;  $c_t <$  12 molecules per unit cell, and then  $\alpha^{\text{diff}}_{\text{CO}_2,\text{C}_2\text{H}_6}$  decreases when the total concentration is increased. This behavior indicates that for the  $CO<sub>2</sub>/eth$  ethane mixture, diffusion is strongly selective at low loading where in average each segment of the framework is occupied by less than one ethane molecule. In the case of methane/ethane mixtures, the  $\alpha_{\text{CH}_4,\text{C}_2\text{H}_6}^{\text{diff}}$  values are in the range of 6–12 and have the same trend as  $\alpha_{\text{CO}_2,\text{C}_2\text{H}_6}^{\text{diff}}$  at low loading. In the case of  $CO_2/m$ ethanol mixtures, it can be seen that the  $\alpha_{CO_2,CH_3OH}^{diff}$  values gradually increase with increasing concentration in the range of 1.0–3.5 for the range of studied concentrations, indicating that the diffusion is selective for  $CO<sub>2</sub>$  over methanol, especially at high concentrations.

### 4. Conclusions

In this work, molecular dynamics simulations have been used to investigate diffusion of three equimolar binary mixtures of  $CO<sub>2</sub>/$ ethane, methane/ethane and  $CO<sub>2</sub>/methanol$ , as well as pure component diffusion of methane,  $CO<sub>2</sub>$ , methanol and ethane molecules. The results showed that the maximum in the self-diffusivity of ethane as a function of loading that was shown to be present only in the flexible lattice appears also in the mixture. The reasons for this maximum have been explained in [5]. Hence, the simulations of some technically important mixtures containing ethane in Zn(tbip) presented in this paper had clearly to be done in the flexible lattice. Moreover, additional simulations of pure  $CO<sub>2</sub>$  and methanol show that for methanol there is also non-negligible influence of the lattice flexibility.

Methane is a more compact molecule than ethane, thus the methane self-diffusivities are larger than for ethane. With increasing concentration, methane molecules are preferably located in the leaf site. And therefore the methane self-diffusivity decreases only monotonically.

 $CO<sub>2</sub>$  is a polar and more slender molecule than ethane, thus the  $CO<sub>2</sub>$  self-diffusivities are larger than for ethane. An increase in the  $CO<sub>2</sub>$  self-diffusivity is not observed.

Methanol is also a polar molecule with a slightly smaller molecular size compared to ethane, thus the methanol self-diffusivities are larger than for ethane. When the concentration increases, methanol molecules are preferably adsorbed and sticking together at the leaf sites, and therefore an increase in its self-diffusivity is also not observed.

In mixtures, the self-diffusivities of all diffusing molecules calculated at different total concentrations show that the faster diffusing molecules accelerate the slower diffusing molecules whereas, in turn, the slower molecules act to slow down the faster molecules through the channel of Zn(tbip) framework.

The diffusion selectivities for methane/ethane,  $CO<sub>2</sub>/eth$ ane and  $CO<sub>2</sub>/methanol give values in the range of 1–12, but they show dif$ ferent trends.

For methane/ethane and  $CO<sub>2</sub>/eth$ ane mixtures, the diffusion selectivities have high values at seemingly low loadings, but high value were found at high loadings in the case  $CO<sub>2</sub>/methanol$  mixture. This is indicating that Zn(tbip) may be a useful material for separating methane/ethane and  $CO<sub>2</sub>/eth$ ane mixtures at low concentrations, and  $CO<sub>2</sub>/methanol$  mixtures at high concentrations.

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